

# Study Guide and Intervention

Alg1 15.0

## Weighted Averages

### Mixture Problems

**Weighted Average**

The weighted average  $M$  of a set of data is the sum of the product of each number in the set and its weight divided by the sum of all the weights.

**Mixture Problems** are problems where two or more parts are combined into a whole. They involve weighted averages. In a mixture problem, the weight is usually a price or a percent of something.

**Example**

**Delectable Cookie Company** sells chocolate chip cookies for \$6.95 per pound and white chocolate cookies for \$5.95 per pound. How many pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies to obtain a mixture that sells for \$6.75 per pound.

Let  $w$  = the number of pounds of chocolate chip cookies

	Number of Pounds	Price per Pound	Total Price
Chocolate Chip	$w$	6.95	$6.95w$
White Chocolate	4	5.95	$4(5.95)$
Mixture	$w + 4$	6.75	$6.75(w + 4)$

Equation:  $6.95w + 4(5.95) = 6.75(w + 4)$

Solve the equation.

$6.95w + 4(5.95) = 6.75(w + 4)$	Original equation
$6.95w + 23.80 = 6.75w + 27$	Simplify.
$6.95w + 23.80 - 6.75w = 6.75w + 27 - 6.75w$	Subtract $6.75w$ from each side.
$0.2w + 23.80 = 27$	Simplify.
$0.2w + 23.80 - 23.80 = 27 - 23.80$	Subtract 23.80 from each side.
$0.2w = 3.2$	Simplify.
$w = 16$	Simplify.

16 pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies.

**Exercises**

- SOLUTIONS** How many grams of sugar must be added to 60 grams of a solution that is 32% sugar to obtain a solution that is 50% sugar?
- NUTS** The Quik Mart has two kinds of nuts. Pecans sell for \$1.55 per pound and walnuts sell for \$1.95 per pound. How many pounds of walnuts must be added to 15 pounds of pecans to make a mixture that sells for \$1.75 per pound?
- INVESTMENTS** Alice Gleason invested a portion of \$32,000 at 9% interest and the balance at 11% interest. How much did she invest at each rate if her total income from both investments was \$3,200.
- MILK** Whole milk is 4% butterfat. How much skim milk with 0% butterfat should be added to 32 ounces of whole milk to obtain a mixture that is 2.5% butterfat?

# Study Guide and Intervention *(continued)*

## Weighted Averages

**Uniform Motion Problems** Motion problems are another application of weighted averages. **Uniform motion problems** are problems where an object moves at a certain speed, or rate. Use the formula  $d = rt$  to solve these problems, where  $d$  is the distance,  $r$  is the rate, and  $t$  is the time.

**Example** Bill Gutierrez drove at a speed of 65 miles per hour on an expressway for 2 hours. He then drove for 1.5 hours at a speed of 45 miles per hour on a state highway. What was his average speed?

$$M = \frac{65 \cdot 2 + 45 \cdot 1.5}{2 + 1.5} \quad \text{Definition of weighted average}$$

$$\approx 56.4 \quad \text{Simplify.}$$

Bill drove at an average speed of about 56.4 miles per hour.

### Exercises

- TRAVEL** Mr. Anders and Ms. Rich each drove home from a business meeting. Mr. Anders traveled east at 100 kilometers per hour and Ms. Rich traveled west at 80 kilometers per hour. In how many hours were they 100 kilometers apart?
- AIRPLANES** An airplane flies 750 miles due west in  $1\frac{1}{2}$  hours and 750 miles due south in 2 hours. What is the average speed of the airplane?
- TRACK** Sprinter A runs 100 meters in 15 seconds, while sprinter B starts 1.5 seconds later and runs 100 meters in 14 seconds. If each of them runs at a constant rate, who is further in 10 seconds after the start of the race? Explain.
- TRAINS** An express train travels 90 kilometers per hour from Smallville to Megatown. A local train takes 2.5 hours longer to travel the same distance at 50 kilometers per hour. How far apart are Smallville and Megatown?
- CYCLING** Two cyclists begin traveling in the same direction on the same bike path. One travels at 15 miles per hour, and the other travels at 12 miles per hour. When will the cyclists be 10 miles apart?
- TRAINS** Two trains leave Chicago, one traveling east at 30 miles per hour and one traveling west at 40 miles per hour. When will the trains be 210 miles apart?