## Lesson 8-8

## Example 1 Solve Inequalities by Dividing

 Solve $4 \boldsymbol{m}<96$. Check your solution.$4 m<96 \quad$ Write the inequality.
$\frac{4 m}{4}<\frac{96}{4} \quad$ Divide each side by 4 .
$m<24$ Simplify.
The solution is $m<24$.
Example 2 Solve Inequalities by Multiplying
Solve $\frac{1}{8} x \geq-4$. Check your solution.

$$
\begin{aligned}
\frac{1}{8} x & \geq-4 & & \text { Write the inequality. } \\
8\left(\frac{1}{8} x\right) & \geq 8(-4) & & \text { Multiply each side by } 8 . \\
x & \geq-32 & & \text { Simplify. }
\end{aligned}
$$

The solution is $x \geq-32$. You can check this solution by substituting -32 and a number greater than -32 into the inequality.

Example 3 Multiply or Divide by a Negative Number
Solve $\frac{n}{-6}<3$. Check your solution.

$$
\begin{aligned}
\frac{n}{-6} & <3 & & \text { Write the inequality. } \\
-6\left(\frac{n}{-6}\right) & >-6(3) & & \text { Multiply each side by }-6 \text { and reverse the inequality symbol. } \\
n & >-18 & & \text { Check this result. }
\end{aligned}
$$

## Example 4 Multiply or Divide by a Negative Number

Solve $-72 \geq-9 w$. Check your solution.

$$
\begin{aligned}
-72 & \geq-9 w & & \text { Write the inequality. } \\
\frac{-72}{-9} & \leq \frac{-9 w}{-9} & & \text { Divide each side by }-9 \text { and reverse the inequality symbol. } \\
8 & \leq w \text { or } w \geq 8 & & \text { Check this result. }
\end{aligned}
$$

## Example 5 Real-World Example

REPAIRS Mrs. Jacobs is hiring a technician to repair her broken refrigerator. The technician charges $\mathbf{\$ 5 0}$ for a service call, plus $\mathbf{\$ 2 5}$ per hour for labor. Write and solve an inequality to find how many hours the technician has to complete the job, if Mrs. Jacobs wants to pay no more than $\mathbf{\$ 1 2 5}$. Interpret the solution.

The phrase no more than means less than or equal to. Let $h=$ the number of hours the technician works. Then write the inequality.

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    \(50+25 h \leq 125 \quad\) Write the inequality.
\(50-50+25 h \leq 125-50 \quad\) Subtract 50 from each side.
    \(25 h \leq 75 \quad\) Simplify.
    \(\frac{25 h}{25} \leq \frac{75}{25} \quad\) Divide each side by 25 .
    \(h \leq 3 \quad\) Simplify.
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The technician has no more than 3 hours to complete the job, so Mrs. Jacobs will not have to pay more than $\$ 125$.

