

Glencoe McGraw-Hill

Study Notebook

Pre-Algebra



Mc
Graw
Hill

Glencoe

The McGraw-Hill Companies



Copyright © by The McGraw-Hill Companies, Inc. All rights reserved. Except as permitted under the United States Copyright Act, no part of this publication may be reproduced or distributed in any form or by any means, or stored in a database or retrieval system, without prior written permission of the publisher.

Send all inquiries to:
Glencoe/McGraw-Hill
8787 Orion Place
Columbus, OH 43240

ISBN: 978-0-07-890748-7
MHID: 0-07-890748-9

Printed in the United States of America

1 2 3 4 5 6 7 8 9 10 047 14 13 12 11 10 09 08

Contents

Chapter 1

Before You Read	1
Key Concepts	2
1-1 Words and Expressions	3
1-2 Variables and Expressions.....	5
1-3 Properties	7
1-4 Ordered Pairs and Relations.....	9
1-5 Words, Equations, Tables, and Graphs.....	11
1-6 Scatter Plots	13
Tie It Together	15
Before the Test	16

Chapter 2

Before You Read	17
Key Concepts	18
2-1 Integers and Absolute Value	19
2-2 Adding Integers	21
2-3 Subtracting Integers	23
2-4 Multiplying Integers	25
2-5 Dividing Integers.....	27
2-6 Graphing in Four Quadrants	29
2-7 Translations and Reflections on the Coordinate Plane.....	31
Tie It Together	33
Before the Test	34

Chapter 3

Before You Read	35
Key Concepts	36
3-1 Fractions and Decimals.....	37
3-2 Rational Numbers.....	39
3-3 Multiplying Rational Numbers.....	41
3-4 Dividing Rational Numbers.....	43
3-5 Adding and Subtracting Like Fractions.....	45
3-6 Adding and Subtracting Unlike Fractions.....	47
Tie It Together	49
Before the Test	50

Chapter 4

Before You Read	51
Key Concepts	52
4-1 The Distributive Property.....	53
4-2 Simplifying Algebraic Expressions	55
4-3 Solving Equations by Adding or Subtracting	57
4-4 Solving Equations by Multiplying or Dividing.....	59
4-5 Solving Two-Step Equations	61
4-6 Writing Equations	63
Tie It Together	65
Before the Test	66

Chapter 5

Before You Read	67
Key Concepts	68
5-1 Perimeter and Area	69
5-2 Solving Equations with Variables on Each Side.....	71
5-3 Inequalities	73
5-4 Solving Inequalities	75
5-5 Solving Multi-Step Equations and Inequalities	77
Tie It Together	79
Before the Test	80

Chapter 6

Before You Read	81
Key Concepts	82
6-1 Ratios	83
6-2 Unit Rates.....	85
6-3 Converting Rates and Measurements.....	87
6-4 Proportional and Nonproportional Relationships.....	89
6-5 Solving Proportions	91
6-6 Scale Drawings and Models.....	93
6-7 Similar Figures	95
6-8 Dilations.....	97
6-9 Indirect Measurement.....	99
Tie It Together	101
Before the Test	102

Chapter 7

Before You Read	103
Key Concepts	104
7-1 Fractions and Percents	105
7-2 Fractions, Decimals, and Percents	107
7-3 Using the Percent Proportion	109
7-4 Find Percent of a Number Mentally	111
7-5 Using Percent Equations.....	113
7-6 Percent of Change	115
7-7 Simple and Compound Interest.....	117
7-8 Circle Graphs	119
Tie It Together	121
Before the Test	122

Chapter 8

Before You Read	123
Key Concepts	124
8-1 Functions.....	125
8-2 Sequences and Equations	127
8-3 Representing Linear Functions	129
8-4 Rate of Change	131
8-5 Constant Rate of Change and Direct Variation.....	133
8-6 Slope	135

8-7 Slope-Intercept Form.....	137
8-8 Writing Linear Equations	139
8-9 Prediction Equations	141
8-10 Systems of Equations.....	143
Tie It Together	145
Before the Test	146

Chapter 9

Before You Read	147
Key Concepts	148
9-1 Powers and Exponents	149
9-2 Prime Factorization	151
9-3 Multiplying and Dividing Monomials	153
9-4 Negative Exponents	155
9-5 Scientific Notation.....	157
9-6 Powers of Monomials.....	159
9-7 Linear and Nonlinear Functions	161
9-8 Quadratic Functions	163
9-9 Cubic and Exponential Functions.....	165
Tie It Together	167
Before the Test	168

Chapter 10

Before You Read	169
Key Concepts	170
10-1 Squares and Square Roots.....	171
10-2 The Real Number System.....	173
10-3 Triangles.....	175
10-4 The Pythagorean Theorem	177
10-5 The Distance Formula.....	179
10-6 Special Right Triangles	181
Tie It Together	183
Before the Test	184

Chapter 11

Before You Read	185
Key Concepts	186
11-1 Angle and Line Relationships.....	187
11-2 Congruent Triangles.....	189
11-3 Rotations	191
11-4 Quadrilaterals	193
11-5 Polygons.....	195
11-6 Area of Parallelograms, Triangles, and Trapezoids.....	197
11-7 Circles and Circumference	199
11-8 Area of Circles.....	201
11-9 Area of Composite Figures	203
Tie It Together	205
Before the Test	206

Chapter 12

Before You Read	207
Key Concepts	208
12-1 Three-Dimensional Figures	209
12-2 Volume of Prisms	211
12-3 Volume of Cylinders	213
12-4 Volume of Pyramids, Cones and Spheres	215
12-5 Surface Area of Prisms	217
12-6 Surface Area of Cylinders	219
12-7 Surface Area of Pyramids and Cones	221
12-8 Similar Solids.....	223
Tie It Together	225
Before the Test	226

Chapter 13

Before You Read	227
Key Concepts	228
13-1 Measures of Central Tendency	229
13-2 Stem-and-Leaf Plots.....	231
13-3 Measures of Variation	233
13-4 Box-and-Whisker Plots.....	235
13-5 Histograms	237
13-6 Theoretical and Experimental Probability.....	239
13-7 Using Sampling to Predict.....	241
13-8 Counting Outcomes.....	243
13-9 Permutations and Combinations	245
13-10 Probability of Compound Events.....	247
Tie It Together	249
Before the Test	250

Note-Taking Tips

Your notes are a reminder of what you learned in class. Taking good notes can help you succeed in mathematics. The following tips will help you take better classroom notes.

- Before class, ask what your teacher will be discussing in class. Review mentally what you already know about the concept.
- Be an active listener. Focus on what your teacher is saying. Listen for important concepts. Pay attention to words, examples, and/or diagrams your teacher emphasizes.
- Write your notes as clear and concise as possible. The following symbols and abbreviations may be helpful in your note-taking.

Word or Phrase	Symbol or Abbreviation	Word or Phrase	Symbol or Abbreviation
for example	e.g.	not equal	\neq
such as	i.e.	approximately	\approx
with	w/	therefore	\therefore
without	w/o	versus	vs
and	+	angle	\angle

- Use a symbol such as a star (★) or an asterisk (*) to emphasize important concepts. Place a question mark (?) next to anything that you do not understand.
- Ask questions and participate in class discussion.
- Draw and label pictures or diagrams to help clarify a concept.
- When working out an example, write what you are doing to solve the problem next to each step. Be sure to use your own words.
- Review your notes as soon as possible after class. During this time, organize and summarize new concepts and clarify misunderstandings.

Note-Taking Don'ts

- Don't write every word. Concentrate on the main ideas and concepts.
- Don't use someone else's notes as they may not make sense.
- Don't doodle. It distracts you from listening actively.
- Don't lose focus or you will become lost in your note-taking.


 CHAPTER
1

The Tools of Algebra

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Tools of Algebra
	<ul style="list-style-type: none"> • A variable represents an unknown number or quantity.
	<ul style="list-style-type: none"> • If the order of numbers multiplied is changed, the product will also change.
	<ul style="list-style-type: none"> • A coordinate plane has an x- and a y-axis.
	<ul style="list-style-type: none"> • A scatter plot sometimes shows a trend in the data, but not always.
	<ul style="list-style-type: none"> • You need an ordered pair with two numbers to plot a point on a coordinate plane.


FOLDABLES® Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- **When you take notes, be sure to describe steps in detail.**
Include examples of questions you might ask yourself during problem solving.
- **When searching for the main idea of a lesson, ask yourself, “What is this paragraph or lesson telling me?”**
Then make certain you answer the question.

CHAPTER
1**The Tools of Algebra****Key Points**

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on variables and expressions, one fact might be that a variable is a letter or symbol used to represent an unknown value. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
1-1 Words and Expressions	
1-2 Variables and Expressions	
1-3 Properties	
1-4 Ordered Pairs and Relations	
1-5 Words, Equations, Tables, and Graphs	
1-6 Scatter Plots	

1-1 Words and Expressions

What You'll Learn

Skim the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the correct term next to each definition.

- _____ ▶ rules to follow when evaluating an expression with more than one operation
- _____ ▶ contains a combination of numbers and operations such as addition, subtraction, multiplication, and division
- _____ ▶ to find the numerical value of an expression

Vocabulary Link *Operation* is a word that is used in everyday English. Find the definition of *operation* using a dictionary. Explain how the English definition can help you remember how *operation* is used in mathematics.

Lesson 1-1

Lesson 1-1 (continued)

Main Idea

Translate Verbal Phrases into Expressions

p. 5

Details

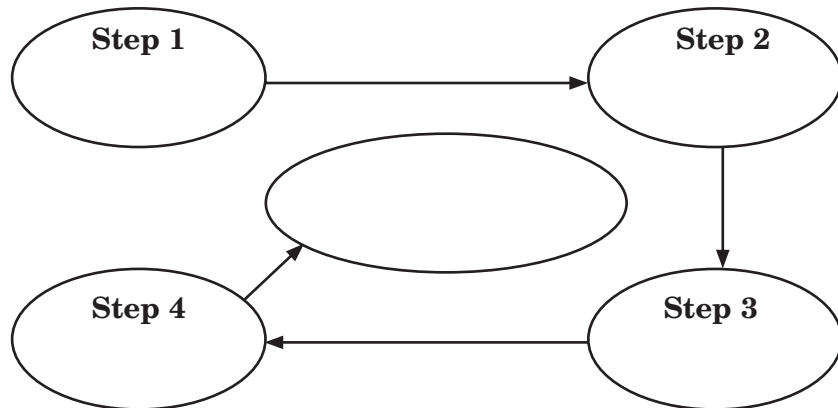
Complete the operation of the numerical expressions for each verbal phrase.

1. the number of weeks in 42 days $\rightarrow 42 \square 7$
2. the difference of 18 and 13 $\rightarrow 18 \square 13$
3. the quotient of 81 and 9 $\rightarrow 81 \square 9$
4. the total number of students if there are 7 boys and 11 girls $\rightarrow 7 \square 11$
5. the total number of tires on 14 cars $\rightarrow 14 \square 4$
6. the sum of 51 and 39 $\rightarrow 51 \square 39$
7. the product of 9 and 6 $\rightarrow 9 \square 6$
8. the cost of 4 candies at \$0.35 each $\rightarrow 4 \square 0.35$

Order of Operations

p. 6

Complete each step to evaluate $2[(7 + 9) \times 3] - 15$.



Helping You Remember

One classmate evaluates the expression $4 + 6 \div 2$ and gets an answer of 5. Another classmate evaluates the same expression and gets an answer of 7. Use the order of operations to explain which answer is correct.

1-2 Variables and Expressions

What You'll Learn

Skim the lesson. Write two things you already know about variables and expressions.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write a numerical expression for each verbal phrase. (*Lesson 1-1*)

18 books shared equally among 6 students _____

a package of 15 pencils minus 3 pencils _____

4 eggs plus 3 eggs _____

New Vocabulary Match the term with its definition by drawing a line to connect the two.

variable an expression with at least one variable and one operation

defining a variable branch of mathematics that uses symbols

algebraic expression a letter or symbol that represents an unknown value

algebra choosing a variable and the quantity it represents

Lesson 1-2 (continued)

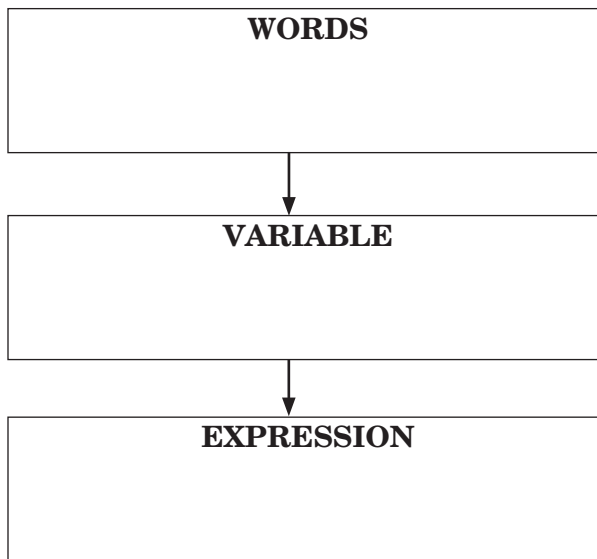
Main Idea

Algebraic Expressions and Verbal Phrases

pp. 11–12

Details

Describe the steps involved in writing algebraic expressions.



Evaluate Expressions

pp. 12–13

Evaluate each expression if $a = 3$, $b = 7$, and $c = 5$.

1. $6c \div 15 = \square$
2. $32 + 4a = \square$
3. $27a - (16 - 3c) = \square$
4. $\frac{bc}{a + 2} = \square$
5. $2b - 4a = \square$

Helping You Remember

Variable is a word used in everyday English as well as in mathematics. Write the definition of *variable*. Explain how the English definition can help you remember how *variable* is used in mathematics.

1-3 Properties

What You'll Learn

Scan Lesson 1-3. List two headings that you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

properties ▶

counterexample ▶

simplify ▶

deductive reasoning ▶

Vocabulary Link *Simplify* has a non-mathematical meaning as well. Use the word *simplify* in a non-mathematical sentence.

Lesson 1-3 (continued)

Main Idea

Details

Properties of Addition and Multiplication

pp. 18–19

Complete the table by writing the definition and an example of each property.

Property	Definition	Example
Commutative Property of Addition		
Associative Property of Multiplication		
Additive Identity		
Multiplication Identity		

Simplify Algebraic Expressions

p. 20

Simplify each expression by filling in the blanks with a variable or number.

1. $(8 + x) + 2$

+

2. $k \times (4 \times 4)$

\times

3. $3 \times (7 \times p)$

\times

4. $9 + (b + 5)$

+

Helping You Remember

In your own words, define counterexample. Tell how it is used in mathematics and why it is important.

1-4 Ordered Pairs and Relations

What You'll Learn

Skim Lesson 1-4. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

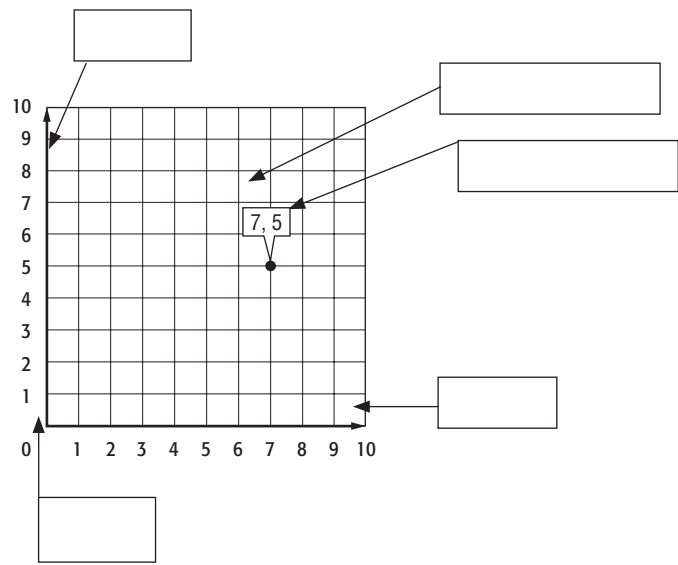
Review Vocabulary Fill in each blank with one correct term. (Lesson 1-2)

2s _____

algebraic expression ► a(n) _____ with at least one _____ and one _____

New Vocabulary Label the diagram with the correct terms.

- origin* ►
- y-axis* ►
- x-axis* ►
- x-coordinate* ►
- y-coordinate* ►



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Lesson 1-4

Lesson 1-4 (continued)

Main Idea

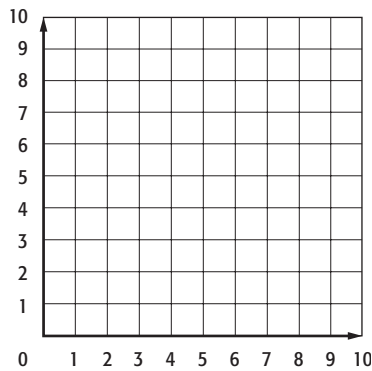
Details

Ordered Pairs

pp. 25–26

Graph each ordered pair on the coordinate plane below.

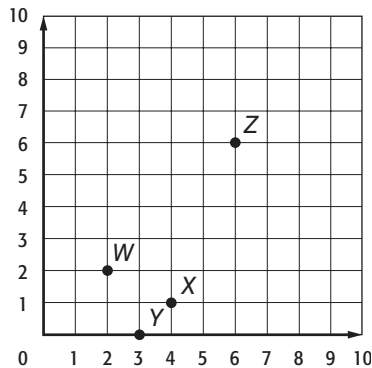
A(6, 4) **B(0, 4)** **C(2, 1)** **D(5, 0)**



Relations

p. 27

Write the relation as a table. Then write the domain and range.



x				
y				

domain:

range:

Helping You Remember

Write two examples of coordinate systems that are used in everyday life.

1-5 Words, Equations, Tables, and Graphs

What You'll Learn

Skim the Examples for Lesson 1-5. Predict two things you think you will learn about words, equations, tables, and graphs.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Explain how the Additive Identity Property and the Multiplicative Identity Property are the same. (*Lesson 1-3*)

New Vocabulary Fill in each blank with the correct term or phrase.

- function* ▶ a _____ where each member of the domain is paired with exactly one member in the _____
- equation* ▶ a mathematical _____ stating that two quantities are _____
- function rule* ▶ the _____ performed on the input in a function to get the _____
- function table* ▶ a table that lists the _____, rule, and the _____

Lesson 1-5 (continued)

Main Idea

Details

Represent Functions

p. 33

Complete each function table. Then write the rule for each function.

1. Nancy bought half as many pants as shirts.

Number of shirts	Input (x)				
Number of pants	Output (y)				

Rule:

2. The recipe calls for 3 times more cups of flour than water.

Cups of water	Input (x)				
Cups of flour	Output (y)				

Rule:

Multiple Representations

p. 34

Represent the function in three different ways.

For each 1,000 meters in altitude, the temperature, which is 35°C , decreases 6.5°C .

Helping You Remember

represented.

Name the four ways that functions can be

1-6 Scatter Plots

What You'll Learn

Scan the text in Lesson 1-6. Write two facts you learned about scatter plots as you scanned the text.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Complete the table below naming the operation, (addition, subtraction, multiplication, or division) that each verbal phrase represents. (*Lesson 1-1*)

Verbal phrase	Operation
less	
more than	
quotient	
total	
shared equally	
difference	
times	
sum	
product	

New Vocabulary Define the following term from this lesson.

scatter plot ►

Vocabulary Link A *scatter plot* can be used to determine trends between two sets of data. Find the definition of *trend* using a dictionary. Describe how *trend* relates to *scatter plots* using your own words.

Lesson 1-6

Lesson 1-6 *(continued)*

Main Idea

Details

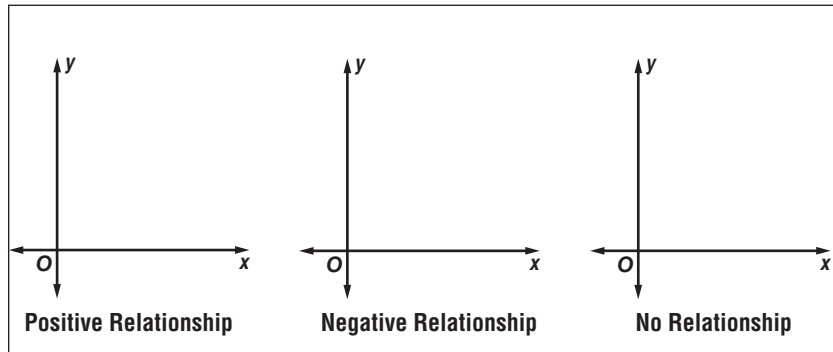
Construct Scatter Plots
p. 40

Compare and contrast the characteristics of scatter plot and a graphical representation of a function.

Scatter plot	Graph of Function

Analyze Scatter Plots
pp. 41–42

Draw a scatter plot that shows each relationship.



Helping You Remember

Describe three real life situations between quantities where the relationship is a positive relationship, a negative relationship, and no relationship.

CHAPTER
1

The Tools of Algebra

Tie It Together

Complete the table with an example from the chapter.

Property	Symbols	Example(s)
Commutative Property		
Associative Property		
Additive Identity		
Multiplicative Identity		
Multiplicative Property of Zero		

Complete the graphic organizer with a term from the chapter.

{0, 1, 2, 3}

{2, 5, 8, 11}

$\{(0, 2), (1, 5), (2, 8), (3, 11)\}$

triple a number and add two

Input (x)	0	1	2	3
Output (y)	2	5	8	11

$y = 3x + 2$


**CHAPTER
1**

Tools of Algebra

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Tools of Algebra	After You Read
<ul style="list-style-type: none"> • A variable represents an unknown number or quantity. 	
<ul style="list-style-type: none"> • If the order of numbers multiplied is changed, the product will also change. 	
<ul style="list-style-type: none"> • A coordinate plane has an x- and a y-axis. 	
<ul style="list-style-type: none"> • A scatter plot sometimes shows a trend in the data, but not always. 	
<ul style="list-style-type: none"> • You need an ordered pair with two numbers to plot a point on a coordinate plane. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 1.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 1 Study Guide and Review in the textbook.
- I took the Chapter 1 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Make a calendar that includes all of your daily classes. Besides writing down all assignments and due dates, include in your daily schedule time to study, work on projects, and review notes you took during class that day.


 CHAPTER
2

Operations with Integers

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Operations with Integers
	<ul style="list-style-type: none"> • A negative number is less than 0.
	<ul style="list-style-type: none"> • Every number has one absolute value.
	<ul style="list-style-type: none"> • Negative numbers can not be used in division problems.
	<ul style="list-style-type: none"> • When a number is added to its opposite, the sum is zero.
	<ul style="list-style-type: none"> • The difference of two negative numbers is a negative number.


FOLDABLES® Study Organizer

Construct the Foldable as directed at the beginning of this chapter.


Note Taking Tips

- **When you take notes, include definitions of new terms, explanations of new concepts, and examples of problems.**
- **At the end of each lesson, write a summary of the lesson, or write in your own words what the lesson was about.**

CHAPTER
2**Operations with Integers****Key Points**

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on integers and absolute value, one fact might be that a positive number is a number greater than zero. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
2-1 Integers and Absolute Value	
2-2 Adding Integers	
2-3 Subtracting Integers	
2-4 Multiplying Integers	
2-5 Dividing Integers	
2-6 Graphing in Four Quadrants	
2-7 Translations and Reflections on the Coordinate Plane	

2-1 Integers and Absolute Value

What You'll Learn

Skim the Examples for Lesson 2-1. Predict two things you think you will learn about integers and absolute value.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the term with the correct definition by drawing a line and connecting the two.

negative number a comparison of numbers or quantities

positive number the distance a number is from zero on a number line

integers a number less than zero

coordinate the counting numbers, their opposites, and zero

inequality a point on a number line or graph

absolute value a number greater than zero

Vocabulary Link List three examples of how *negative numbers* are used in everyday life.

Lesson 2-1 (continued)

Main Idea

Details

Compare and Order Integers

pp. 61–62

Fill in the blank with $<$, $>$, or $=$ to make each numerical sentence true.

1. -19 -17
2. 0 -3
3. $-1 + -3$ -4
4. -7 $-10 - 17$
5. $1 - 6$ $2 - 4$

Absolute Value

p. 63

Graph $|-5|$ on a number line. Write its value on the line below your number line. Then explain how you used a number line to find the absolute value of -5 .

Helping You Remember

Absolute is a word used in the English language.

Find a definition of *absolute* in a dictionary. Write the definition that most closely relates to mathematics. Explain how the definition you wrote down can help you remember the meaning of *absolute value* in mathematics.

2-2 Adding Integers

What You'll Learn

Skim Lesson 2-2. Predict two things you expect to learn based on the headings and the Key Concept box.

1. _____

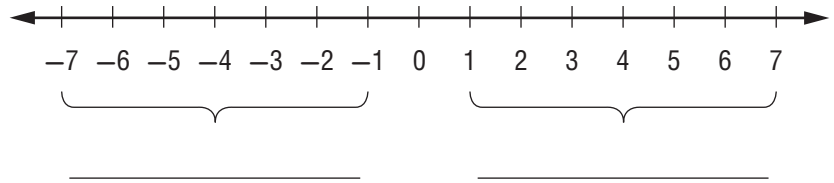
2. _____

Active Vocabulary

Review Vocabulary Label the diagram with the correct terms. (Lesson 2-1)

positive numbers ▶

negative numbers ▶



New Vocabulary Fill in each blank with the correct term or phrase.

opposites ▶ two _____ with the same _____ but different _____

additive inverse ▶ an _____ and its _____

Vocabulary Link *Opposites* can have non-mathematical meanings as well. Name the opposite of the terms listed.

up _____

on _____

day _____

hot _____

boy _____

south _____

Lesson 2-2 *(continued)*

Main Idea

Details

Add Integers

pp. 69–71

Model the addition sentence $3 + (-4)$ on a number line. Write the sum on the line under your model. Then explain in words how you used the number line to find the sum.

Add More Than Two Integers

pp. 71–72

Write each property used to simplify the expression.

$$5 + (-7) - 2$$

$$= 5 + 2 + (-7) \quad \underline{\hspace{2cm}}$$

$$= (5 + 2) + (-7) \quad \underline{\hspace{2cm}}$$

$$= 7 + (-7) \quad \text{Simplify.} \quad \underline{\hspace{2cm}}$$

$$= 0 \quad \underline{\hspace{2cm}}$$

Helping You Remember

Suppose that one of your friends was absent from math class the day you learned to add integers. Write an explanation to your friend about how to add integers with the *same signs*. Then explain how to add integers with *different signs*.

2-3 Subtracting Integers

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Define each term. Include two examples in your definitions. (*Lessons 2-1 and 2-2*)

additive inverse ▶

integer ▶

opposites ▶

Vocabulary Link *Integers* are used in everyday life. For each description, write the integer.

four degrees below zero _____

twelve inches long _____

twenty-five feet below sea level _____

fifty dollars overdrawn _____

Lesson 2-3 (continued)

Main Idea

Details

Subtract Integers

pp. 76–77

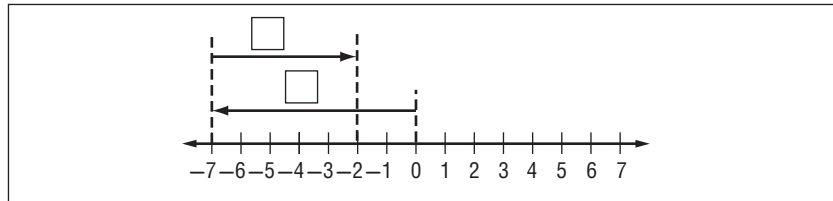
Describe how to subtract integers with the same and different signs and how to add integers with the same and different signs.

	Add Integers	Subtract Integers
same sign		
different signs		

Evaluate Expressions

p. 78

Label the following diagram of a subtraction sentence. Then write the subtraction sentence and solve.



Helping You Remember

Write an example for each difference described below. Then use addition to find each difference.

subtract a positive integer from a positive integer _____

subtract a positive integer from a negative integer _____

subtract a negative integer from a positive integer _____

subtract a negative integer from a negative integer _____

2-4 Multiplying Integers

What You'll Learn

Scan the text in Lesson 2-4. Write two facts you learned about multiplying integers.

1. _____

2. _____

Active Vocabulary

Vocabulary Link *Commute* and *associate* are words that are used in everyday English. Find the definition of *commutative* and *associative* using a dictionary. Explain how the English definitions can help you remember how *commutative* and *associative* are used in mathematics.

Lesson 2-4 (continued)

Main Idea

Details

Multiply Integers

pp. 83–85

Fill in the boxes to simplify each expression.

1. $-3(-5)$

2. -8×4

3. 12×10

4. $4(-2)$

5. $-9(-7)$

6. $-6 \cdot 6$

Algebraic Expressions

p. 85

Simplify the expression given the reason for each step.

$-3(12 + m + 18)$

$=$ _____ Replace m with 50.

$=$ _____ Commutative Property

$=$ _____ Simplify inside.

$=$ _____ Multiply.

Helping You Remember

In your own words, explain why the product of three negative integers is negative. Give an example.

2-5 Dividing Integers

What You'll Learn

Scan the text in Lesson 2-5. Write two facts you learned about dividing integers.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in the blank with the correct value. (Lessons 2-1 and 2-2)

- additive inverse* ▶ The *additive inverse* of -8 is _____.
- opposite* ▶ The *opposite* of 6 is _____.
- absolute value* ▶ The *absolute value* of $|-9|$ is _____.

New Vocabulary Write the definition next to the term.

- mean* ▶ _____

Vocabulary Link Write two examples of how the mathematical term *mean* is used in everyday life.

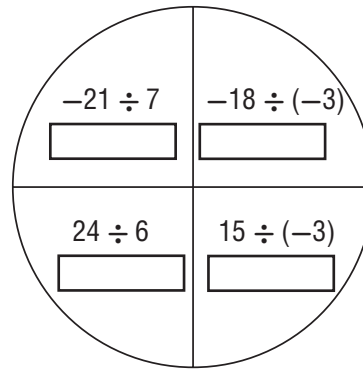
Lesson 2-5 (continued)

Main Idea

Details

Divide Integers
pp. 90–91

Write *positive* or *negative* to identify each quotient.



Mean (Average)
p. 92

Evan wanted to make sure his golf score average did not go above 42. He previously scored 44, 38, 33, 47, and 41. Fill in the blanks to solve the equation for x that will tell Evan the maximum score he could get and still have an average of 42.

$$\frac{44 + 38 + 33 + 47 + 41 + x}{\square} = 42 \quad \text{There are 6 data items.}$$

$$\frac{\square + x}{\square} = 42$$

Find the sum of the numerator.

$$6\left(\frac{\square + x}{\square}\right) = 42 \times \square$$

Eliminate the denominator by multiplying each side by 6.

$$\square + x = \square$$

Simplify.

$$x = \square$$

Subtract 203 from each side.

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Write one example of each quotient described

below. Then find the quotient.

dividing a positive integer by a negative integer _____

dividing a negative integer by a negative integer _____

dividing a negative integer by a positive integer _____

2-6 Graphing in Four Quadrants

What You'll Learn

Skim the lesson. Write two things you already know about graphing in four quadrants.

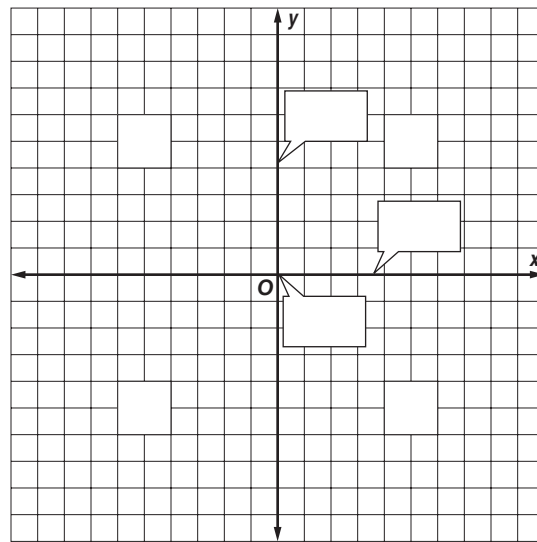
1. _____

2. _____

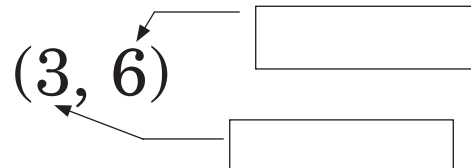
Active Vocabulary

Review Vocabulary Label the diagram with the correct terms. (Lesson 1-4)

- origin* ▶
- y-axis* ▶
- x-axis* ▶



- x-coordinate* ▶
- y-coordinate* ▶
- quadrants* ▶



New Vocabulary Label the diagram above with the correct quadrant: I, II, III, or IV.

Lesson 2-6 (continued)

Main Idea

Details

Graph Points

pp. 96–97

Match the ordered pairs with the correct quadrant by drawing a line to connect the coordinates with the quadrant. Circle coordinates that are not in any quadrant.

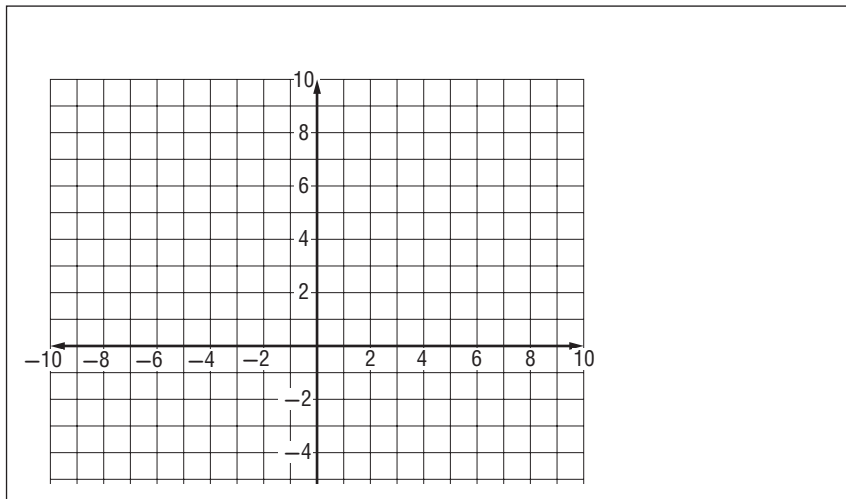
Quadrant I	(-3, -3)
	(-2, 0)
Quadrant II	(1, -5)
	(6, 2)
Quadrant III	(-1, 4)
	(0, 0)
Quadrant IV	

Graph Algebraic Relationships

p. 97

Model the following function by creating a function table with input and output values. Then graph the function.

The sum of one negative and one positive number is 3.



Helping You Remember

Draw a coordinate grid with points to represent your classroom and where your classmates sit. Explain how to name the location of your classmates.

2-7 Translations and Reflections on the Coordinate Plane

What You'll Learn

Skim Lesson 2-7. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the correct term next to each definition.

- _____ ▶ a transformation where each point of the original figure has a corresponding figure on the other side of a line of symmetry
- _____ ▶ a transformation where each point of an original figure moves the same distance in the same direction
- _____ ▶ a line of reflection
- _____ ▶ an operation that maps an original geometric figure onto a new figure
- _____ ▶ a transformed figure

Vocabulary Link *Transform* is a word that is used in everyday English. Find the definition of *transform* using a dictionary. Explain how the English definition can help you remember how *transformation* is used in mathematics.

Lesson 2-7

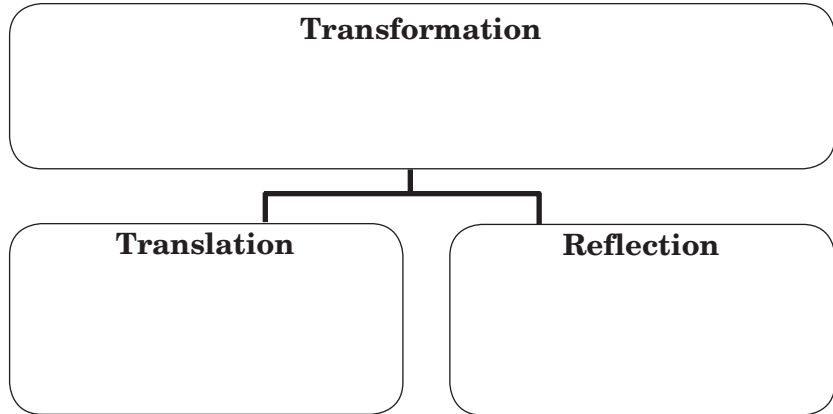
Lesson 2-7 (continued)

Main Idea

Details

Transformations
p. 101

Complete the organizer by defining the terms in your own words.



Translations and Reflections
pp. 102–103

Compare and contrast *translation* and *reflection*.

	Translation	Reflection
How they are alike		
How they are different		

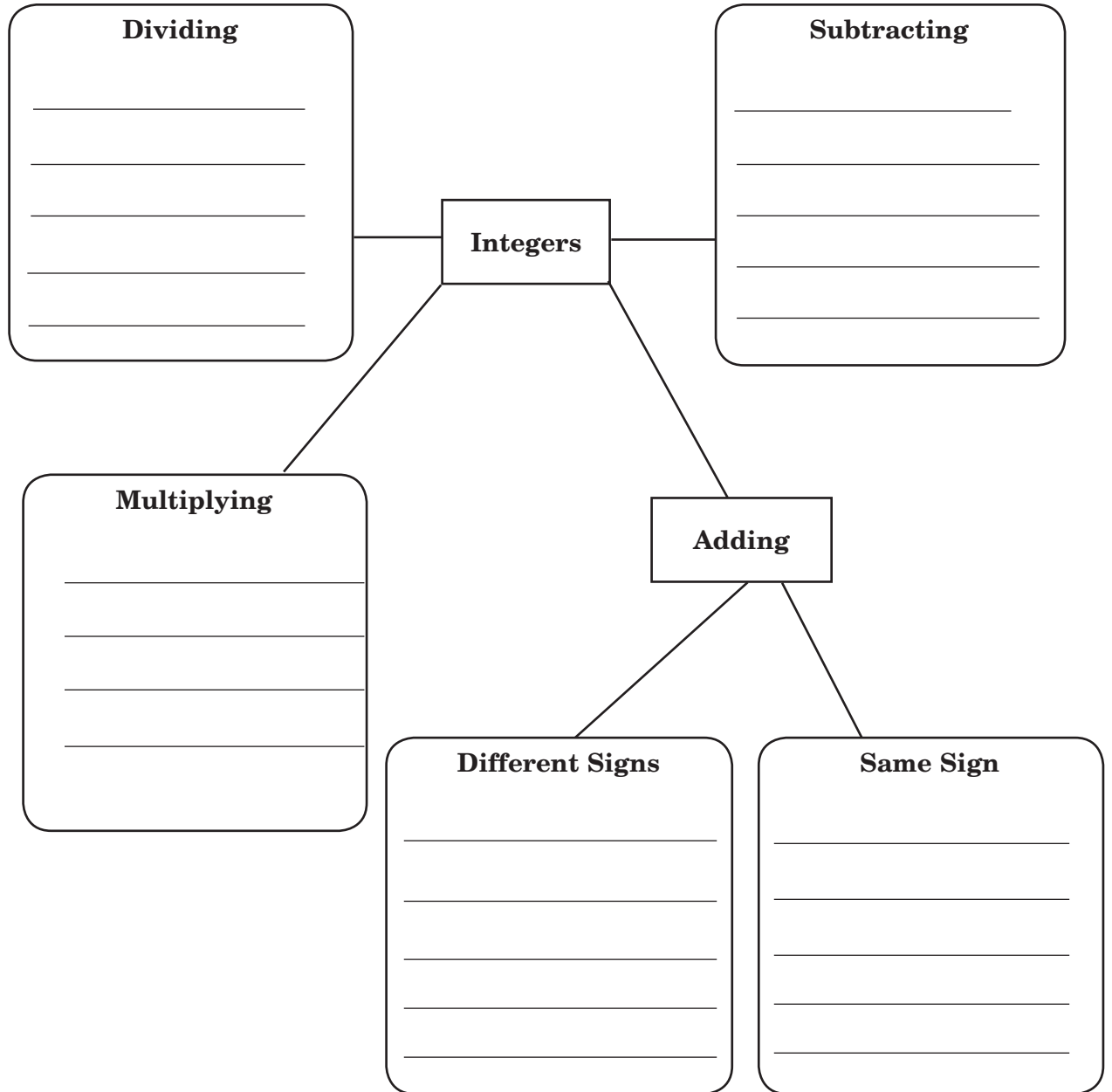
Helping You Remember Identify each type of transformation. Then describe in your own words how you know that you are correct.

CHAPTER
2

Operations with Integers

Tie It Together

Complete the graphic organizer with a phrase to help you remember the process.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
2

Operations with Integers

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Operations with Integers	After You Read
<ul style="list-style-type: none"> • A negative number is less than 0. 	
<ul style="list-style-type: none"> • Every number has one absolute value. 	
<ul style="list-style-type: none"> • Negative numbers can not be used in division problems. 	
<ul style="list-style-type: none"> • When a number is added to its opposite, the sum is zero. 	
<ul style="list-style-type: none"> • The difference of two negative numbers is a negative number. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 2.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 2 Study Guide and Review in the textbook.
- I took the Chapter 2 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Make up acronyms to remember lists or sequences. PEMDAS is one acronym for remembering the order of operations (parentheses, exponents, multiply and divide, add and subtract). (Please Excuse My Dear Aunt Sally)


 CHAPTER
3

Operations with Rational Numbers

Before You Read

Before you read the chapter, think about what you know about rational numbers. List three things you already know about operations with rational numbers in the first column. Then list three things you would like to learn about them in the second column.

K What I know...	W What I want to find out...


 FOLDABLES[®] Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- As you read each lesson, list ways the new knowledge has been or will be in your daily life.
- When you take notes, record real-life examples of how you can use fractions and decimals such as telling time and making change.

CHAPTER
3**Operations with Rational Numbers****Key Points**

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on dividing rational numbers, one fact might be that reciprocals are two numbers whose product is 1. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
3-1 Fractions and Decimals	
3-2 Rational Numbers	
3-3 Multiplying Rational Numbers	
3-4 Dividing Rational Numbers	
3-5 Adding and Subtracting Like Fractions	
3-6 Adding and Subtracting Unlike Fractions	

3-1 Fractions and Decimals

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Define *inequality* in your own words. (*Lesson 2-1*)

inequality ▶

New Vocabulary Match the term with its definition.

bar notation

decimals with a pattern in digits that have no end

terminating decimal

line placed over repeating digits

repeating decimal

decimals that divide evenly with no remainder

Vocabulary Link *Terminate* is a word that is used in everyday English. Find the definition of *terminate* using a dictionary. Explain how the English definition can help you remember how *terminate* is used in mathematics.

Lesson 3-1

Lesson 3-1 (continued)

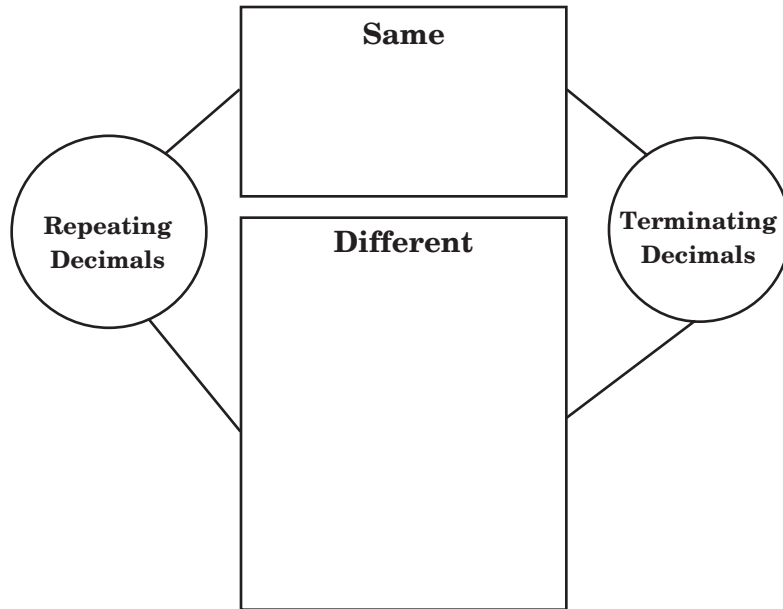
Main Idea

Write Fractions as Decimals

pp. 121–123

Details

Complete the diagram by comparing and contrasting repeating decimals and terminating decimals.



Compare Fractions and Decimals

pp. 123–124

Fill in the blank with $<$, $>$, or $=$ to make each numerical sentence true.

1. $\frac{5}{6}$ $\frac{2}{3}$

2. -0.36 $-\frac{1}{3}$

3. $\frac{23}{100}$ $\frac{1}{5}$

4. $\frac{7}{19}$ $\frac{4}{15}$

5. $-\frac{7}{8}$ $-\frac{8}{9}$

6. $-\frac{1}{5}$ -0.2

7. $\frac{3}{8}$ $\frac{6}{7}$

8. $\frac{4}{11}$ $\frac{5}{21}$

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember In your own words, explain the difference between 0.6 and $0.\overline{6}$. Which number is greater?

3-2 Rational Numbers

What You'll Learn

Scan the text in Lesson 3-2. Write two facts you learned about rational numbers as you scanned the text.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term. (Lessons 1-3 and 2-1)

integers ▶

properties ▶

New Vocabulary Fill in the blanks with the correct term or phrase.

rational numbers ▶ any _____ that can be written as _____

Vocabulary Link *Rational* is a word used in everyday English. Find the definition of *rational* in a dictionary. Then use the dictionary to find the antonym, or a word that means the opposite, of *rational*.

Lesson 3-2 (continued)

Main Idea

Rational Numbers
pp. 128–129

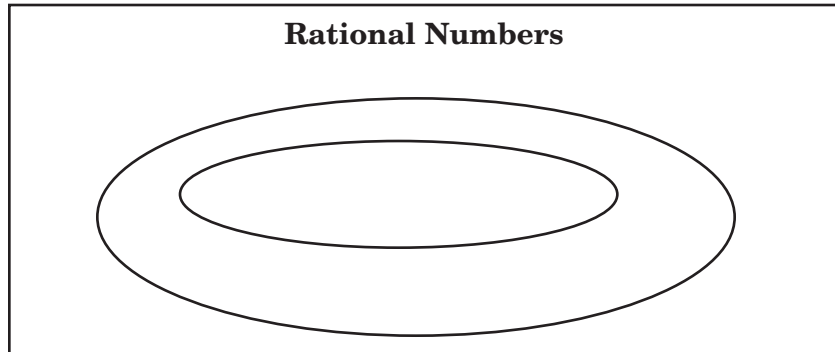
Identify and Classify Rational Numbers
p. 130

Details

Match each repeating decimal with its equivalent fraction.

$0.\overline{3}$	$\frac{14}{33}$
$0.\overline{125}$	$\frac{1}{3}$
$0.\overline{42}$	$\frac{1}{33}$
$0.\overline{03}$	$\frac{7}{9}$
$0.\overline{7}$	$\frac{125}{999}$

Complete the diagram by labeling each oval with the correct set of numbers. Use the terms *whole numbers* and *integers*. Then include three examples of whole numbers, integers, and rational numbers.



Helping You Remember

Describe the relationship among whole numbers, integers, and rational numbers, in your own words. Give an example of a number that is *not* rational and explain why it is not.

3-3 Multiplying Rational Numbers

What You'll Learn

Skim Lesson 3-3. Predict two things that you learn based on the headings and figures in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lessons 2-2 and 3-2*)

_____ ▶ a number less than zero

_____ ▶ the counting numbers, their opposites, and zero

_____ ▶ any number that can be written as a fraction

_____ ▶ a number greater than zero

Vocabulary Link *Multiplication* is the same as repeated addition. In Lesson 2-2 you used a number line to add integers. Explain how you can use 'repeated addition' to demonstrate $4 \cdot \frac{1}{2}$ on a number line.

Lesson 3-3 (continued)

Main Idea

Details

Multiply Fractions
pp. 134–135

Use the model to find $\frac{3}{5} \times \frac{4}{7}$. Explain your steps on the lines below.

Evaluate Expressions with Fractions
pp. 135–136

Fill in the blanks to find each product in simplest form.

Use $x = \frac{2}{3}$, $y = -\frac{7}{11}$, and $z = \frac{3}{5}$.

1. xy

$$\square \times \square = \square$$

2. $-2y$

$$-2 \times \square = \square$$

3. $\frac{5}{9}z$

$$\frac{5}{9} \times \square = \square$$

4. xyz

$$\square \times \square \times \square = \square$$

Helping You Remember

Explain in your own words how to find the product of two fractions with a model. What portion of the model is the product?

3-4 Dividing Rational Numbers

What You'll Learn

Scan Lesson 3-4. List two headings you would use to make an outline for this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in the blank with the correct term or phrase. (*Lesson 2-2*).

additive inverse ► an _____ and its opposite

New Vocabulary Write the definition next to each term.

multiplicative inverses ► _____

reciprocals ► _____

Vocabulary Link *Reciprocal* is a word that is used in everyday English. Find the definition of *reciprocal* using a dictionary. Explain how the English definition can help you remember how *reciprocal* is used in mathematics.

Lesson 3-4 (continued)

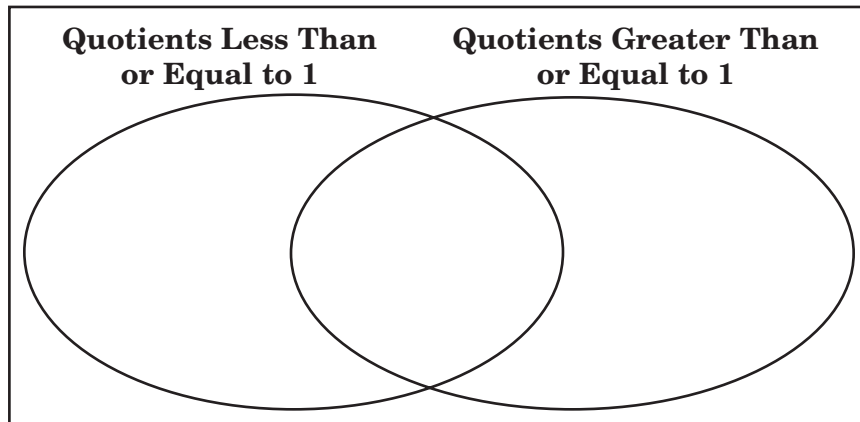
Main Idea

Details

Divide Fractions

pp. 141–143

Place three division expressions in each section of the Venn diagram.



Divide Algebraic Expressions

p. 143

Simplify each expression.

1. $\frac{x^2}{4} \div \frac{xy}{2}$

2. $\frac{b}{6ab} \div \frac{3b}{a}$

3. $\frac{7}{gh} \div \frac{5}{4fh}$

4. $\frac{14x}{xy} \div \frac{1}{10xy}$

5. $\frac{q}{12} \div \frac{n^2}{2}$

6. $\frac{b}{2d} \div \frac{2}{9c}$

Helping You Remember

In your own words, explain how you know whether the quotient of two fractions will be less than 1, equal to 1, or greater than 1.

3-5 Adding and Subtracting Like Fractions

What You'll Learn

Skim the examples for Lesson 3-5. Predict two things you think you will learn about adding and subtracting like fractions.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lesson 2-1*).

- _____ ▶ the distance a number is from zero on a number line
- _____ ▶ a number less than zero
- _____ ▶ the counting numbers, their opposites, and zero
- _____ ▶ a number greater than zero

New Vocabulary Write the definition next to the term.

like fractions ▶ _____

Vocabulary Link *Like* is a word that is used in everyday English. Find the definition of *like* using a dictionary. Explain how the English definition can help you remember how *like* is used in mathematics.

Lesson 3-5 (continued)

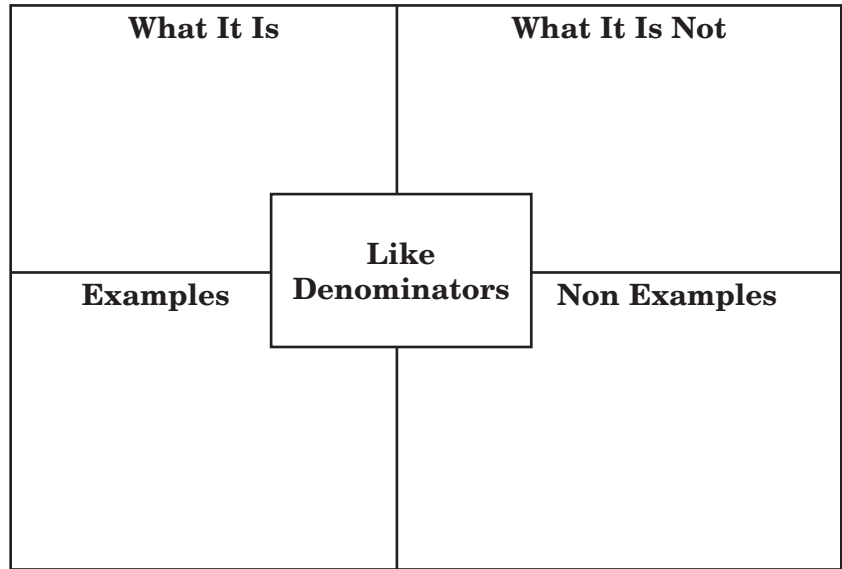
Main Idea

Details

Add Like Fractions

pp. 147–148

Complete the diagram.



Subtract Like Fractions

pp. 148–150

Fill in the blanks with each difference.

1. $3\frac{3}{5} - 2\frac{2}{5} = \square$

2. $8\frac{3}{7} - 5\frac{5}{7} = \square$

3. $\frac{1}{9} - 1\frac{8}{9} = \square$

4. $\frac{3}{10} - \frac{9}{10} = \square$

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Sketch a model to show each sum or difference.

a. $\frac{3}{10} + \frac{6}{10}$

b. $\frac{6}{7} - \frac{3}{7}$

3-6 Adding and Subtracting Unlike Fractions

What You'll Learn

Skim the lesson. Write two things you already know about adding and subtracting unlike fractions.

1. _____

2. _____

Active Vocabulary

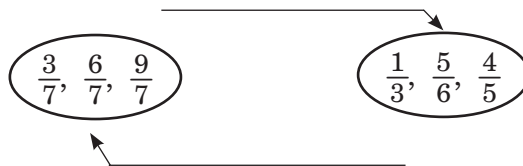
Review Vocabulary Write the definition next to the term. (Lessons 2-2 and 3-5)

opposites ▶

New Vocabulary Label the diagram with the correct terms.

like fractions ▶

unlike fractions ▶



Vocabulary Link *Unlike* can have non-mathematical meanings as well. Give an example of two things that are *unlike* each other. Then give an example of two things that are like each other.

unlike: _____

like: _____

Lesson 3-6

Lesson 3-6 (continued)

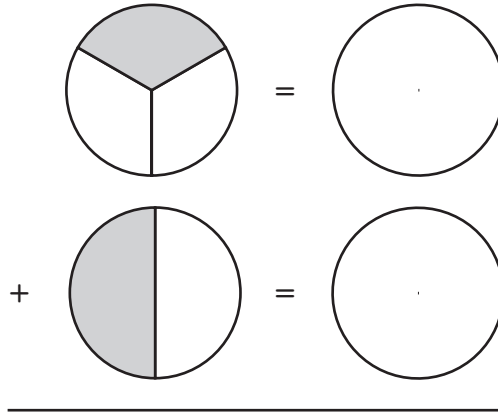
Main Idea

Details

Add Unlike Fractions

pp. 153–154

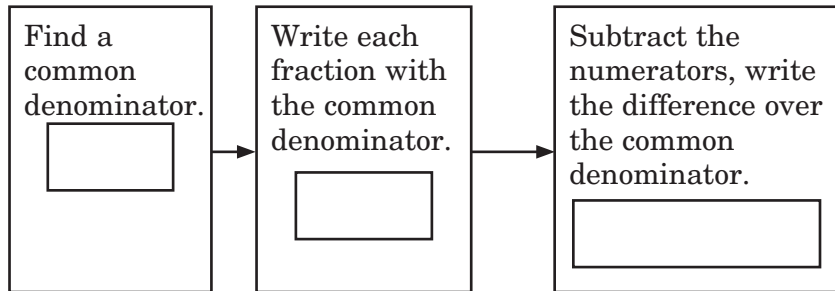
Shade each circle to show equivalent fractions for $\frac{1}{3}$ and $\frac{1}{2}$ using the LCD. Then write the addition sentence the model represents.



Subtract Unlike Fractions

pp. 154–155

Write each step used to find $\frac{5}{6} - \frac{1}{4}$.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Describe two methods that you can use to add

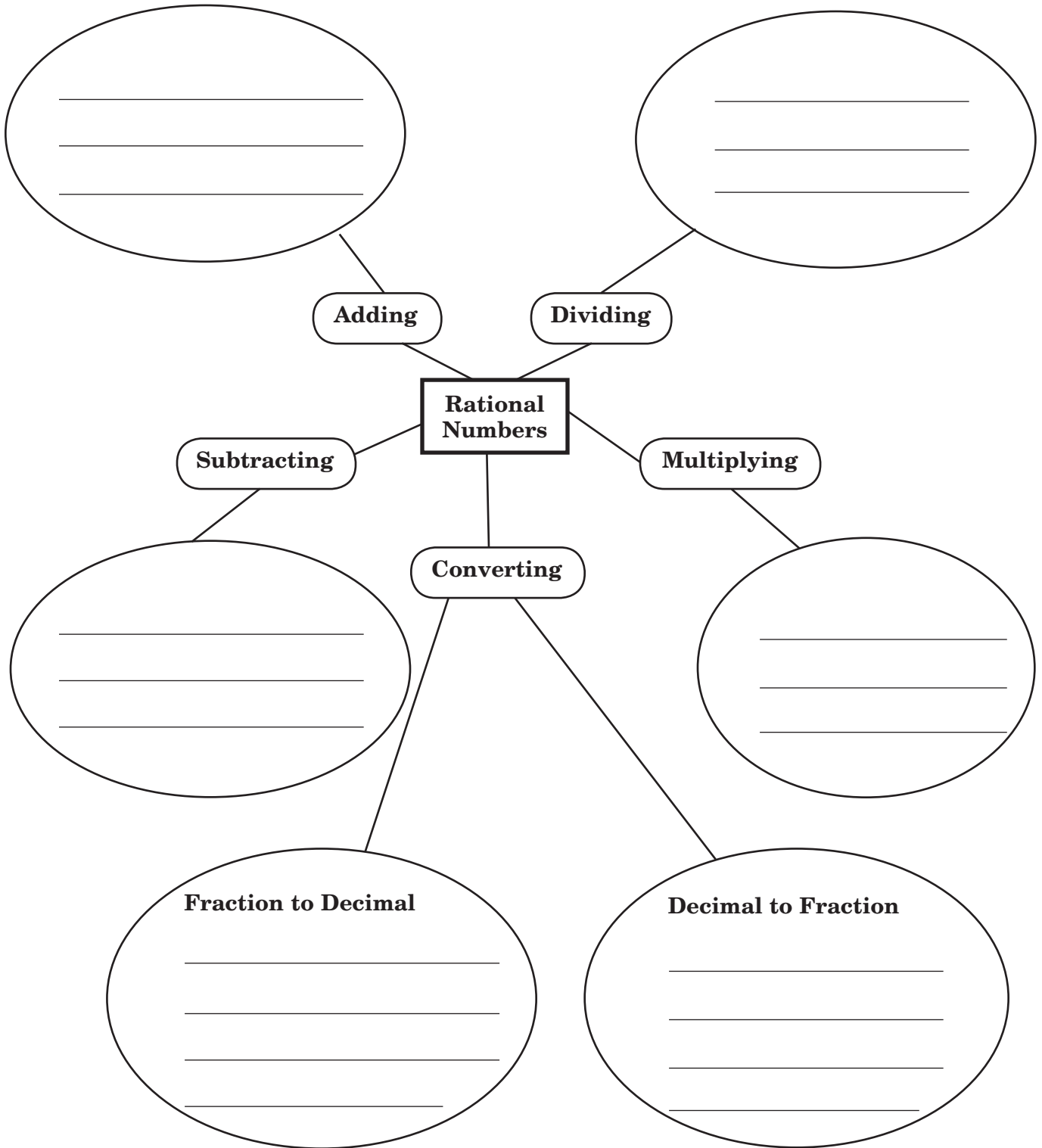
$1\frac{1}{3}$ and $3\frac{3}{5}$. Then find the sum.

CHAPTER
3

Operations with Rational Numbers

Tie It Together

Complete each graphic organizer with a phrase to help you remember the process.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
3

Operations with Rational Numbers

Before the Test

Review the ideas you listed in the table at the beginning of the chapter. Cross out any incorrect information in the first column. Then complete the table by filling in the third column.

K What I know...	W What I want to find out...	L What I learned...

Math Online Visit *glencoe.com* to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 3.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 3 Study Guide and Review in the textbook.
- I took the Chapter 3 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Get a good nights rest before a test. Students that take the time to sleep usually do better than students who stay up late cramming.


 CHAPTER
4

Expressions and Equations

Before You Read

Before you read the chapter, think about what you know about expressions and equations. List three things you already know about them in the first column. Then list three things you would like to learn about them in the second column.

K What I know...	W What I want to find out...


 FOLDABLES[®] Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- **When you take notes, listen or read for main ideas.**
Then record those ideas for future reference.
- **Write down questions that you have about what you are reading in the lesson.**
Then record the answer to each question as you study the lesson.

CHAPTER
4**Expressions and Equations****Key Points**

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on simplifying algebraic expressions, one fact might be that a term without a variable is called a constant. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
4-1 The Distributive Property	
4-2 Simplifying Algebraic Expressions	
4-3 Solving Equations by Adding or Subtracting	
4-4 Solving Equations by Multiplying or Dividing	
4-5 Solving Two-Step Equations	
4-6 Writing Equations	

4-1 The Distributive Property

What You'll Learn

Skim Lesson 4-1. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

equivalent expressions ▶

Distributive Property ▶

Vocabulary Link *Distribute* is a word that is used in everyday English. Find the definition of *distribute* using a dictionary. Explain how the English definition can help you remember how *distributive* is used in mathematics.

Lesson 4-1

Lesson 4-1 (continued)

Main Idea

Details

Numerical Expressions

pp. 171–172

Complete each expression using the Distributive Property.

1. $5(3 + 4) = 5 \cdot 3 + 5 \cdot \square$
2. $6(4 - 1) = 6 \cdot \square - 6 \cdot 1$
3. $2(8 - 7) = 2 \cdot \square - 2 \cdot \square$
4. $3(4 + 9) = \square \cdot 4 + \square \cdot 9$
5. $(2 + 5)8 = 2 \cdot 8 + 5 \cdot \square$
6. $(6 - 3)7 = \square \cdot 7 - \square \cdot 7$

Algebraic Expressions

pp. 172–173

Model the expression $3(x + 2)$. Then model 3 groups of x and 3 groups of 2. Write two equivalent expressions below your model.

Helping You Remember

A classmate states that $3(x + 1) = 3x + 1$. How would you model to your classmate that $3(x + 1) = 3x + 3$ *not* $3x + 1$ Include drawings with your explanation.

4-2 Simplifying Algebraic Expressions

What You'll Learn

Scan Lesson 4-2. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the term with its definition by drawing a line to connect the two.

coefficient a term without a variable

constant each part of an algebraic expression

like terms terms that contain the same variables

simplest form the numerical part of a term that contains a variable

simplifying the expression an algebraic expression that has no like terms and no parentheses

term using the Distributive Property to combine like terms

Lesson 4-2 (continued)

Main Idea

Parts of Algebraic Expressions

pp. 178–179

Details

Identify the parts of the algebraic expression below.

$$4x + 9y + 7y - 2x + 5$$

How many terms are there in the expression? _____

How many sets of like terms are there? _____

Circle one pair of like terms. _____

List another pair of like terms. _____

What is the constant term? _____

Simplify Algebraic Expressions

pp. 179–180

Simplify each expression by combing like terms.

1. $4x + 3x = \square x$

2. $10 + 4y + 6y = 10 + \square y$

3. $15a + 6b - 3b + 2a = \square a + \square b$

4. $3t + 1 + 8t - 6 = \square t - \square$

5. $2m - 4k + 3 - 8m + 2 = \square m - \square k + \square$

Helping You Remember

Constant is a word used in everyday English as well as in mathematics. Write the definition of *constant*. Explain how the English definition can help you remember how *constant* is used in mathematics.

4-3 Solving Equations by Adding or Subtracting

What You'll Learn

Skim the Examples for Lesson 4-3. Write two things you already know about solving equations by adding or subtracting.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the correct term next to each definition.

- _____ ► undoes each other
- _____ ► a mathematical sentence that contains an equals sign (=)
- _____ ► a value for the variable that makes an equation true

Vocabulary Link *Inverse operations* can have non-mathematical meanings as well. For each activity, name the inverse operation that would undo the activity.

- turning on a light switch _____
- driving 5 miles north _____
- tying a shoelace _____
- opening a window _____

Lesson 4-3 (continued)

Main Idea

Details

Solve Equations by Adding

pp. 184–185

Fill in the blanks to solve each equation.

1. $x - 2 = 7$

$$\frac{\boxed{}}{x} = \frac{\boxed{}}{}$$

2. $y - 4 = -3$

$$\frac{\boxed{}}{y} = \frac{\boxed{}}{}$$

3. $b - 1\frac{2}{3} = \frac{1}{6}$

$$\frac{\boxed{}}{b} = \frac{\boxed{}}{}$$

4. $c - 6.2 = -9.7$

$$\frac{\boxed{}}{c} = \frac{\boxed{}}{}$$

Solve Equations by Subtracting

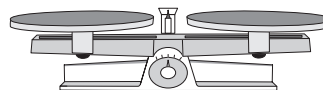
pp. 185–186

Model the following situation by drawing algebra tiles. Then solve.

Grace and Carrie have 14 necklaces combined. Carrie has 9 necklaces. How many does Grace have?

Helping You Remember

How is adding the same number of blocks to each side of a balance scale like the Addition Property of Equality?



4-4 Solving Equations by Multiplying or Dividing

What You'll Learn

Skim the lesson. Write two things you already know about solving equations by multiplying and dividing.

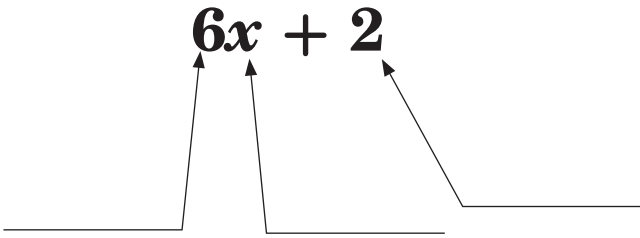
1. _____

2. _____

Active Vocabulary

Review Vocabulary Label the diagram with the correct terms. (Lesson 4-2)

- coefficient* ▶
- constant* ▶
- variable* ▶



Vocabulary Link *Variable* and *constant* are two words used in everyday English. Find the definitions of *variable* and *constant* using a dictionary. List an example of something in your life that is variable. List an example of something in your life that is constant.

Lesson 4-4 (continued)

Main Idea

Details

Solve Equations by Dividing

pp. 191–192

Fill in the blanks to solve each equation.

1. $3m = 18$

$$\frac{3m}{\square} = \frac{18}{\square}$$

$$m = \square$$

2. $-5n = 35$

$$\frac{-5n}{\square} = \frac{35}{\square}$$

$$n = \square$$

3. $0.6s = -42$

$$\frac{0.6s}{\square} = \frac{-42}{\square}$$

$$s = \square$$

4. $-8t = -48$

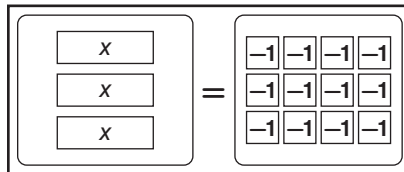
$$\frac{-8t}{\square} = \frac{-48}{\square}$$

$$t = \square$$

Solve Equations by Multiplying

p. 193

Write an equation to represent the model below. Then solve.



Helping You Remember

Write two examples of equations that can be solved using each of the four properties of equations below.

Addition Property of Equality: _____

Subtraction Property of Equality: _____

Multiplication Property of Equality: _____

Division Property of Equality: _____

4-5 Solving Two-Step Equations

What You'll Learn

Scan the text in Lesson 4-5. Write two facts you learned about solving two-step equations.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Identify the following inverse operations. Draw a line from each operation to its inverse. (*Lessons 4-3 and 4-4*).

addition

addition

subtraction

subtraction

multiplication

multiplication

division

division

New Vocabulary Define the following terms from this lesson.

two-step equation ►

Vocabulary Link *Two-step equations* can be illustrated by real-world examples. Consider the two-step process of putting on socks and putting on shoes. Explain how to “undo” the process. Write an example of another real-world process that takes two steps to “undo”.

Lesson 4-5 (continued)

Main Idea

Details

Solve Two-Step Equations

pp. 199–201

Justify each step used in solving the equation.

$$6x - 14 = 16$$

$$6x - 14 + 14 = 16 + 14 \quad \underline{\hspace{2cm}}$$

$$6x = 30 \quad \underline{\hspace{2cm}}$$

$$\frac{6x}{6} = \frac{30}{6} \quad \underline{\hspace{2cm}}$$

$$x = 5 \quad \underline{\hspace{2cm}}$$

Solve the equation given the justification for each step.

$$\frac{y}{9} + 4 = -2$$

$$\boxed{\hspace{1cm}} = \boxed{\hspace{1cm}} \quad \text{Subtraction Property of Equality}$$

$$\boxed{\hspace{1cm}} = \boxed{\hspace{1cm}} \quad \text{Simplify.}$$

$$\boxed{\hspace{1cm}} = \boxed{\hspace{1cm}} \quad \text{Multiplication Property of Equality}$$

$$y = \boxed{\hspace{1cm}} \quad \text{Simplify.}$$

Helping You Remember

List the steps you would use in the order you would use them to “undo” each equation.

$$2x + 17 = 35 \quad \underline{\hspace{2cm}}$$

$$\frac{x}{6} - 1 = 18 \quad \underline{\hspace{2cm}}$$

$$\frac{x + 3}{4} = 5 \quad \underline{\hspace{2cm}}$$

4-6 Writing Equations

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Complete the table below listing words that indicate each operation. Use the words below the table. (*Lesson 1-1*)

Addition	Subtraction	Multiplication	Division

decreased by
 increased by
 less than
 product
 sum
 total

difference
 less
 more than
 quotient
 times
 twice

Lesson 4-6

Lesson 4-6 (continued)

Main Idea

Details

Write Two-Step Equations

pp. 205–206

Answer each question using the information below.

Miguel and Carla spent \$64 at the bookstore combined. Carla spent \$15 less than Miguel.

1. Who spent less money at the bookstore? _____
2. How much less? _____
3. Write an expression to represent the amount of money Miguel spent, in terms of m . _____
4. Write an expression to represent the amount of money Carla spent, in terms of m . _____
5. Write an equation to represent the amount Miguel and Carla spent combined, in terms of m . _____
6. How much did each person spend at the bookstore?

Two-Step Verbal Problems

p. 206

Write a verbal sentence to represent the equation below. Then solve.

$$\frac{x}{12} + 4 = 16$$

Helping You Remember

Write a word problem that can be solved using a two-step equation. Solve the equation.

CHAPTER
4

Expressions and Equations

Tie It Together

Complete the graphic organizer to review writing and solving equations.

Georgia and her brother collected cans for a recycling program. Georgia collected three more than twice as many cans as her brother. They collected a total of 213 cans. How many cans did each person collect?

Steps	Example
Write the equation by translating from words to symbols, to the equation.	
Combine ___ terms.	
Work _____ through the order of operations to “undo” operations. _____ first.	
_____ next.	
Check your answer by _____.	
Answer the question that was asked.	

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
4

Expressions and Equations

Before the Test

Review the ideas you listed in the table at the beginning of the chapter. Cross out any incorrect information in the first column. Then complete the table by filling in the third column.

K What I know...	W What I want to find out...	L What I learned...

Math Online Visit *glencoe.com* to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 4.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 4 Study Guide and Review in the textbook.
- I took the Chapter 4 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- When you are preparing to read new material, scan the text first, briefly looking over headings, highlighted text, pictures, and call out boxes. Think of questions you might answer as you read.

CHAPTER
5

Multi-Step Equations and Inequalities

Before You Read

Before you read the chapter, think about what you know about solving multi-step equations and inequalities. List three things you already know about them in the first column. Then list three things you would like to learn about them in the second column.

K What I know...	W What I want to find out...

FOLDABLES® Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- **A visual (graph, diagram, picture, chart) can present information in a concise, easy-to-study format.**
Clearly label your visuals and write captions when needed.
- **When you take notes, you may wish to use a highlighting marker to emphasize important concepts.**

CHAPTER
5**Multi-Step Equations and Inequalities****Key Points**

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on inequalities, one fact might be that an inequality is a mathematical sentence that compares quantities that are not equal. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
5-1 Perimeter and Area	
5-2 Solving Equations with Variables on Each Side	
5-3 Inequalities	
5-4 Solving Inequalities	
5-5 Solving Multi-Step Equations and Inequalities	

5-1 Perimeter and Area

What You'll Learn

Scan the text in Lesson 5-1. Write two facts you learned about perimeter and area as you scanned the text.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lesson 1-2*)

variable ▶ a _____ or _____ that represents an _____ value

algebraic expression ▶ an _____ with a least one _____ and one _____

New Vocabulary Match the term with its definition by drawing a line to connect the two.

area distance around a geometric figure

perimeter equation that shows a relationship among certain quantities

formula measure of the surface enclosed by a figure

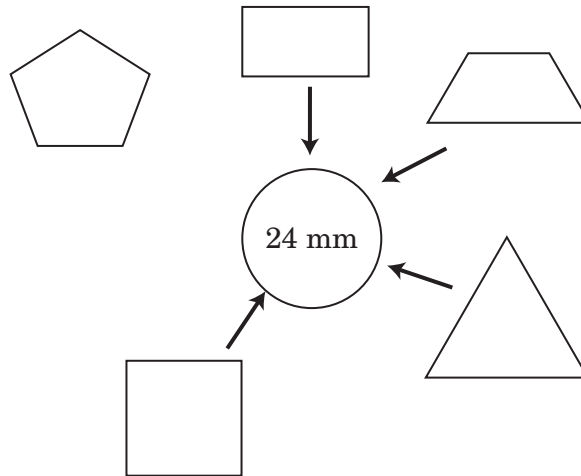
Lesson 5-1 *(continued)*

Main Idea

Details

Perimeter
pp. 221–222

Complete the diagram by labeling each figure so that its perimeter is equal to 24 millimeters.



Area
pp. 222–223

Model a triangle with height of 12 inches and base length of 10 inches. Then find its area.

Helping You Remember

Compare and contrast the units used for perimeter and area. Explain why area uses square units and perimeter does not.

5-2 Solving Equations with Variables on Each Side

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lessons 4-2 and 4-3*)

like terms ▶ terms that contain the same _____

simplest form ▶ an algebraic expression that has no _____ terms and no _____

simplifying the expression ▶ You can use the _____ _____ to combine like terms.

Additive or Subtraction Properties of Equality ▶ allows you to _____ or _____ the same quantity from each side of an _____ to keep the two sides equal

Vocabulary Link *Equality* is a word that is used in everyday English. Find the definition of *equality* by using a dictionary. List an example of something in your life that has *equality*.

Lesson 5-2

Lesson 5-2 (continued)

Main Idea

Equations with Variables on Each Side
pp. 229–230

Details

Model the equation $3x - 2 = 5x - 4$ using algebra tiles. Then solve.

Fill in the blanks to solve each equation.

1. $2x + 5 = 3x$

= x

2. $7b + 5 = -3b - 10$

$10b =$

$b =$

3. $21 - 16t = 4t - 14$

$t = -35$

$t =$

4. $0.8y + 1.6 = 0.6y - 1$

$0.2y =$

$y =$

5. $9a - 3 = 15$

$9a =$

$a =$

6. $18x + 6 = 9 - 3x$

$x = 3$

$x =$

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Write an equation with a variable on both sides, along with all the steps needed to solve the equation. Trade with a partner. Then each of you should explain verbally why each step in solving the equation was carried out.

5-3 Inequalities

What You'll Learn

Skim the lesson. Write two things you already know about inequalities.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to each definition.
(Lesson 2-1)

_____ ▶ a number less than zero

_____ ▶ the counting numbers, their opposites, and zero

_____ ▶ a number greater than zero

New Vocabulary Write the definition next to the term.

inequality ▶ _____

Vocabulary Link *Inequality* is a word that is used in everyday English. Find the definition of *inequality* using a dictionary. Explain how the English definition can help you remember how *inequality* is used in mathematics.

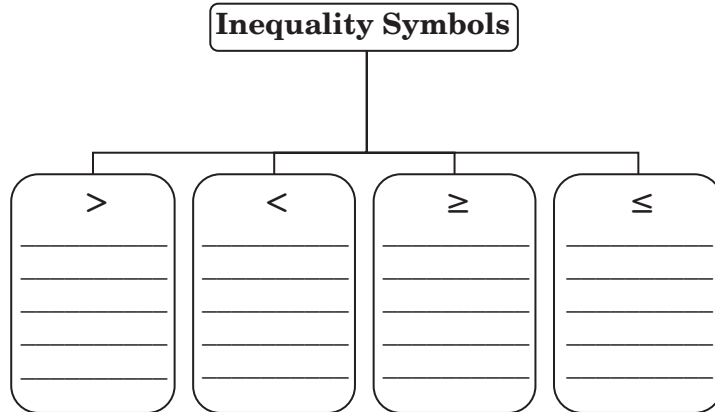
Lesson 5-3 (continued)

Main Idea

Details

Write Inequalities
pp. 234–235

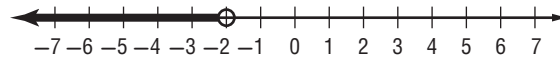
Fill in the organizer with words that describe the symbols.



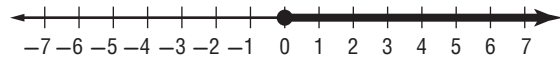
Graph Inequalities
p. 236

Write an inequality for each model.

1. _____



2. _____



Helping You Remember Write a paragraph explaining how to graph an inequality to a classmate that was absent from class the day it was taught. Include an explanation of the symbols used, as well as the use of open and closed dots or points.

5-4 Solving Inequalities

What You'll Learn

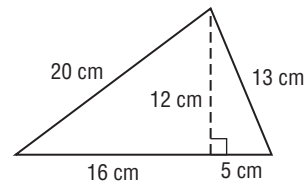
Scan Lesson 5-4. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Use the diagram to fill in each blank with the correct term. (*Lesson 5-1*)



formula ►

The _____ for the triangle is 126 cm^2 and the _____

perimeter ►

for the triangle is 54 cm.

area ►

$A = \frac{1}{2}bh$ is the _____ for the area of a triangle.

Vocabulary Link *Addition and Subtraction Properties* allow you to add or subtract the same quantities to each side of an equation or inequality with the sentence remaining true.

List an example of something in everyday life that you have to do “the same on both sides” to keep it equal or the same.

Lesson 5-4 (continued)

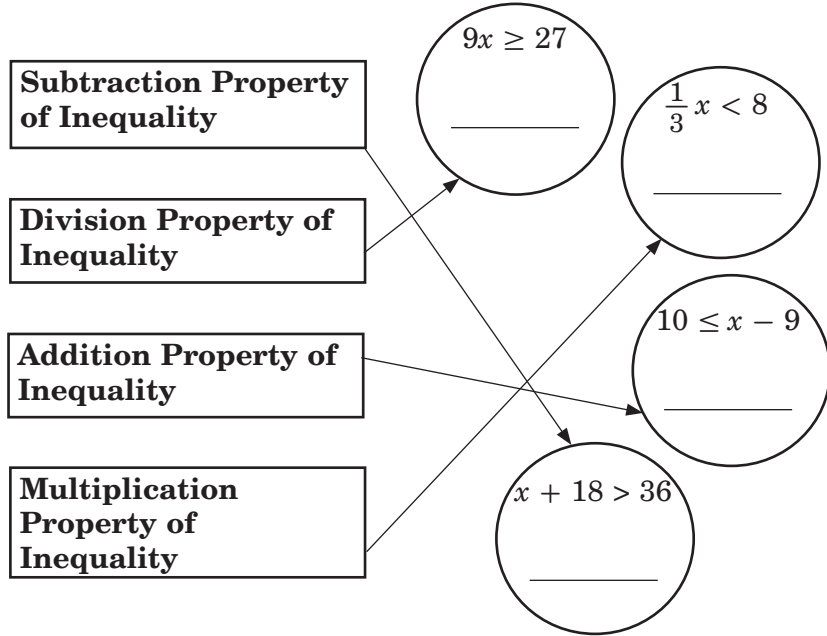
Main Idea

Details

Solve Inequalities by Adding or Subtracting
pp. 241–242

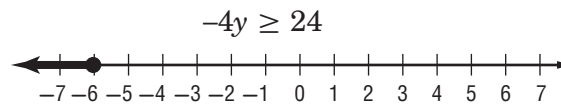
Draw an arrow and match the correct property needed to solve the inequality. Then solve each inequality.

Solve Inequalities by Multiplying or Dividing by a Positive Number
pp. 242–243



Multiply or Divide an Inequality by a Negative Number
pp. 243–244

Model the solution of the inequality on the number line.



Helping You Remember

In the boxes below, write examples of inequalities in which the sign does and does not reverse. Write at least three examples in each box.

5-5 Solving Multi-Step Equations and Inequalities

What You'll Learn

Skim the Examples for Lesson 5-5. Predict two things you think you will learn about solving multi-step equations and inequalities.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lesson 4-1*)

Distributive Property ▶ To _____ a sum or difference by a number, _____ each term inside the _____ by the number outside of the _____.

New Vocabulary Write the definition next to each term.

null or empty set ▶ _____

identity ▶ _____

Vocabulary Link *Null* is a word that is used in everyday English. Find the definition of *null* using a dictionary. Explain how the English definition can help you remember how *null* is used in mathematics.

Lesson 5-5 *(continued)*

Main Idea

Details

Solve Equations and Inequalities with Grouping Symbols

pp. 248–249

Complete the organizer by following the steps given to solve the inequality.

Steps in Solving Multi-Step Equations and Inequalities

$$2(x - 3) \quad 4(x + 3) - 6x$$

Step 1: Use the Distributive Property to remove parentheses

Step 1:

Step 2: Combine like terms on same side

Step 2:

Step 3: Use the Addition or Subtraction Properties

Step 3:

Step 4: Use the Multiplication or Division Properties

Step 4:

No Solution or All Numbers as Solutions

p. 250

Write an equation that has a solution that is an identity. Then write an equation with a null or empty set.

identity:

null or empty set:

Helping You Remember

An identity is an equation that is true for every value of the variable. A null or empty set occurs when an equation has no solution. Write and solve an example of each type of equation.

CHAPTER
5

Multi-Step Equations and Inequalities

Tie It Together

Complete the graphic organizer to compare and contrast equations and inequalities.

Multi-Step Equations

Inequalities

Symbol(s)

_____	_____
_____	_____
_____	_____
_____	_____

Steps to solve

_____	_____
_____	_____
_____	_____
_____	_____

Graph

_____	_____
_____	_____
_____	_____
_____	_____


 CHAPTER
5

Multi-Step Equations and Inequalities

Before the Test

Review the ideas you listed in the table at the beginning of the chapter. Cross out any incorrect information in the first column. Then complete the table by filling in the third column.

K What I know...	W What I want to find out...	L What I learned...

Math Online Visit *glencoe.com* to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 5.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 5 Study Guide and Review in the textbook.
- I took the Chapter 5 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- On test day, look over the entire test to get an idea of its length and scope so that you can pace yourself. Answer what you know first, then go back and complete the problems you skipped. When finished, check for errors. Don't change an answer unless you are certain you are correct.


 CHAPTER
6

Ratio, Proportion, and Similar Figures

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Ratio, Proportion, and Similar Figures
	<ul style="list-style-type: none"> • A ratio is a comparison of quantities by addition.
	<ul style="list-style-type: none"> • Unit rates are useful when comparing prices.
	<ul style="list-style-type: none"> • Ratios are used to change a measurement from one unit to another.
	<ul style="list-style-type: none"> • When two figures are proportional, they will have the same side and angle measures.
	<ul style="list-style-type: none"> • A scale drawing is sometimes proportional to the actual object.


 FOLDABLES® Study Organizer

Construct the Foldable as directed at the beginning of this chapter.


 Note Taking Tips

- **To help you organize data, create study cards when taking notes, recording and defining vocabulary words, and explaining concepts.**
- **When taking notes, use a table to make comparisons about the new material.** Determine what will be compared, decide what standards will be used, and then use what is known to find similarities and differences.

CHAPTER
6

Ratio, Proportion, and Similar Figures

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on solving proportions, one fact might be that the cross products of any proportion are equal. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
6-1 Ratios	
6-2 Unit Rates	
6-3 Converting Rates and Measurements	
6-4 Proportional and Nonproportional Relationships	
6-5 Solving Proportions	
6-6 Scale Drawings and Models	
6-7 Similar Figures	
6-8 Dilations	
6-9 Indirect Measurement	

6-1 Ratios

What You'll Learn

Scan Lesson 6-1. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Define *simplify* in your own words. (Lesson 1-3)

simplify ► _____

New Vocabulary Fill in each blank with the correct term or phrase.

ratio ► a _____ of two _____ by division that is usually written in _____ form

Vocabulary Link *Ratio* is a word that is used in everyday English. Find the definition of *ratio* using a dictionary. List two examples of real-life ratios.

Lesson 6-1 (continued)

Main Idea

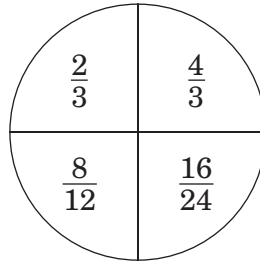
Write Ratios as Fractions in Simplest Form

pp. 265–266

Details

Cross out the ratio that is not equivalent to the following ratio.

16 girls out of 24 students



Simplify Ratios Involving Measurements

p. 266

Write each ratio in simplest form.

1. 15 cans out of 9 cases = 2. 4 rings to 7 bracelets =

3. 2 c to 32 oz = 4. 16 in. to 4 ft =

5. 11 dramas out of 17 DVDs =

6. 6 hours 14 days =

Helping You Remember

Ratios can represent part to part, part to whole, or whole to part relationships. Write a problem that can be expressed with these three ratios. Include the ratios in your description.

6-2 Unit Rates

What You'll Learn

Skim the Examples for Lesson 6-2. Predict two things you think you will learn about unit rates.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lesson 5-1*)

area ► The _____ of the _____ enclosed by a figure.

New Vocabulary Write the definition next to each term.

rate ► _____

unit rate ► _____

Vocabulary Link *Rate* is a word that is used in everyday English. Find the definition of *rate* using a dictionary. Write two examples of rates used in everyday life.

Lesson 6-2 (continued)

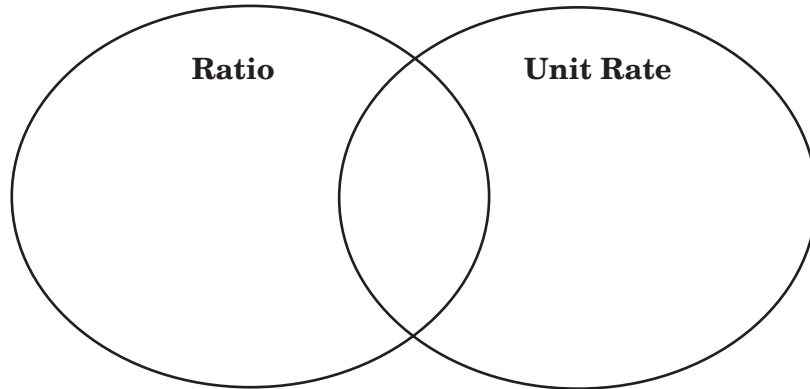
Main Idea

Find Unit Rates

p. 270

Details

Complete the Venn diagram by writing the phrases in the correct position. Use the phrases below the diagram.



usually a fraction
 4 miles to 1,000 feet
 has 1 in numerator
 5 inches per second

same units
 different units
 uses "out of"
 uses "per"

Compare Unit Rates

p. 271

Fill in each blank with $<$, $>$, or $=$ to compare the unit rates.

1. 10 notebooks for \$12 15 notebooks for \$18.75
2. 12 cans for \$4.20 20 cans for \$6
3. 171 miles with 9 gallons 300 miles with 15 gallons
4. 4,000 ft in 16 seconds 7,500 ft in 30 seconds
5. 77 pages in 1 hour 108 pages in 120 minutes

Helping You Remember

The word rate is part of the term *unit rate*.

Explain how a rate can be written as a unit rate.

6-3 Converting Rates and Measurements

What You'll Learn

Skim Lesson 6-3. Predict two things that you expect to learn based on the headings.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lesson 4-3*)

- _____ ▶ a mathematical sentence that contains an equals sign, (=), showing that two expressions are equal
- _____ ▶ a value for the variable that makes an equation true
- _____ ▶ operations that “undo” each other

New Vocabulary Fill in each blank with the correct term or phrase.

dimensional analysis ▶ the process of including _____ of _____ as factors when you compute

Vocabulary Link *Analysis* is a word that is used in everyday English. Find the definition of *analysis* using a dictionary. Explain how the English definition can help you remember how *analysis* is used in mathematics.

Lesson 6-3 (continued)

Main Idea

Details

Dimensional Analysis

pp. 275–276

Fill in each conversion factor and solve each problem.

- Convert 8 cups of juice per 1 gallon of water to cups of juice per quart of water.

$$\frac{8 \text{ cups}}{1 \text{ gallon}} \cdot \frac{1 \text{ gallon}}{\boxed{} \text{ quarts}} = \boxed{}$$

- Convert 110 millimeters per meter to millimeters per centimeter.

$$\frac{110 \text{ mm}}{1 \text{ m}} \cdot \frac{1 \text{ m}}{\boxed{}} = \boxed{}$$

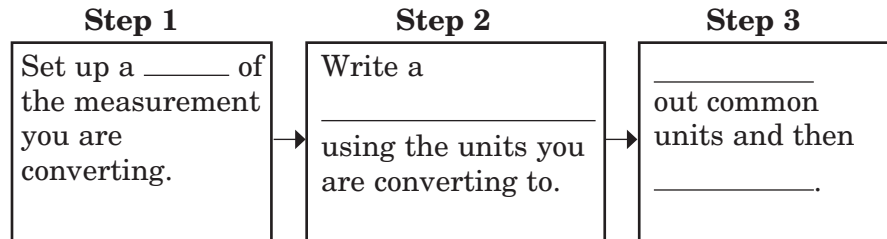
- Convert 80 ounces per minute to ounces per second.

$$\frac{80 \text{ oz}}{1 \text{ min}} \cdot \frac{\boxed{}}{\boxed{}} = \boxed{}$$

Convert Between Systems

pp. 276–277

Fill in the diagram to complete the steps to convert between measurement systems. Use the terms *simplify, ratio, divide, and conversion factor*.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Describe how to convert 18 pounds to kilograms.

In the conversion factor, which quantity is in the numerator and which quantity is in the denominator?

6-4 Proportional and Nonproportional Relationships

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match the term with the correct definition by drawing a line to connect the two. (*Lessons 6-1 and 6-2*)

ratio a simplified rate with a denominator of 1

unit rate a ratio with two quantities that have different kinds of units

rate comparison of two quantities by division

New Vocabulary Write the correct term next to each definition.

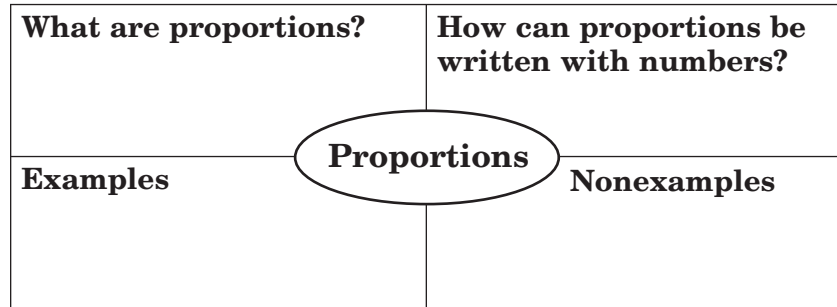
- _____ ► the relationship between two quantities where the ratio or rate is *not* constant
- _____ ► a constant ratio or unit rate of a proportion
- _____ ► a relationship where two quantities have a constant ratio or rate

Lesson 6-4 (continued)

Main Idea

Identify Proportions
pp. 281–282

Fill in the organizer about proportions.



Describe Proportional Relationships
p. 282

Fill in the blanks so that each table represents a proportional relationship.

1.

cups of juice	2	4	6	8
cups of water	6			

2.

oranges	1		3	
apples	4	8		16

3.

cats	3	9		
dogs	5		25	35

Helping You Remember

All relationships can be classified as either proportional or nonproportional. Think of six examples of numerical relationships that you use on a daily basis and classify each as proportional or nonproportional.

6-5 Solving Proportions

What You'll Learn

Scan the text in Lesson 6-5. Write two facts you learned about solving proportions.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term.
(Lesson 4-3)

equation ▶

solution ▶

New Vocabulary Fill in each blank with the correct word or phrase.

proportion ▶

an _____ that states that two _____ or rates are _____

cross products ▶

If $\frac{a}{b} = \frac{c}{d}$, then _____ = _____.

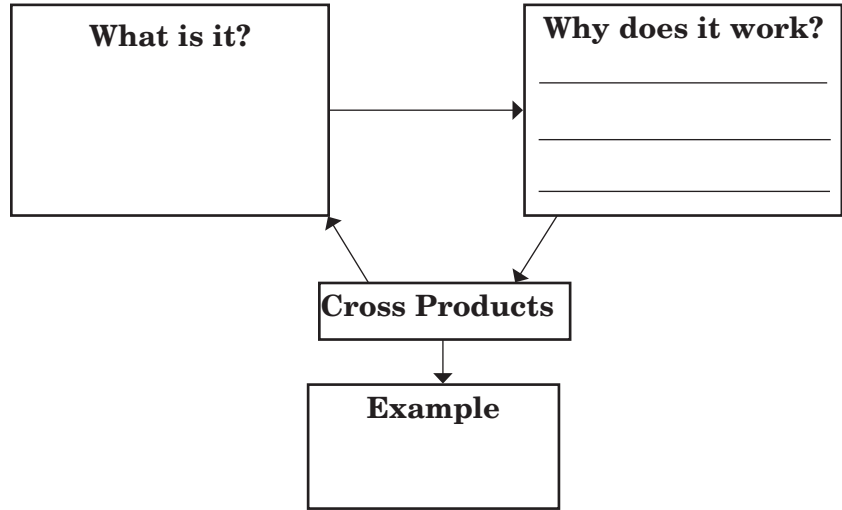
Lesson 6-5 (continued)

Main Idea

Details

Proportions
pp. 287–288

Complete the organizer for cross products.



Use Proportions to Solve Problems
pp. 288–289

Fill in each blank with a ratio that forms a proportion.

1. $\frac{4}{12} = \square$

2. $\frac{10}{20} = \square$

3. $\frac{3.0}{1.8} = \square$

4. $\frac{7}{28} = \square$

Helping You Remember

Proportion is a common word in the English language. Use a dictionary to look up its definition. Explain how the definition from the dictionary can help you remember the mathematical definition of *proportion*.

6-6 Scale Drawings and Models

What You'll Learn

Skim the lesson. Write two things you already know about scale drawings and models.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the term with the correct definition by drawing a line to connect the two.

- | | |
|----------------------|---|
| <i>scale factor</i> | a ratio of a given length on a scale model or drawing to its corresponding length on the actual object |
| <i>scale model</i> | a diagram used to represent an object that is too large or small to be drawn at actual size |
| <i>scale</i> | the relationship between the measurements on a drawing or model and the measurements of the real object |
| <i>scale drawing</i> | a model used to represent an object that is too large or small to be built at actual size |

Vocabulary Link *Scale* is a word that is used in everyday English. Find the definition of *scale* using a dictionary. Explain how the English definition can help you remember how *scale* is used in mathematics.

Lesson 6-6 (continued)

Main Idea

Use Scale Drawings and Models
pp. 294–295

Details

Fill in the table using the information provided.

The actual measurements of a 5-room apartment are in the table below. Use the scale of $\frac{1}{2}$ in. = 4 ft to find the missing lengths of the drawing.

Room	Living room	Kitchen	Bathroom	Bedroom #1	Bedroom #2
Actual length (ft)	14	10	6	8	12
Drawing length (in.)					

Construct Scale Drawings
p. 296

Construct a scale drawing of the floor plan of the 5-room apartment above using the values you calculated for the lengths of each room.

Helping You Remember

Explain how a scale is different than a scale factor.

6-7 Similar Figures

What You'll Learn

Scan Lesson 6-7. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition of *proportion* in your own words. (Lesson 6-4)

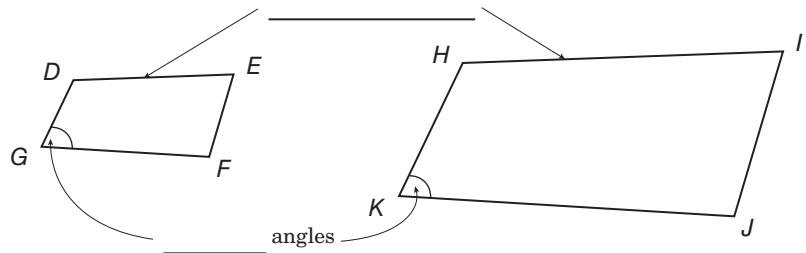
proportion ▶

New Vocabulary Quadrilateral $DEFG \sim$ quadrilateral $HJKI$. Label the diagram with the correct terms. Use each term once.

similar figures ▶

corresponding parts ▶

congruent ▶



$DEFG$ and $HJKI$ are _____.

Vocabulary Link *Similar* and *congruent* are two words used in everyday English. Find the definitions of *similar* and *congruent* using a dictionary.

Lesson 6-7 (continued)

Main Idea

Details

Corresponding Parts of Similar Figures

pp. 301–302

Use the triangles below.

List the congruent angles.

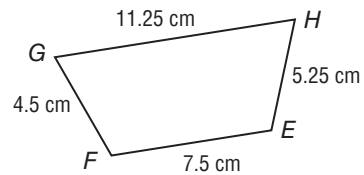
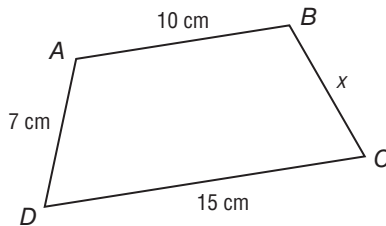
List the corresponding sides.

Scale Factors

p. 303

Fill in each blank to answer the questions about the figures below.

$ABCD \sim EFGH$



1. List all the corresponding sides. _____
2. List all the congruent angles.

3. What is the scale factor? _____
4. What is the value of x ? _____

Helping You Remember

Make a list of what you learned about similar figures.

figures.

6-8 Dilations**What You'll Learn**

Skim the Examples for Lesson 6-8. Predict two things you think you will learn about dilations.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match the term with its definition by drawing a line to connect the two. (*Lessons 1-4 and 2-7*)

x-coordinate a pair of numbers used to locate any point on a coordinate plane

ordered pair second number in an ordered pair

coordinate plane movement of a geometric figure

y-coordinate first number in an ordered pair

transformation formed by the intersection of two number lines that meet at right angles at their zero points

New Vocabulary Fill in each blank with the correct term or phrase.

dilation ► a _____ that enlarges or reduces a figure by a _____ factor

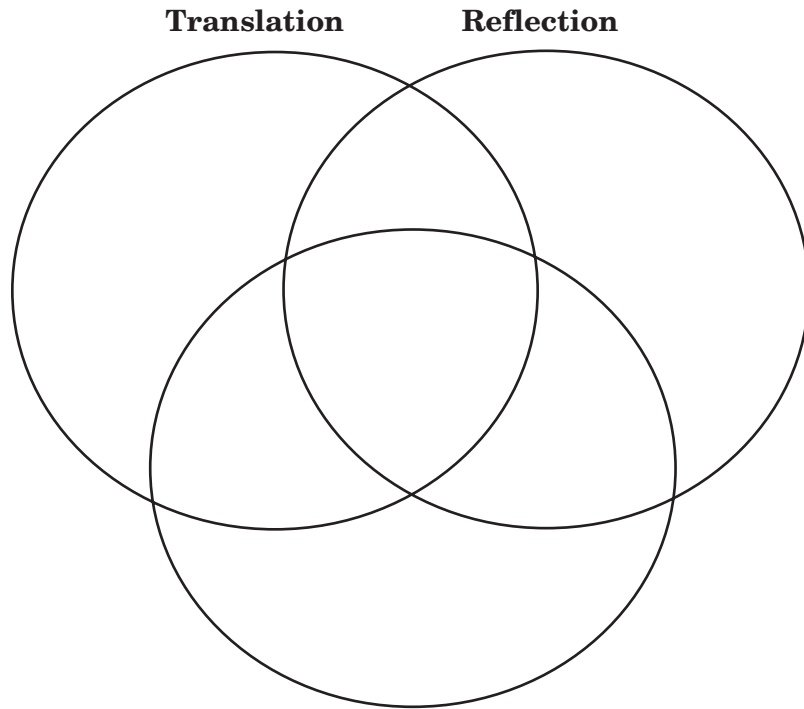
Lesson 6-8 (continued)

Main Idea

Details

Dilations
pp. 307–309

Compare and contrast the three types of transformations by completing the diagram below, using the terms under the diagram.



slide
enlarge or reduce
keeps original shape
same orientation

Dilation

changes size (unless $k = 1$)
same size
changes orientation
results in similar figures

Helping You Remember

Dilation is a word used in everyday English as well as in mathematics. Write the definition of *dilation*. Explain how the English definition can help you remember how *dilation* is used in mathematics.

6-9 Indirect Measurement

What You'll Learn

Skim the Examples for Lesson 6-9. Predict two things that you will learn about indirect measurement.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lessons 6-5 and 6-7*)

- _____ ▶ a statement of equality of two or more ratios
- _____ ▶ If $\frac{a}{b} = \frac{c}{d}$, then $ad = cb$.
- _____ ▶ figures that have the same shape but not necessarily the same size

New Vocabulary Fill in each blank with the correct term or phrase.

- indirect measurement* ▶ allows you to use the properties of _____ to find measurements that are difficult to measure _____

Vocabulary Link *Indirect* is a word that is used in everyday English. Find the definition of *indirect* using a dictionary. Explain how the English definition can help you remember how *indirect* is used in mathematics.

Lesson 6-9 *(continued)*

Main Idea

Details

Indirect Measurement

p. 313

Model the following situation with a labeled drawing. Then solve.

A flagpole casts a shadow that is 32 feet long. At the same time, a statue that is 7 feet tall casts a shadow that is $17\frac{1}{2}$ feet long. How tall is the flagpole?

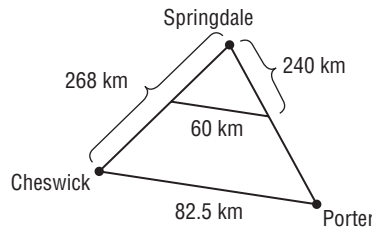


Surveying Methods

p. 314

Fill in the blank of the missing measure.

The triangles below are similar. What is the distance from Springdale to Porter?



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

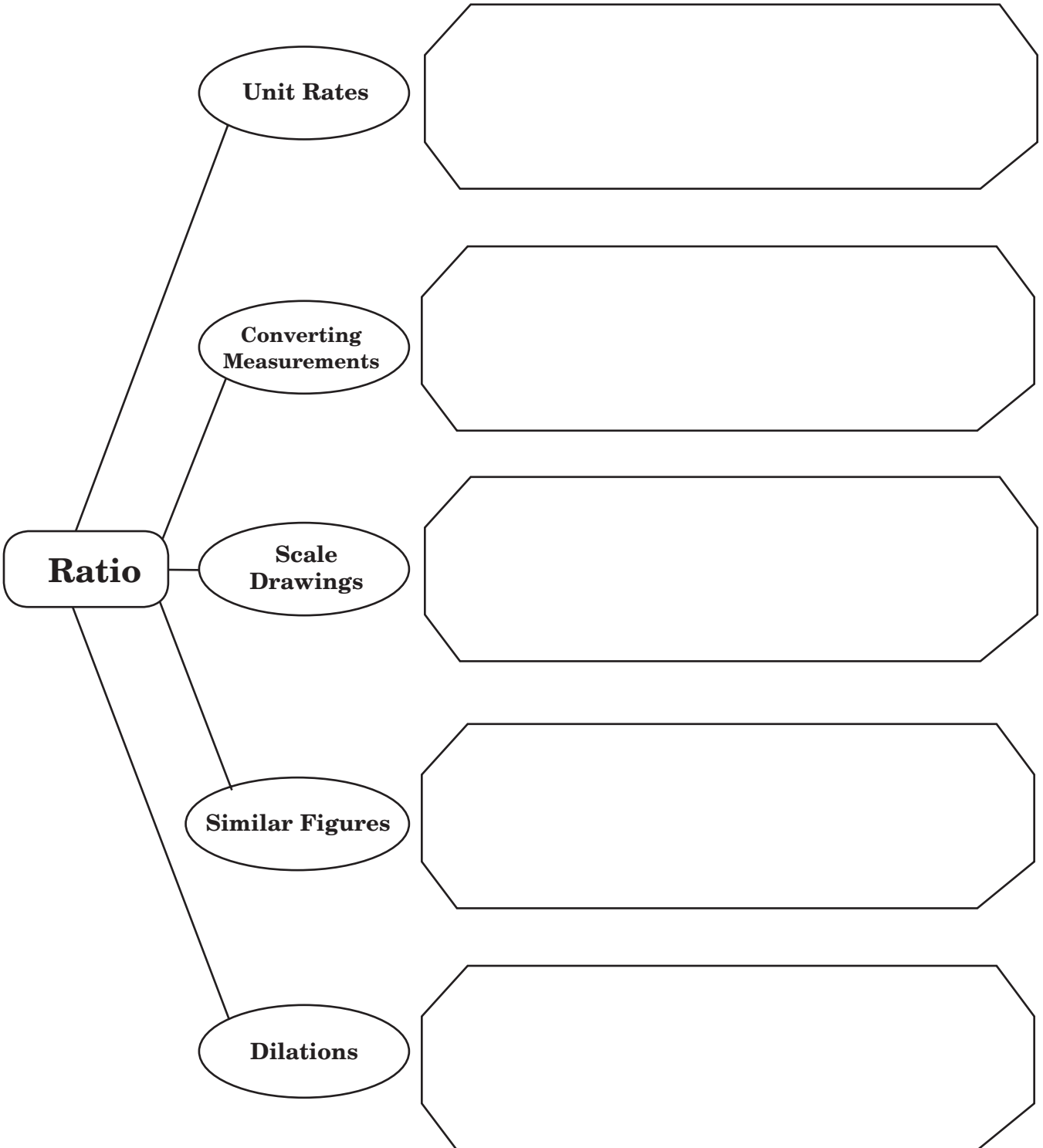
Write a paragraph explaining how to find a missing measurement using similar triangles to a classmate that was absent from class the day it was taught. Include an example.

CHAPTER
6

Ratio, Proportion, and Similar Figures

Tie It Together

Describe how ratios are used in each application.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
6

Ratio, Proportion, and Similar Figures

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Ratio, Proportion, and Similar Figures	After You Read
<ul style="list-style-type: none"> • A ratio is a comparison of quantities by addition. 	
<ul style="list-style-type: none"> • Unit rates are useful when comparing prices. 	
<ul style="list-style-type: none"> • Ratios are used to change a measurement from one unit to another. 	
<ul style="list-style-type: none"> • When two figures are proportional, they will have the same side and angle measures. 	
<ul style="list-style-type: none"> • A scale drawing is sometimes proportional to the actual object. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 6.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 6 Study Guide and Review in the textbook.
- I took the Chapter 6 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- You will do better on a test if you are relaxed. If you feel anxious, try some deep breathing exercises. Don't worry about how quickly others are finishing. Do your best and use all the time that is available to you.


 CHAPTER
7

Percent

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Percent
	<ul style="list-style-type: none"> • A percent is a comparison of a number and 100.
	<ul style="list-style-type: none"> • To write a decimal as a percent, divide by 100.
	<ul style="list-style-type: none"> • Percents can be written in fraction, decimal, or percent form.
	<ul style="list-style-type: none"> • A percent proportion is solved with cross products.
	<ul style="list-style-type: none"> • The percent equation can only be used with percents in their fraction form.


 FOLDABLES[®] Study Organizer

Construct the Foldable as directed at the beginning of this chapter.


 Note Taking Tips

- **When taking notes, write clean and concise explanations.**
Someone who is unfamiliar with the math concepts should be able to read your explanations and learn from them.
- **If your instructor points out definitions or procedures from your text, write a reference page in your notes.**
You can then write these referenced items in their proper place in your notes after class.


 CHAPTER
7

Percent

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on simple and compound interest, one fact might be that the formula used to solve simple interest problems is $I = prt$. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
7-1 Fractions and Percents	
7-2 Fractions, Decimals, and Percents	
7-3 Using the Percent Proportion	
7-4 Find Percent of a Number Mentally	
7-5 Using Percent Equations	
7-6 Percent of Change	
7-7 Simple and Compound Interest	
7-8 Circle Graphs	

7-1 Fractions and Percents

What You'll Learn

Scan Lesson 7-1. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lessons 6-1 and 6-4*)

- _____ ▶ a comparison of two quantities by division that is often written in fraction form
- _____ ▶ describes the relationship between two quantities where the ratio or rate is not constant
- _____ ▶ the k in the equation $y = kz$
- _____ ▶ a relationship where two quantities have a constant ratio or rate

New Vocabulary Write the definition next to the term.

percent ▶ _____

Vocabulary Link *Percent* is a word that is used in everyday English. Find the definition of *percent* using a dictionary. List two examples of everyday uses of *percents*.

Lesson 7-1

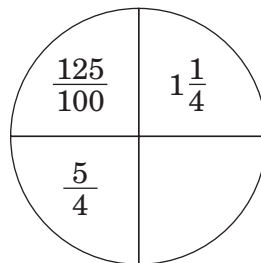
Lesson 7-1 (continued)

Main Idea

Percents as Fractions
pp. 331–332

Details

Fill in the fraction that completes the circle. Then define the relationship between the four parts.



The relationship:

Fractions as Percents
pp. 332–333

Fill in each blank of the proportion to find the percent following the given steps.

What percent is 16 out of 24?

$$\frac{16}{24} = \square$$

Write a proportion.

$$\square \cdot \square = \square \cdot \square$$

Cross products are equal.

$$\square = \square$$

Multiply.

$$\square = n$$

Simplify.

$$\text{So, } \frac{16}{24} = \square \text{ or } \square$$

Helping You Remember

Write and solve two questions where you would use proportions and percents to solve.

7-2 Fractions, Decimals, and Percents

What You'll Learn

Skim the lesson. Write two things you already know about fractions, decimals, and percents.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lessons 6-1, 6-5, and 7-1*)

- ratio* ▶ a _____ of two quantities by _____ that is usually written in _____ form
- percent* ▶ a _____ that compares a number to _____
- proportion* ▶ an _____ that states that two _____ or rates are _____
- cross products* ▶ If $\frac{a}{b} = \frac{c}{d}$, then _____ = _____.

Vocabulary Link The historical form of *percent* was *per cent*. Use a dictionary to look up the words *per* and *cent*. Relate these two meanings to the current definition of *percent*.

Lesson 7-2

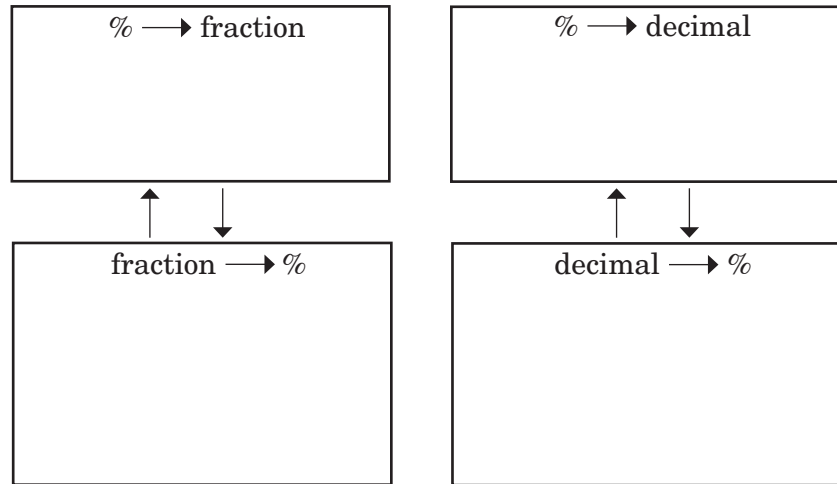
Lesson 7-2 (continued)

Main Idea

Details

Percents and Decimals
pp. 337–339

Complete the diagram by filling out each box with a description and example of each process described.



Compare Fractions, Decimals, and Percents
p. 339

At a local school, 22% of students walk to school, 0.35 take the bus, and three eighths are driven in a car. The rest of the students ride their bikes. Which of these groups are the largest?

Helping You Remember

Suppose you are a percent. Write a paragraph describing your experiences as a percent.

7-3 Using the Percent Proportion

What You'll Learn

Skim the Examples in Lesson 7-3. Predict two things that you think you will learn about using percent proportions.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match the term with its definition by drawing a line connecting the two. (*Lessons 4-3, 6-1, and 6-5*)

- | | |
|-----------------------|---|
| <i>equation</i> | a ratio that compares a number to 100 |
| <i>cross products</i> | a mathematical sentence that contains an equals sign, (=), showing that two expressions are equal |
| <i>proportion</i> | an equation that states that two ratios or rates are equal |
| <i>percent</i> | If $\frac{a}{b} = \frac{c}{d}$, then $ad = cb$. |

New Vocabulary Write the definition next to the term.

percent proportion ► _____

Vocabulary Link *Percent* and *proportion* are words that are used in everyday English. Find the definition of *percent* and *proportion* using a dictionary. How can their individual definitions help you remember what a percent proportion is?

Lesson 7-3 (continued)

Main Idea

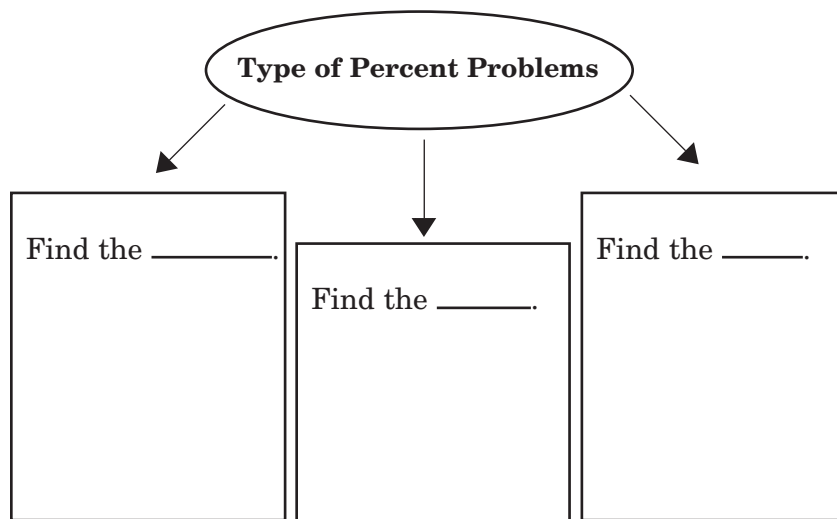
Details

The Percent Proportion
pp. 345–347

Complete the model for the *percent proportion*.

$$\frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}}$$

Complete the organizer. Write the types of percent problems. Then write a word problem to show an example for each.



Helping You Remember

Fill in each blank to identify the whole, the part, and the percent in the following percent proportion.

$$\frac{\underline{\hspace{1cm}}}{\underline{\hspace{1cm}}} = \left(\frac{65}{100} \right) \frac{\underline{\hspace{1cm}}}{\underline{\hspace{1cm}}}$$

7-4 Find Percent of a Number Mentally

What You'll Learn

Skim Lesson 7-4. Predict two things you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lessons 6-2, 6-5, 7-1, and 7-2*)

- _____ ▶ a ratio that compares a number to 100
- _____ ▶ a ratio that compares part of a quantity to the whole quantity
- _____ ▶ a ratio of two quantities that have different kinds of units
- _____ ▶ an equation that states two ratios or rates are equal

Vocabulary Link *Mental* and *math* are both words used in everyday English. Look up *mental* and *math* in the dictionary. Explain how the two words fit together to be the *mental math* that is used in everyday mathematics.

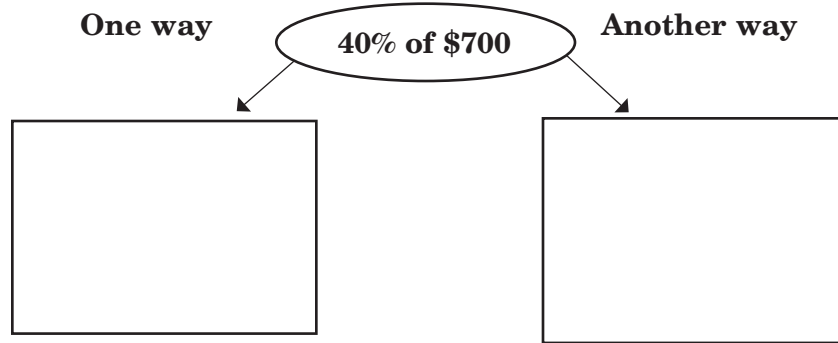
Lesson 7-4 (continued)

Main Idea

Find Percent of a Number Mentally
pp. 351–352

Details

Complete the organizer with two ways that you can mentally find 40% of \$700.



Estimates with Percents
pp. 352–353

Fill in the table with the mental strategy of how you found the estimate. Use a different strategy each time.

Estimate the Answer	Describe your Strategy
150% of 98	
76% of 160	
$\frac{1}{2}\%$ of 280	

Helping You Remember

There are situations when an exact answer is needed. There are other times when an estimate is good enough. Give examples of when an exact answer and an estimate are appropriate. Explain your reasoning.

7-5 Using Percent Equations

What You'll Learn

Scan the text in Lesson 7-5. Write two facts you learned about solving using percent equations as you scanned the text.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term. (Lessons 4-3, 6-5, and 7-3)

proportion ▶

percent proportion ▶

equation ▶

cross products ▶

New Vocabulary Fill in each blank with the correct term or phrase.

percent equation ▶

an _____ form of the _____ in which the percent is written as a _____

Lesson 7-5 (continued)

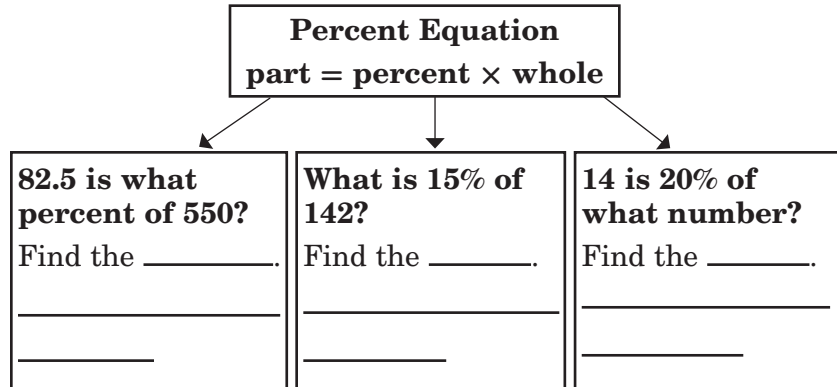
Main Idea

Details

Percent Equations

pp. 357–359

Complete the organizer. Write the type of percent problem using the terms part, whole, and percent. Then solve using the percent equation.



Fill in each blank using the information below.

Terri and Kraig each bought an MP3 player. Terri paid \$45 minus an 18% discount. Kraig has a coupon for 15% off, which is a \$6 discount.

1. What is the original price of Kraig’s player?
2. How much did Terri pay after her discount?
3. Suppose Kraig pays 6.5% and Terri pays 6% sales tax. How much did Kraig and Terri spend total for both players, including tax? Round to the nearest cent if needed.

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

The label over each oval represents what is missing from a percent equation. In each oval, write and solve a percent equation to find that missing information.

Missing Whole

Missing Part

Missing Percent

7-6 Percent of Change

What You'll Learn

Skim Lesson 7-6. Predict two things that you expect to learn based on the headings and Key Concept box.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the term with the correct definition by drawing a line to connect the two.

<i>percent of decrease</i>	ratio that compares the change in quantity to the original amount
<i>selling price</i>	the amount the price of an item is increased above the price the store paid for an item
<i>discount</i>	a positive percent of change
<i>percent increase</i>	total amount consumer pays for item
<i>markup</i>	a negative percent of change
<i>percent of change</i>	the amount by which the regular price of an item is reduced

Vocabulary Link *Percent change* is a term that is used in everyday English. List two ways in which *percent change* is used in everyday life.

Lesson 7-6

Lesson 7-6 (continued)

Main Idea

Details

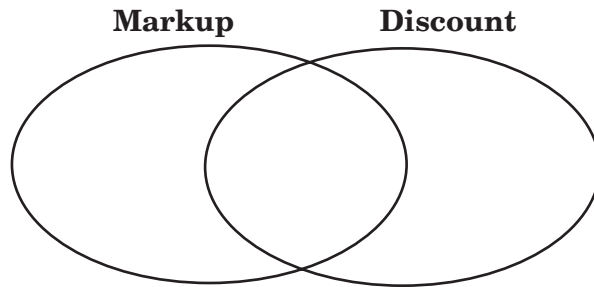
Find Percent of Change
pp. 364–365

Find the percent of change. Round to the nearest tenth if necessary. Then fill in each blank with either *percent increase* or *percent decrease*.

1. from 89° to 77° _____ percent of _____.
2. from \$45 to \$58 _____ percent of _____.
3. In her first week of training, Cherie ran 5.4 miles. Six weeks later she ran 7.1 miles. What is the percent change in the 6 weeks? _____
4. Marcus weighed 113 pounds at the start of wrestling season and 106 pounds at the end. What is the percent change from the start to the end of the season?

Using Markup and Discount
pp. 365–366

Complete the Venn diagram for the terms *markup* and *discount*. Use the terms *percent increase*, *percent decrease*, *percent of change*, *positive*, and *negative*.



Helping You Remember

For a percent of increase, is the percent of change always positive or negative? Why? For a percent of decrease, is the percent of change always positive or negative? Why?

7-7 Simple and Compound Interest

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in this lesson.

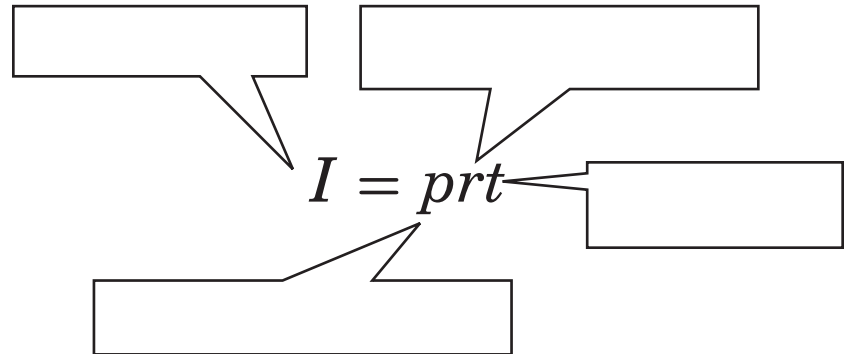
1. _____

2. _____

Active Vocabulary

New Vocabulary Label the diagram with the correct terms.

- principal* ▶
- interest* ▶
- annual interest rate* ▶
- time year* ▶



Vocabulary Link *Principal* is a word used in everyday English as well as in mathematics. Write the definition of *principal*. Explain how the English definition can help you remember how *principal* is used in mathematics.

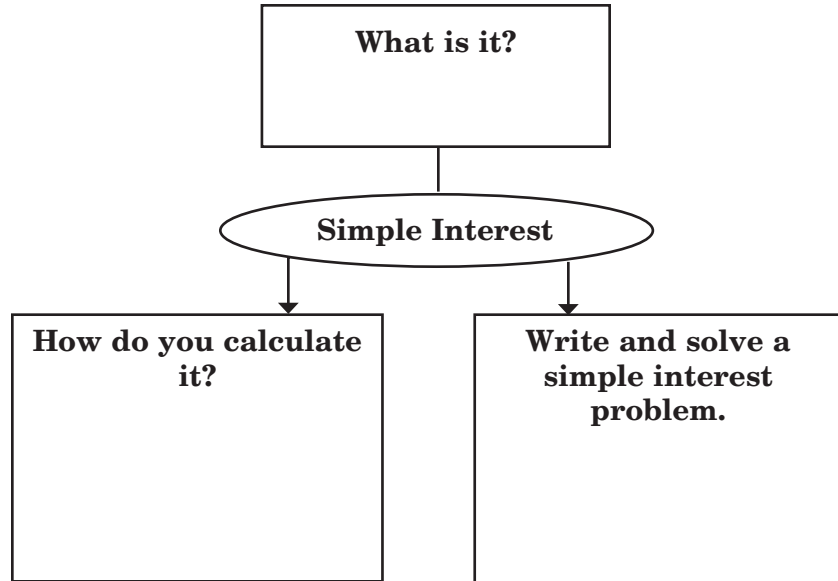
Lesson 7-7 (continued)

Main Idea

Simple Interest
pp. 370–371

Details

Complete the organizer. Sample answers are given.



Compound Interest
p. 371

Compare the two types of interest.

Types of Interest	Description
Simple	
Compound	

Helping You Remember

Write a real-world problem dealing with compound interest. Find the answer then trade with a partner and solve.

7-8 Circle Graphs

What You'll Learn

Skim the Examples for Lesson 7-8. Predict two things you think you will learn about circle graphs.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to each definition.
(Lessons 3-1 and 7-1)

_____ ▶

a decimal whose digits end

_____ ▶

a decimal whose digits repeat in groups of one or more without end

_____ ▶

a ratio that compares a number to 100

New Vocabulary Write the definition next to the term.

circle graph ▶

Vocabulary Link A circle graph displays data. Look up *data* in a dictionary. Find a sentence in the lesson that uses that word.

Definition: _____

Sentence: _____

Lesson 7-8 (continued)

Main Idea

Details

Circle Graphs

pp. 376–377

Model a circle graph by following the steps below.

Count the number of students in your classroom. Then count the number of students that are wearing various colored shirts. For example, there may be 7 students wearing blue shirts, 3 wearing pink shirts, and 6 wearing white shirts. Construct and label a circle graph with your data.

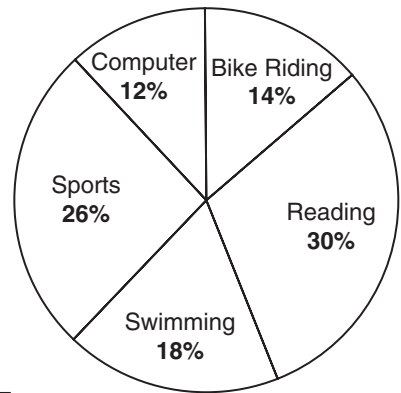
Analyze Circle Graphs

p. 378

Answer each question using the circle graph.

250 students were surveyed about their favorite activities. The results are in the circle graph.

Favorite Activity



How many students favor computer? _____

How many more students favor sports than favor swimming? _____

Which activity is most favored?

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Describe how to construct a circle graph in detail

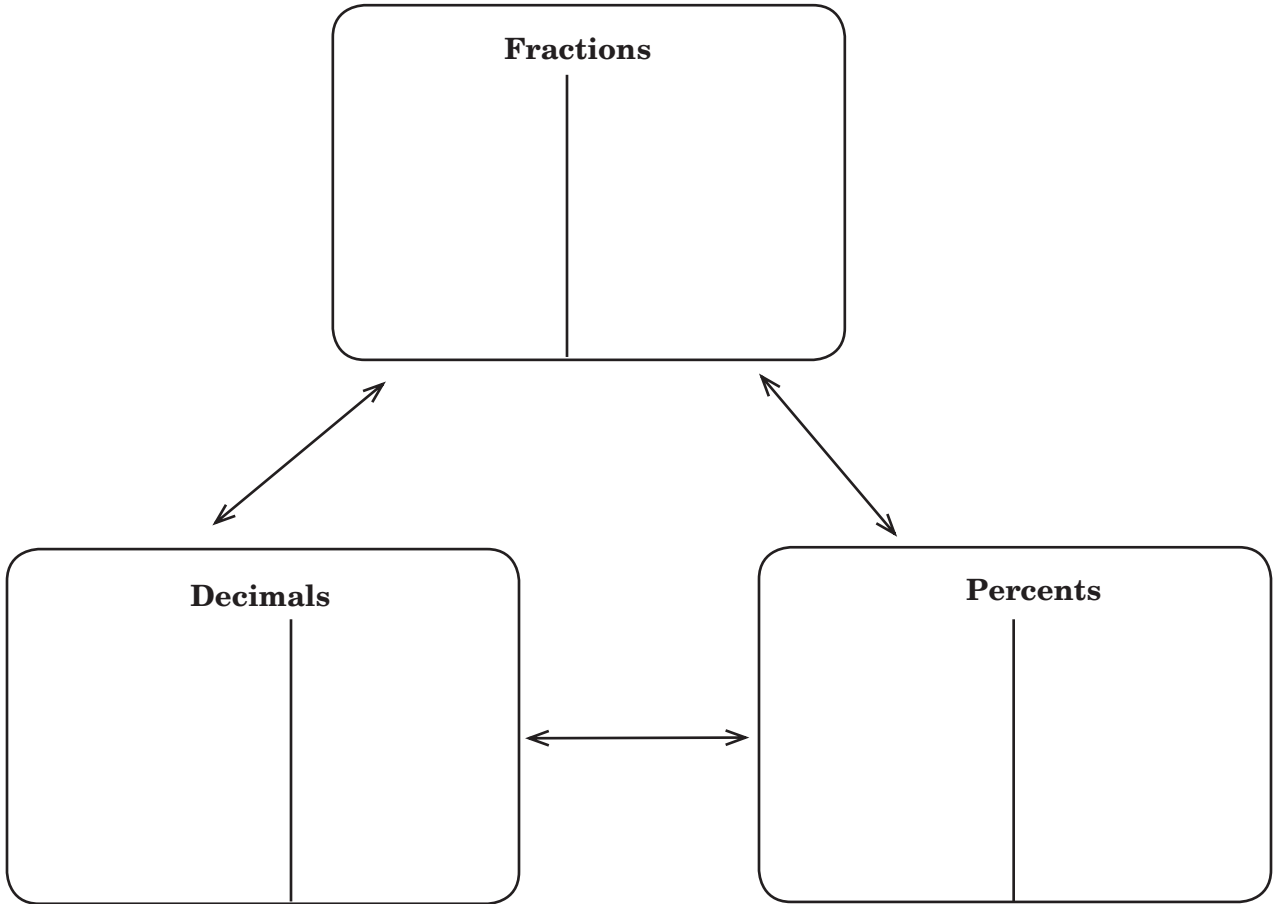
to a classmate who was absent.

CHAPTER
7

Percent

Tie It Together

Use the fraction $\frac{3}{4}$ to show how to convert to different forms of numbers.



Complete the proportion with the words “part”, “whole”, and the symbols % and 100.


 CHAPTER
7

Percent

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Percent	After You Read
<ul style="list-style-type: none"> • A percent is a comparison of a number and 100. 	
<ul style="list-style-type: none"> • To write a decimal as a percent, divide by 100. 	
<ul style="list-style-type: none"> • Percents can be written in fraction, decimal, or percent form. 	
<ul style="list-style-type: none"> • A percent proportion is solved with cross products. 	
<ul style="list-style-type: none"> • The percent equation can only be used with percents in their fraction form. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 7.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 7 Study Guide and Review in the textbook.
- I took the Chapter 7 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Designate a place to study at home that is free of clutter and distraction. Try to study at about the same time each afternoon or evening so that it is part of your routine.

CHAPTER
8

Linear Functions and Graphing

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Linear Function and Graphing
	<ul style="list-style-type: none"> • In a function, a member of the domain can be paired with more than one member of the range.
	<ul style="list-style-type: none"> • An arithmetic sequence has a common ratio between each term.
	<ul style="list-style-type: none"> • A linear function has both straight and curved lines.
	<ul style="list-style-type: none"> • If a rate of change is proportional, its graph will be a straight line.
	<ul style="list-style-type: none"> • In the equation $y = 5x + 3$, the slope is 3.

FOLDABLES Study Organizer

Construct the Foldable as directed at the beginning of this chapter.

 **Note Taking Tips**

- **When you take notes, write concise definitions in your own words.**
Add examples that illustrate the concepts.
- **When taking notes, write down a question mark by anything you do not understand.**
Before your next quiz, ask your instructor to explain these sections.

CHAPTER
8

Linear Functions and Graphing

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on slope, one fact might be that positive slopes represent a rate of increase. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
8-1 Functions	
8-2 Sequences and Equations	
8-3 Representing Linear Functions	
8-4 Rate of Change	
8-5 Constant Rate of Change and Direct Variation	
8-6 Slope	
8-7 Slope-Intercept Form	
8-8 Writing Linear Equations	
8-9 Prediction Equations	
8-10 Systems of Equations	

8-1 Functions

What You'll Learn

Skim the Examples for Lesson 8-1. Predict two things you think you will learn about functions.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match each term with its definition by drawing a line to connect the two.

- | | |
|-----------------------------|--|
| <i>function notation</i> | a value that is chosen and does not depend on the other variable |
| <i>independent variable</i> | a value that depends on the input value |
| <i>vertical line test</i> | a way to write an equation using $f(x)$ |
| <i>dependent variable</i> | use to determine if a graph is a function |

Vocabulary Link *Independent* and *dependent* are two words used in everyday English. Find the definitions of *independent* and *dependent* using a dictionary. Write an example of a variable in everyday life that is *independent*. Write an example of a variable that is *dependent*.

Lesson 8-1

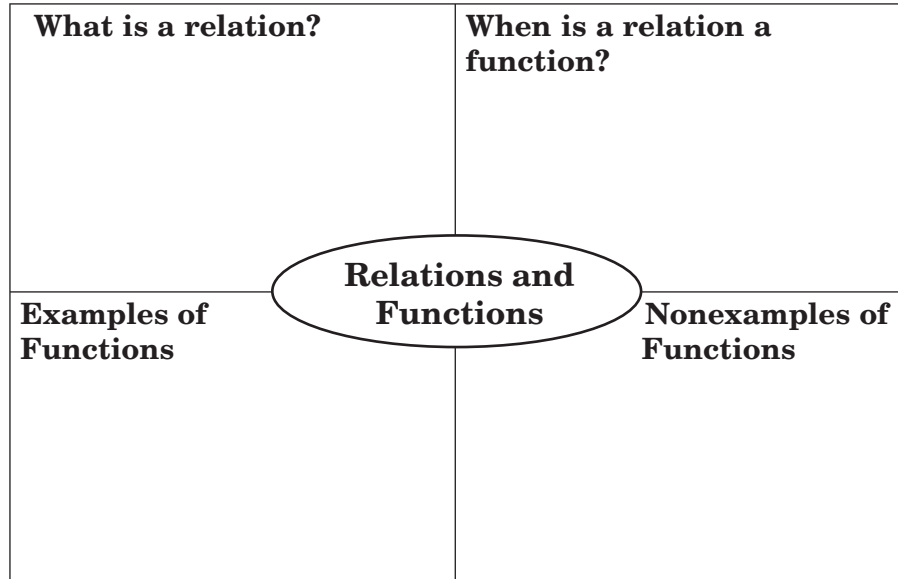
Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Lesson 8-1 (continued)

Main Idea **Details**

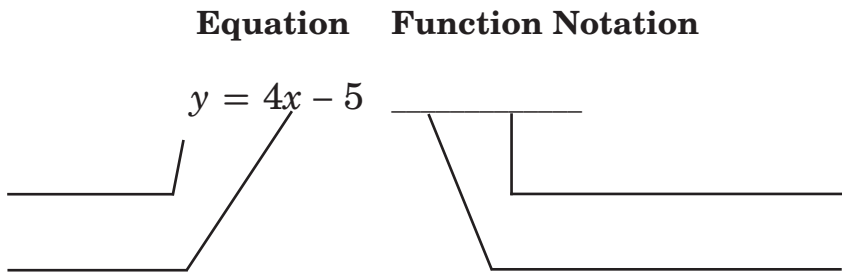
Relations and Functions
pp. 395–396

Complete the organizer for *functions*.



Function Notation
p. 396

Write the equation in function notation. Label *both* forms with the terms *independent variable* and *dependent variable*.



Describe Relationships
p. 397

In the function above, what is the value of y if $x = 7$? ____

Helping You Remember Explain how the vertical line test works to tell whether a relation is a function.

8-2 Sequences and Equations

What You'll Learn

Scan Lesson 8-2. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

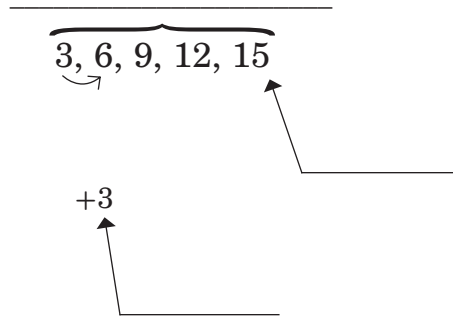
Active Vocabulary

New Vocabulary Label the diagram with the correct terms.

common difference ▶

arithmetic sequence ▶

term ▶



Main Idea

Details

Describe Sequences
p. 401

Fill in each blank to complete the arithmetic sequence.

Term Number (<i>n</i>)	1		3	
Term (<i>t</i>)	12		24	

The difference of the term numbers is ____.

The common difference of the terms is ____.

The equation that describes the sequence is _____.

Lesson 8-2 (continued)

Main Idea

Details

Finding Terms
p. 402

Complete the organizer to find a term in an arithmetic sequence.

To find a term in an arithmetic sequence...

14, 21, 28, 35, 42, 49, ...
Find the 11th term.

Step 1: Find the common difference.

Step 1:

Step 2: Write an equation to describe the sequence.

Step 2:

Step 3: Use the equation to find the term.

Step 3:

Helping You Remember

Suppose you are an arithmetic sequence. Write a paragraph describing your experiences.

8-3 Representing Linear Functions

What You'll Learn

Scan the text in Lesson 8-3. Write two facts you learned about representing linear functions as you scanned the text.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to each definition. (*Lesson 1-5*)

_____ ► a mathematical sentence stating that two quantities are equal

_____ ► a relation where each member of the domain is paired with exactly one member in the range

New Vocabulary Fill in each blank with the correct term or phrase.

linear equation ► an equation whose graph is a _____

x-intercept ► the _____ of the point at which the graph crosses the _____

y-intercept ► the _____ of the point at which the graph crosses the _____

Lesson 8-3 (continued)

Main Idea

Solve Linear Equations
pp. 406–407

Details

Fill in the blanks to complete each table. Write the ordered pairs under the table.

1. $y = 3x + 1$

x	y
-2	
	1
	4
2	

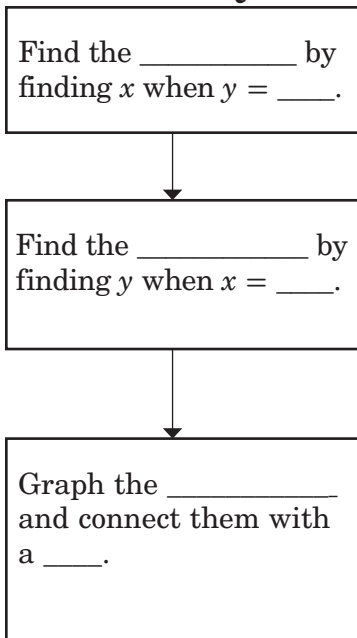
2. $y = -x + 2$

x	y
-1	
	2
2	0
3	-1

Graph Linear Equations
pp. 407–408

Compare the two methods of graphing a linear function.

One Way:

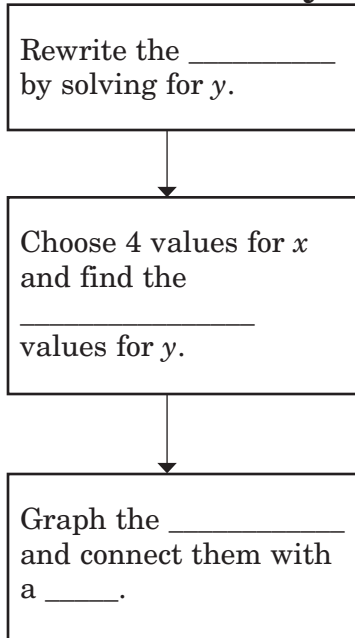


Step 1

Step 2

Step 3

Another Way:



8-4 Rate of Change

What You'll Learn

Skim Lesson 8-4. Predict two things that you expect to learn based on the headings and the Key Concept Box.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to the term.

rate of change ►

Main Idea

Details

Rate of Change
pp. 412–414

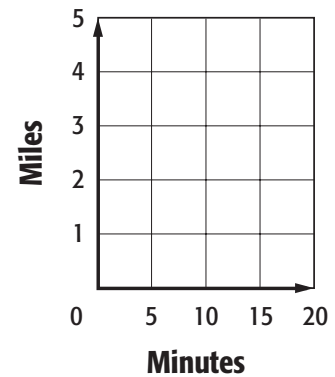
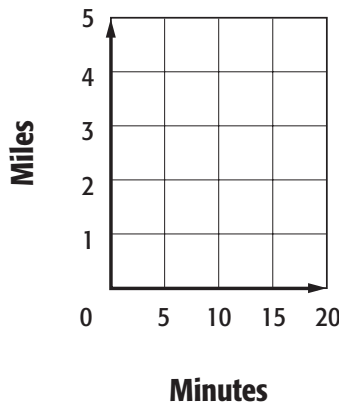
Model a graph with a *positive* and then a *negative* rate of change. Describe your graph with words.

Positive Rate of Change

Negative Rate of Change

Time and Distance Traveled

Time and Distance Traveled



Lesson 8-4 (continued)

Main Idea

Details

Summarize the following situation.

Emily is filling a bathtub with water. She turns the faucet on, and 7 minutes later when the bathtub is full, she turns the faucet off.

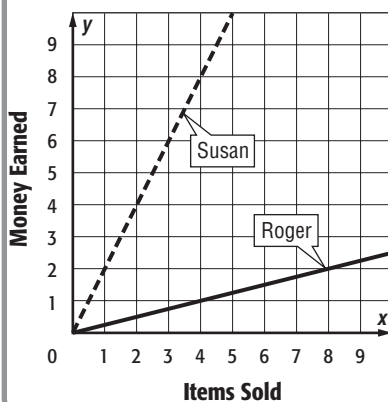
Describe the rate of change. How would the graph of the water flow appear?

Describe another situation where the rate of change of the graph would appear the same.

Helping You Remember

The graph below shows the earnings of Roger and Susan. Compare the two rates of change by comparing the steepness of the lines.

Roger's and Susan's Earnings



8-5 Constant Rate of Change and Direct Variation

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term.
(Lessons 6-4 and 8-4)

rate of change ▶

proportion ▶

New Vocabulary Write the correct term next to each definition.

_____ ▶ the constant of proportionality, the k in the equation $y = kx$

_____ ▶ the relationship between two quantities that results in a straight-line graph

_____ ▶ when the ratio between two variable quantities is constant

_____ ▶ a linear relationship where the rate of change between any two data points is the same

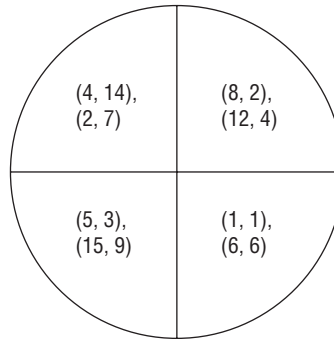
Lesson 8-5 (continued)

Main Idea

Constant Rate of Change
pp. 418–420

Details

Cross out the set of coordinates in the circle that do not belong. Then describe the relationship.



The relationship is _____.

Direct Variation
pp. 420–421

Fill in the organizer about *direct variation*.

What is it?	How can it be written using symbols?
Examples	Nonexamples

Helping You Remember

All directly proportional relationships are linear, but not all linear relationships are proportional. Give an example of a linear relationship that has a constant rate of change but is not proportional.

8-6 Slope

What You'll Learn

Skim the lesson. Write two things you already know about slope.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lessons 6-1 and 8-5*)

ratio ▶ a _____ of two _____ by division that is often written in _____ form

constant rate of change ▶ a _____ where the rate of change between any two data points is _____

New Vocabulary Write the definition next to the term.

slope ▶ _____

Main Idea

Slope
pp. 427–428

Details

Match the different types of slopes to the correct coordinates by drawing a line to connect the two.

positive slope $A(2, 4), B(2, 5)$

negative slope $C(-5, 3), D(-3, 2)$

undefined slope $E(7, 4), F(-7, 4)$

zero slope $G(-1, -3), H(-3, -5)$

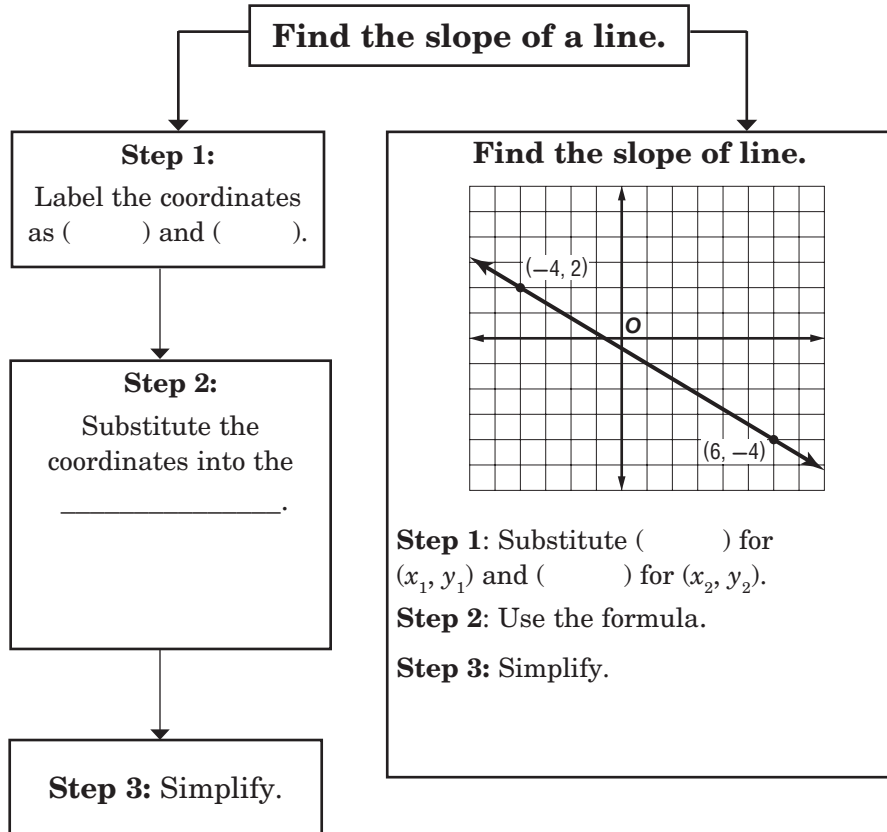
Lesson 8-6 (continued)

Main Idea

Slope and Constant Rate of Change
pp. 428–429

Details

Complete the organizer to find the slope of a line. Fill in each blank to find the slope in the example.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Use words to describe how a line appears with

the given slopes.

positive: _____

negative: _____

zero: _____

undefined: _____

8-7 Slope-Intercept Form

What You'll Learn

Skim the Example for Lesson 8-7. Predict two things you think you will learn about slope-intercept form.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lessons 6-5 and 8-3*)

_____ ▶ a statement of equality of two or more ratios

_____ ▶ an equation whose graph is a straight line

_____ ▶ the first number of an ordered pair

_____ ▶ the second number of an ordered pair

New Vocabulary Write the definition next to the term.

slope-intercept form ▶ _____

Lesson 8-7 (continued)

Main Idea

Find Slope and y-intercept

pp. 433–434

Details

Identify the slope and y-intercept in each equation.

1. $y = 4x + 5$ slope: _____ y-intercept: _____

2. $x + y = 6$ slope: _____ y-intercept: _____

3. $y + 3 = -7x$ slope: _____ y-intercept: _____

4. $-x - y = -2$ slope: _____ y-intercept: _____

Graph Equations

pp. 434–435

Complete the organizer by following the steps given to graph an equation.

Step 1: Find the slope and y-intercept.

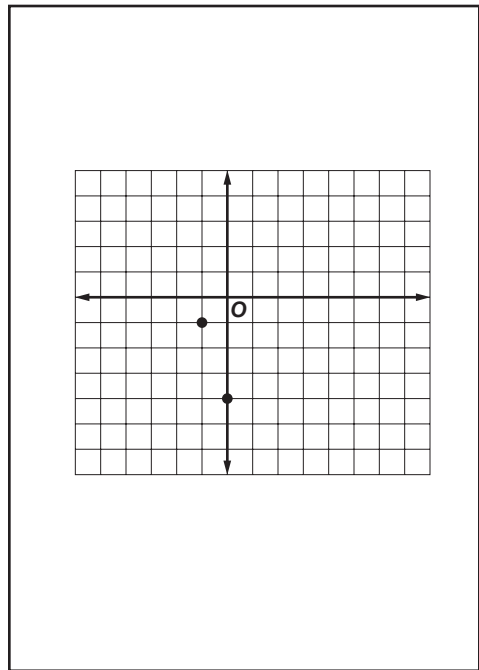
Graph: $y = -3x - 4$

Step 1: slope: _____ y-intercept: _____

Step 2: Graph the y-intercept at $(0, -4)$.

Step 3: Write the slope as $\frac{-3}{1}$. Use it to locate another point on the line.

Step 4: Draw a line through the 2 points and extend the line.



8-8 Writing Linear Equations

What You'll Learn

Skim Lesson 8-8. Predict two things that you expect to learn based on the headings and the Key Concept Box.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lessons 8-6 and 8-7*)

slope ► the ratio of the _____, or _____ change, to the _____, or _____ change of a line

slope-intercept form ► a linear _____ in the form _____, where m is the slope and b is the _____

New Vocabulary Write the definition next to the term.

point-slope form ► _____

Lesson 8-8 (continued)

Main Idea

Write Equations in Slope-Intercept Form

pp. 441–442

Solve Problems

pp. 443–444

Details

Fill in each blank to write a linear equation given two points.

Given: (4, -5), and (-1, -3)

Find the slope: $m = \frac{\text{change of } y}{\text{change of } x} =$

Use $y - y_1 = m(x - x_1)$ form: $y - (\underline{\quad}) = \underline{\quad}(x - (\underline{\quad}))$.

Simplify to $y - mx + b$ form: $y = \underline{\quad} - \underline{\quad}$.

Complete the chart by summarizing the procedure.

Writing Linear Equations	
Forms	Procedure
from slope and y-intercept	
from a graph	
from two points	
from a table	

8-9 Prediction Equations

What You'll Learn

Scan the text in Lesson 8-9. Write two facts you learned about prediction equations as you scanned the text.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to the term. (Lesson 1-6)

scatter plot ►

New Vocabulary Fill in each blank with the correct term or phrase.

line of fit ►

a _____ that is drawn on a _____ that closely approximates the _____

Vocabulary Link In this lesson you will make *predictions* using a line or equation. *Prediction* is a word that is used in everyday English. Find the definition of *prediction* using a dictionary. Give an example of how *predictions* are used in everyday life.

Lesson 8-9 (continued)

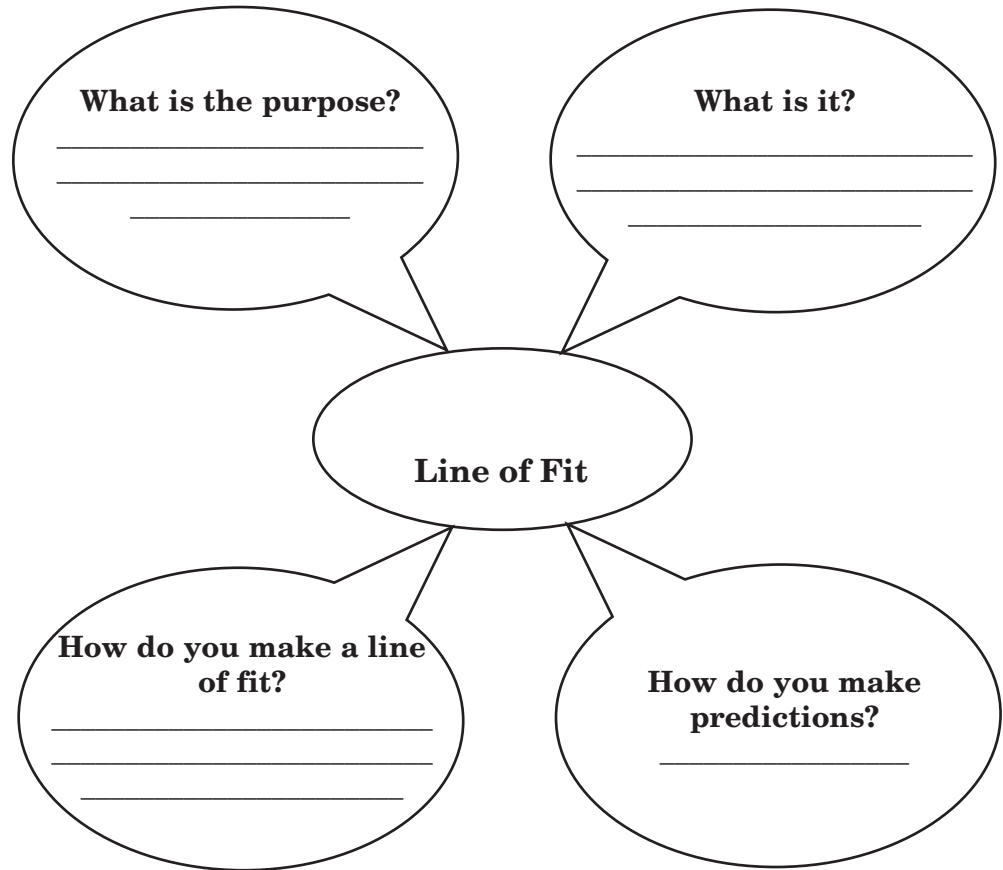
Main Idea

Details

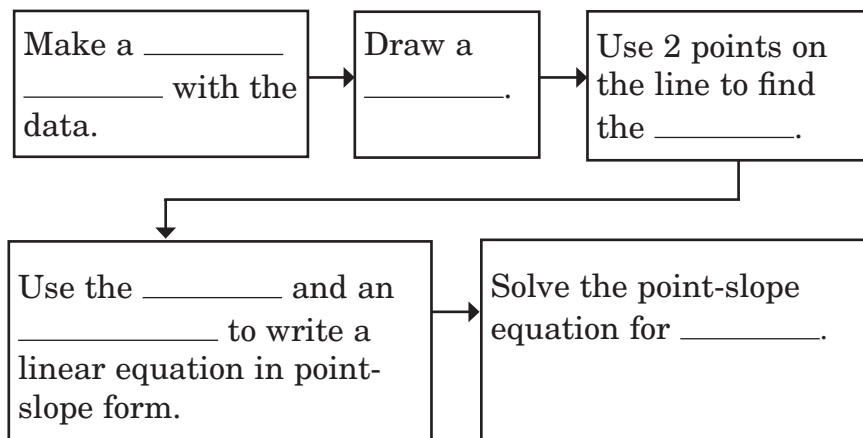
Lines of Fit

p. 448

Complete the organizer about the *line of fit*.



Fill in each blank to complete the graphic organizer for finding the equation of a line of best fit.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

8-10 Systems of Equation

What You'll Learn

Scan Lesson 8-10. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Fill in each blank with the correct term or phrase.

system of equations ► a set of two or more _____ with the same _____

substitution ► an _____ method of finding an exact _____ of a system of equations

Vocabulary Link *Substitution* is a word used in everyday English. Find the definition of *substitution* using a dictionary. Explain how the English definitions can help you remember how *substitution* is used in mathematics.

Lesson 8-10 (continued)

Main Idea

Solve Systems by Graphing
pp. 453–454

Details

Compare solutions by completing the chart.

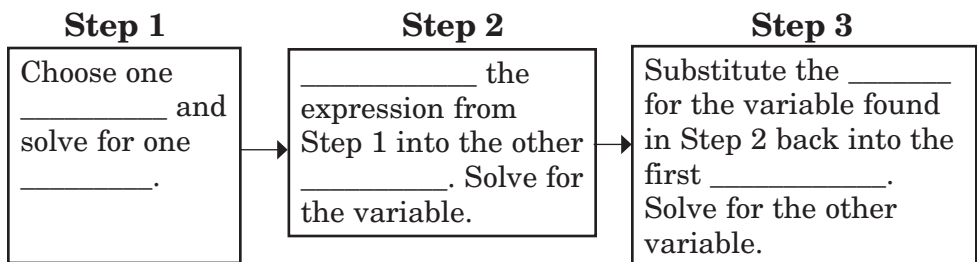
Solutions for Systems of Equations		
Solution	Description	Graph
infinite solutions	_____	

one solution	_____	

no solutions	_____	

Solve Systems by Substitution
p. 455

Fill in the diagram to complete the steps to solve a system of equations by substitution. Use the terms *variable*, *value*, *equation*, and *substitute* as often as needed.



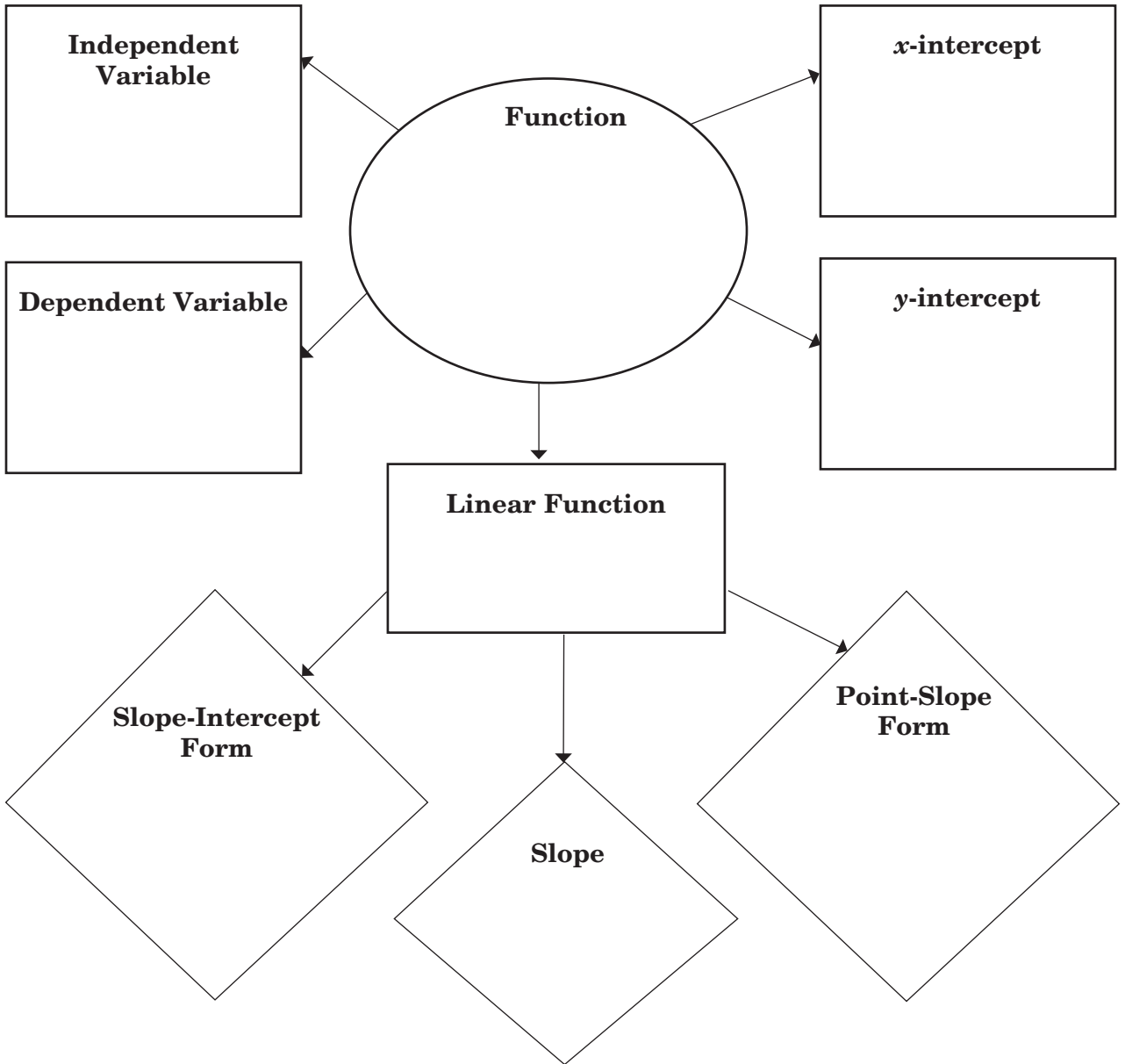
Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

CHAPTER
8

Linear Functions and Graphing

Tie It Together

Complete the graphic organizer with definitions and concepts about each topic.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
8

Linear Functions and Graphing

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Linear Function and Graphing	After You Read
<ul style="list-style-type: none"> • In a function, a member of the domain can be paired with more than one member of the range. 	
<ul style="list-style-type: none"> • An arithmetic sequence has a common ratio between each term. 	
<ul style="list-style-type: none"> • A linear function has both straight and curved lines. 	
<ul style="list-style-type: none"> • If a rate of change is proportional, its graph will be a straight line. 	
<ul style="list-style-type: none"> • In the equation $y = 5x + 3$, the slope is 3. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 8.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 8 Study Guide and Review in the textbook.
- I took the Chapter 8 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Be an active listener in class. Take notes, circle or highlight information that your teacher stresses, and ask questions when ideas are unclear to you.


 CHAPTER
9

Powers and Nonlinear Functions

Before You Read

Before you read the chapter, think about what you know about powers and nonlinear functions. List three things you already know about them in the first column. Then list three things you would like to learn about them in the second column.

K What I know...	W What I want to find out...


 FOLDABLES® Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- When you take notes, be sure to listen actively.**
 Always think before you write, but don't get behind in your note-taking. Remember to enter your notes legibly.
- When you take notes, circle, underline, or star anything the teacher emphasizes.**
 When your teacher emphasizes a concept, it will usually appear on a test, so make an effort to include it in your notes.

CHAPTER
9

Powers and Nonlinear Functions

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on prime factorization, one fact might be that a monomial is a number, a variable, or a product of numbers and/or variables. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
9-1 Powers and Exponents	
9-2 Prime Factorization	
9-3 Multiplying and Dividing Monomials	
9-4 Negative Exponents	
9-5 Scientific Notation	
9-6 Powers of Monomials	
9-7 Linear and Nonlinear Functions	
9-8 Quadratic Functions	
9-9 Cubic and Exponential Functions	

9-1 Powers and Exponents

What You'll Learn

Skim Lesson 9-1. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to the term.
(Lesson 1-1)

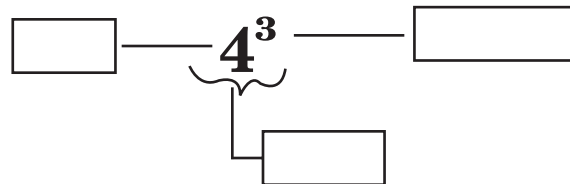
order of operations ▶

New Vocabulary Label the diagram with the correct term.

exponent ▶

power ▶

base ▶



Vocabulary Link *Base* is a word that is used in everyday English. Find the definition of *base* using a dictionary. Explain how the English definition can help you remember how *base* is used in mathematics.

Lesson 9-1

Lesson 9-1 (continued)

Main Idea

Details

Use Exponents

pp. 471–472

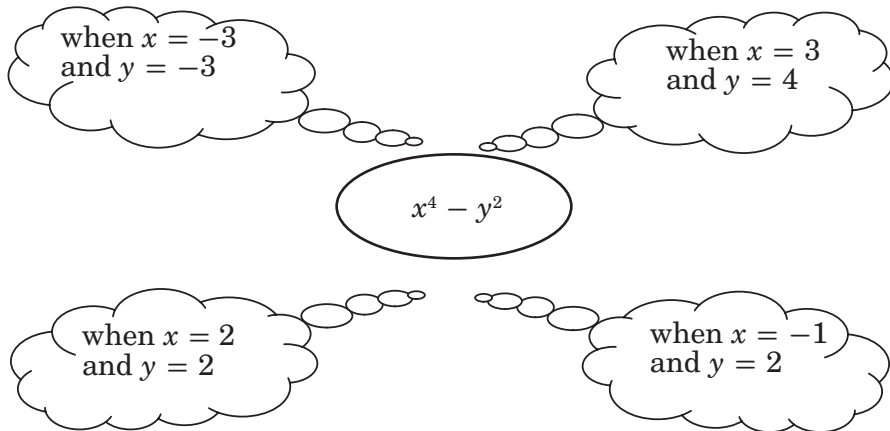
Fill in the blank for each verbal expression with a numeric expression with exponents.

1. 8 to the seventh power _____
2. 3 cubed _____
3. 6 to the fourth power _____
4. 4 to the first power _____
5. 7 squared _____

Evaluate Expressions

pp. 472–473

Complete the organizer to evaluate the expression with the values given for x and y .



Helping You Remember

A classmate states that $3^2 = 6$. How would you explain the correct solution? Use words, drawings, or models in your explanation.

9-2 Prime Factorization

What You'll Learn

Scan Lesson 9-2. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the term with its definition by drawing a line to connect the two.

monomial

when a composite number is expressed as the product of prime factors

composite number

to write a number as a product of its factors

factor tree

a whole number with exactly two unique factors, 1 and itself

factor

an expression that is a number, a variable, or a product of numbers and variables

prime number

a way to find the prime factorization of a number

prime factorization

a whole number that has more than two factors

Vocabulary Link *Composite* is a word that is used in everyday English. Find the definition of *composite* using a dictionary. Explain how the English definition can help you remember how a *composite number* is used in mathematics.

Lesson 9-2 (continued)

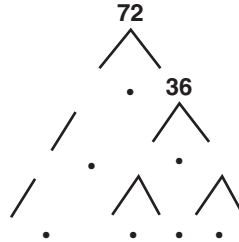
Main Idea

Write Prime Factorization

pp. 476–477

Details

Complete the factor tree.



The prime factorization of 72 is _____.

Factor Monomials

pp. 477–478

Fill in each blank with the monomial whose factors are shown.

1. $2^3 \cdot 3^3 \cdot x \cdot y \cdot y$ _____
2. $-1 \cdot 5^5 \cdot a \cdot a \cdot a$ _____
3. $3^3 \cdot 7 \cdot 11 \cdot s \cdot s \cdot s \cdot s \cdot s$ _____
4. $-1 \cdot x \cdot x \cdot x$ _____

Helping You Remember

Explain the relationship between the terms *base*, *exponent*, and *power*.

9-3 Multiplying and Dividing Monomials

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to the definition.
(Lessons 1-3 and 2-1)

_____ ▶

a number greater than zero

_____ ▶

a number less than zero

_____ ▶

the whole numbers and their opposites

_____ ▶

The order numbers are multiplied does not change the product.

_____ ▶

The order numbers are grouped does not change the sum.

_____ ▶

Finish each property.

Product of Powers Property

$$a \cdot a^n = a^m$$

Quotient of Powers Property

$$a^m \div a = a^n$$

Lesson 9-3 (continued)

Main Idea

Details

Multiply Monomials

pp. 481–482

Fill in the blanks to find each product.

1. $4^3 \cdot 4^2 = 4^{\square} + \square = 4^{\square}$

2. $2^5 \cdot 2^3 = 2^{\square} + \square = \square^{\square}$

3. $5^3 \cdot 5^4 = 5^{\square} + \square = \square^{\square}$

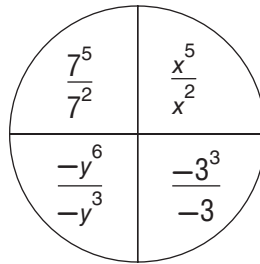
4. $2y^3 \cdot -3y^3 = \square^{\square} + \square = \square^{\square}$

5. $5x^4 \cdot 3x^3 = \square^{\square} + \square = \square^{\square}$

Divide Monomials

pp. 482–483

Cross out the one that does not belong. Then state the relationship among the three remaining parts of the circle.



The relationship is:

Helping You Remember

Restate the Product of Powers Property and the Quotient of Powers Property in your own words.

9-4 Negative Exponents

What You'll Learn

Skim Lesson 9-4. Predict two things you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definitions next to each term.
 (Lessons 1-1, 1-2, 1-3 and 9-1)

deductive reasoning ▶ _____

exponent ▶ _____

power ▶ _____

base ▶ _____

evaluate ▶ _____

algebraic expression ▶ _____

Lesson 9-4 (continued)

Main Idea

Details

Negative Exponents

pp. 486–487

Fill in each blank to prove $y^{-3} = \frac{1}{y^3}$.

Start with $\frac{y^4}{y^7}$.

$\frac{y^4}{y^7} \longrightarrow$

Using the _____,
the quotient is $\frac{\square}{\square} = \frac{\square}{\square}$.

$\frac{y^4}{y^7} \longrightarrow$

By _____, the quotient is
 $\frac{y \cdot y \cdot y \cdot y}{y \cdot y \cdot y \cdot y \cdot y \cdot y} = \frac{\square}{\square}$.

Because $\frac{y^4}{y^7}$ is equal to both $\frac{\square}{\square}$ and $\frac{\square}{\square}$, $\square = \square$.

Evaluate Expressions

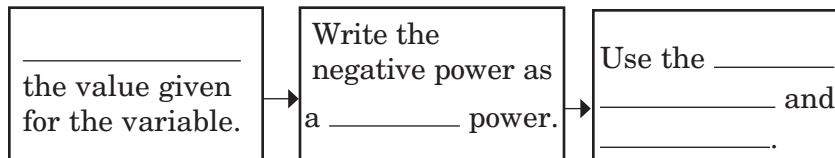
p. 488

Fill in the diagram to complete the steps to evaluate an expression with negative exponents. Use the terms *order of operations*, *positive*, *replace*, and *simplify*.

Step 1

Step 2

Step 3



Helping You Remember

Explain how negative exponents can be written as positive exponents.

9-5 Scientific Notation

What You'll Learn

Scan the text in Lesson 9-5. Write two facts you learned about scientific notation as you scanned the text.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the following terms with the correct examples by drawing a line to connect the two.

standard form

0.000050

5.0×10^5

scientific notation

2.8×10^3

3,700

8,900,000,000

Vocabulary Link *Standard* is a word that is used in everyday English. Find the definition of *standard* using a dictionary. Explain how the English definition can help you remember how *standard form* is used in mathematics.

Lesson 9-5 (continued)

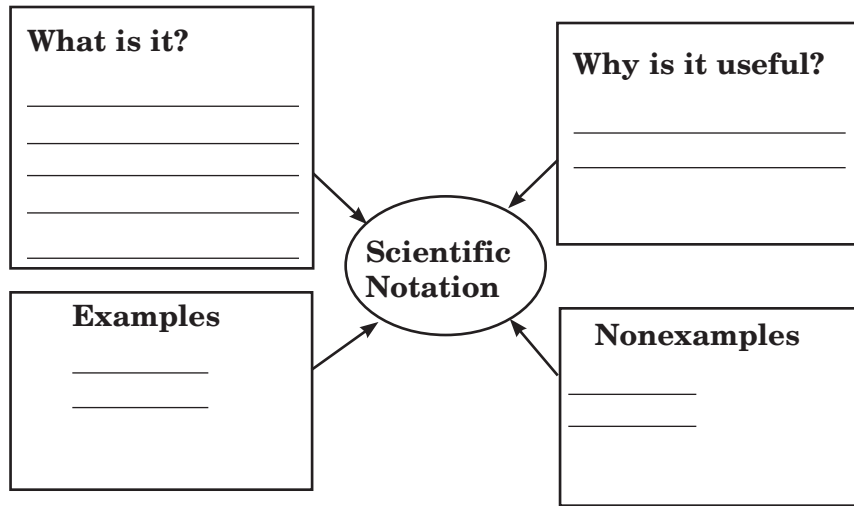
Main Idea

Scientific Notation

pp. 493–494

Details

Complete the organizer about *scientific notation*.



Compare and Order Numbers

p. 495

Write the numbers in order from greatest to least.

1. 4.05×10^5 , 4.2×10^5 , 3.0×10^5 , 1.3×10^5

2. 2.4×10^{-3} , 2.0×10^{-2} , 3.1×10^3 , 2.9×10^{-2}

Helping You Remember

Explain how to express a number greater than 1, a number less than 1, and then the number 1 in scientific notation.

9-6 Powers of Monomials

What You'll Learn

Skim the lesson. Write two things you already know about powers of monomials.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lessons 9-1 and 9-2*)

monomial ► an expression that is a number, a _____, or a _____ of numbers and or variables

power ► a _____ that is expressed using an _____

Vocabulary Link Write a *power* that has a *base* of 7 and an *exponent* of 4. Then write x to the fifth *power*. Write y *squared*. Write a monomial that is the product of the number 2 and k cubed.

Finish for each property.

Power of a _____ Property

$$(a^m)^n = a^{m \cdot n}$$

Power of a _____ Property

$$(ab)^m = a^m \cdot b^m$$

Lesson 9-6 *(continued)*

Main Idea

Details

Power of a Power

p. 499

Fill in the blanks with each product.

1. $(5^3)^2 = 5 \square \square = 5 \square$

2. $(x^5)^4 = x \square \square = x \square$

3. $(6^2)^{-2} = 6 \square \square = 6 \square$ or $\frac{\square}{\square}$

4. $(y^{-3})^{-4} = y \square \square = y \square$

Power of a Product

pp. 500–501

Compare the two properties of powers by filling out the chart.

	Power of Powers	Power of a Product
Why?		
How?		
Example		

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Compare and contrast the Quotient of Powers

Property and the Product of Powers Property.

9-7 Linear and Nonlinear Function

What You'll Learn

Skim the Examples for Lesson 9-7. Predict two things you think you will learn about linear and nonlinear function.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term.
(Lesson 1-5)

function ▶

function rule ▶

function table ▶

New Vocabulary Fill in each blank with the correct term or phrase.

nonlinear functions ▶

functions that _____ have constant _____,
therefore their graphs are *not* _____

Lesson 9-7 (continued)

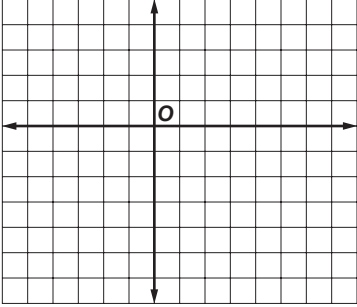
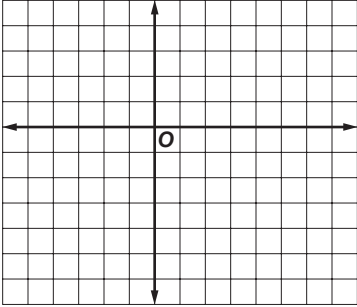
Main Idea

Details

Graphs of Nonlinear Functions

p. 504

Model a *linear* and *nonlinear* function on the coordinate planes. On the lines below, write a real-life example of each kind of function.

Linear Function	Nonlinear Function
	

Equations and Tables

pp. 505–506

Complete the organizer to summarize three ways to determine if a function is *linear* or *nonlinear*.

Is the graph a straight line?	Yes <input style="width: 100%;" type="text"/> No <input style="width: 100%;" type="text"/>
Can the equation of the line be written in the form $y = mx + b$?	Yes <input style="width: 100%;" type="text"/> No <input style="width: 100%;" type="text"/>
In a function table, are the changes in x and y constant?	Yes <input style="width: 100%;" type="text"/> No <input style="width: 100%;" type="text"/>

9-8 Quadratic Functions

What You'll Learn

Scan Lesson 9-8. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

parabola ▶

quadratic function ▶

Vocabulary Link A *parabola* is the shape that is seen in everyday life. Give an example of something that has a parabola shape in real life.

Lesson 9-8 (continued)

Main Idea

Graph Quadratic Function
pp. 510–511

Complete the organizer by filling in the blanks. Then complete the example.

Graph a Quadratic Function

Step 1:
Make a _____.

↓

Step 2:
_____ the ordered pairs.

↓

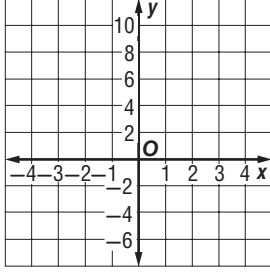
Step 3:
_____ the points
with a curved _____.

Graph: $y = 2x^2 + 3$

Step 1:

x	$y = 2x^2 + 3$	y

Step 2 and Step 3:



Use Quadratic Function
p. 511

Fill in the blanks by using the information below.

A ball is thrown into the sky. The equation that gives the ball's height in meters h as a function of time t is $h = -4.9t^2 + 12t + 3$.

1. What is the height of the ball after $t = 1$ second?

2. How high is the ball after 2 seconds? _____
3. What can you say about the ball's path between 1 and 2 seconds?

_____.

9-9 Cubic and Exponential Functions

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lesson 9-8*)

quadratic function ▶ a function that can be written in the form _____, where $a \neq 0$

parabola ▶ the graph of a _____ function graph

New Vocabulary Match the term with the correct form by drawing a line to connect the two.

cubic function $y = a^x + c$, where $a \neq 0$, $a \neq 1$

exponential function $y = ax^3 + bx^2 + cx + d$, where $a \neq 0$

Vocabulary Link *Exponential* is a word that is used in everyday English. Find the definition of *exponential* using a dictionary. Explain how the English definition can help you remember the shape of the graph of an *exponential function* in mathematics.

Lesson 9-9 (continued)

Main Idea

Cubic Functions
pp. 516–517

Details

Fill in the organizer for *cubic functions* are given.

<p>What is a cubic function?</p>	<p>Sketch the shape of a graph of a cubic function.</p>
<p>Cubic Functions</p>	
<p>Examples of Cubic Functions</p>	<p>Nonexamples of Cubic Functions</p>

Exponential Functions
pp. 517–518

Fill in each blank with the value of *y*.

1. $y = 2^x - 1$, when $x = 3$: (3, _____)
2. $y = 4^x + 2$, when $x = -1$: (-1, _____)
3. $y = 2^x - 3$, when $x = 2$: (2, _____)
4. $y = 5^x$, when $x = -2$: (-2, _____)

Helping You Remember

You have learned to graph quadratic and cubic functions. Make a list of the steps you use to graph the two functions.

CHAPTER
9

Powers and Nonlinear Functions

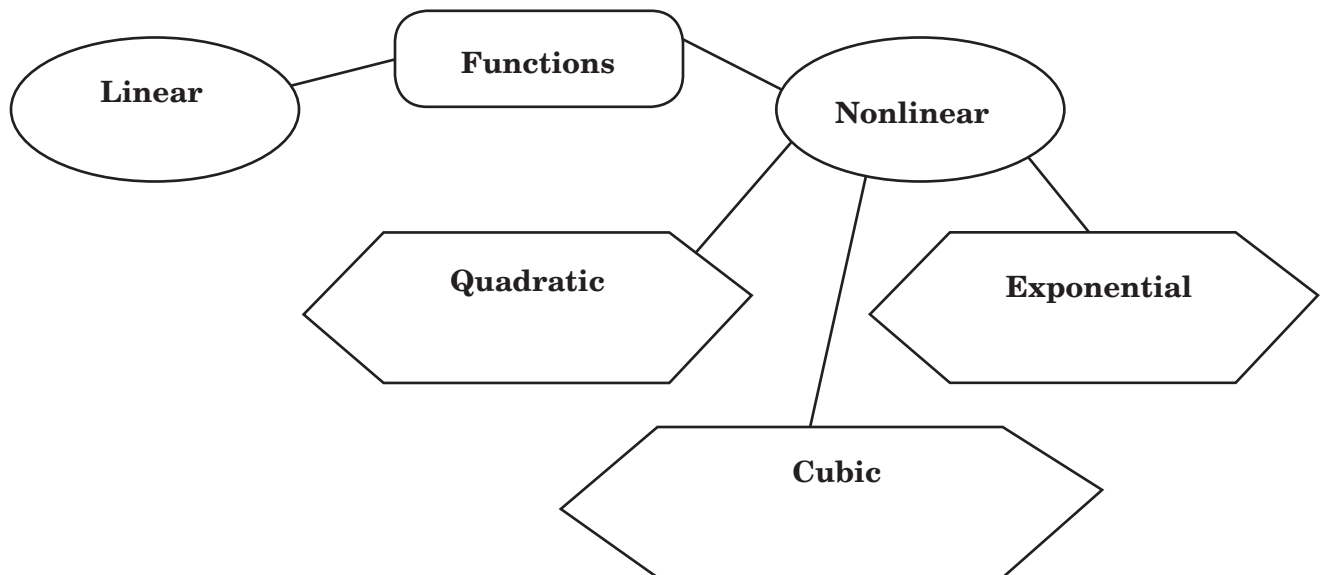
Tie It Together

Complete the graphic organizer by writing an equivalent form of the exponential expression.

_____ $\rightarrow x^a \leftarrow$ _____

$x^m \cdot x^n$	
$\frac{x^m}{x^n}$	
$(x^m)^n$	
$(xy)^m$	
x^{-m}	
x^0 , when $\neq 0$	

Complete the graphic organizer with types of functions and their general equations.




 CHAPTER
9

Powers and Nonlinear Functions

Before the Test

Review the ideas you listed in the table at the beginning of the chapter. Cross out any incorrect information in the first column. Then complete the table by filling in the third column.

K What I know...	W What I want to find out...	L What I learned...

Math Online Visit *glencoe.com* to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 9.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 9 Study Guide and Review in the textbook.
- I took the Chapter 9 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Complete reading assignments before class. Write down or circle any questions you may have about what was in the text.


 CHAPTER
10

Real Numbers and Right Triangles

Before You Read

Before you read the chapter, think about what you know about real numbers and right triangles. List three things you already know about them in the first column. Then list three things you would like to learn about them in the second column.

K What I know...	W What I want to find out...


 FOLDABLES[®] Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- Before going to class, look over your notes from the previous class, especially if the day's topic builds from the last one.
- When you take notes, write down the math problem and each step in the solution using math symbols.

Next to each step, write down, in your own words, exactly what you are doing.

**CHAPTER
10****Real Numbers and Right Triangles****Key Points**

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on triangles, one fact might be that a vertex is a point where line segments intersect. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
10-1 Squares and Square Roots	
10-2 The Real Number System	
10-3 Triangles	
10-4 The Pythagorean Theorem	
10-5 The Distance Formula	
10-6 Special Right Triangles	

10-1 Squares and Square Roots

What You'll Learn

Scan the text in Lesson 10-1. Write two facts you learned about squares and square roots as you scanned the text.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match the term with its definition by drawing a line to connect the two.

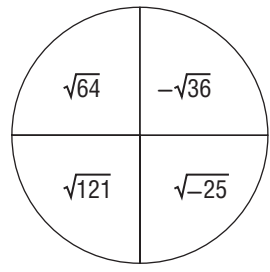
- | | |
|-----------------------|---|
| <i>perfect square</i> | one of a number's two equal factors |
| <i>square root</i> | indicates a positive square root |
| <i>radical sign</i> | a rational number whose square root is a whole number |

Main Idea

Find Square Roots
p. 537

Details

Cross out the square root in the concept circle that does not belong. Then describe the relationship of the remaining three parts.



The relationship is _____
_____.

Lesson 10-1

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Lesson 10-1 (continued)

Main Idea

Details

Estimate Square Roots
pp. 538–539

Complete the organizer by following the steps to estimate a square root. Then complete the example.

Estimate a square root.

Step 1: Find the perfect square just below the number.

Step 2: Find the perfect square just above the number.

Step 3: Decide which is closest.

Estimate $-\sqrt{24}$ to the nearest integer.

Step 1:

Step 2:

Step 3:

Helping You Remember

Tell whether each number has a square root and explain why or why not. Then state if it is a perfect square and explain.

	Real Square Root?	Perfect Square?
26		
-81		
256		
2500		
-5		

10-2 The Real Number System

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about the real number system.

1. _____

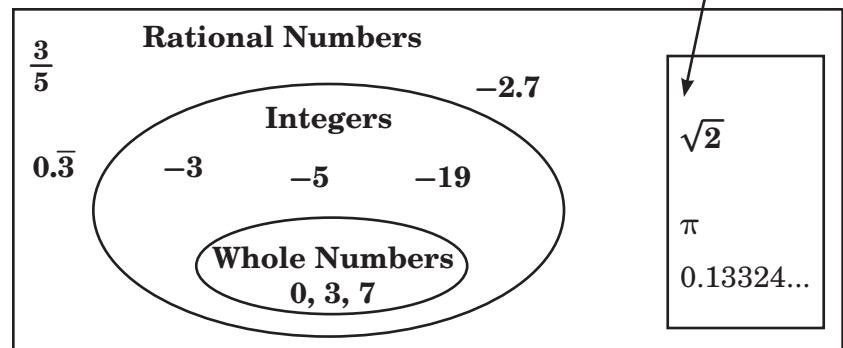
2. _____

Active Vocabulary

irrational numbers ▶

real numbers ▶

New Vocabulary Label the diagram with the correct term.



Vocabulary Link *Irrational* is a word that is used in everyday English. Find the definition of *irrational* using a dictionary. Explain how the English definition can help you remember how *irrational* is used in mathematics.

Lesson 10-2

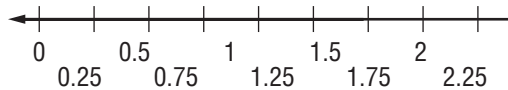
Lesson 10-2 (continued)

Main Idea

Identify and Compare Real Numbers
pp. 543–544

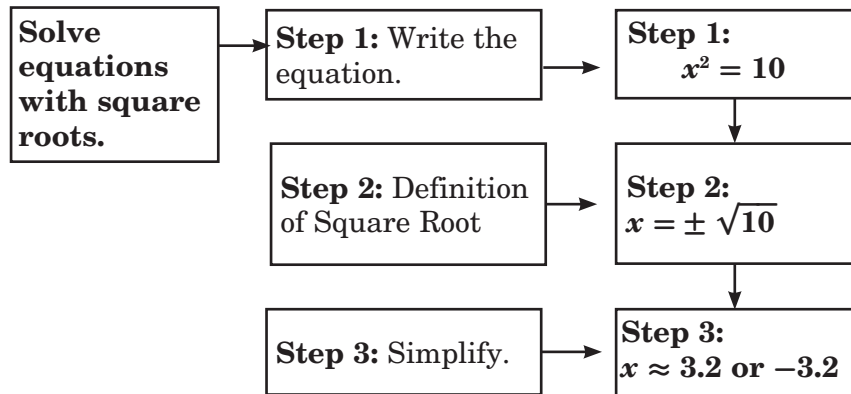
Details

Model and explain how to use a number line to list $\frac{7}{8}$, $0.\overline{67}$, $\sqrt{3}$, and $\frac{3}{4}$ from least to greatest. Write an equality and explanation on the lines below.



Solve Equations
p. 545

Complete the organizer by following the steps to solve the equation $x^2 = 10$ using the definition of a square root.



10-3 Triangles

What You'll Learn

Skim Lesson 10-3. Predict two things that you expect to learn based on the headings and the Key Concept boxes.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

congruent ▶

triangle ▶

vertex ▶

line segment ▶

Main Idea

Find Angle Measures
pp. 550–551

Details

Fill in the diagram to determine the angle measures of $\triangle KLM$ with a ratio of 1:3:1.

Step 1

Use x to represent the measure of the _____ and _____.
_____.

Step 2

Use _____ to represent the measure of the _____.
_____.

Step 3

Write the equation, _____.
_____.
Solve for x .

Because $x =$ _____, the measure of the angles are _____.

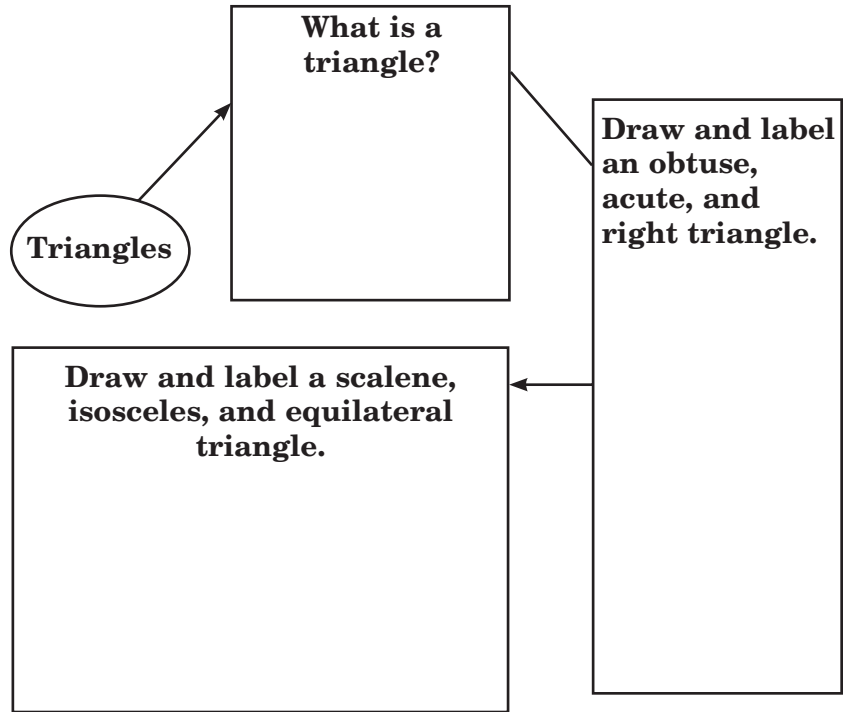
Lesson 10-3 (continued)

Main Idea

Details

Classify Triangles
pp. 551–552

Summarize information about triangles in the graphic organizer. Sample answers are given.



Helping You Remember

Describe an obtuse, scalene triangle.

Describe an equilateral triangle. _____

10-4 The Pythagorean Theorem

What You'll Learn

Skim the Examples in Lesson 10-4. Predict two things you think you will learn about the Pythagorean Theorem.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

hypotenuse ▶

Pythagorean Theorem ▶

legs ▶

solving a right triangle ▶

*converse of the
Pythagorean Theorem* ▶

Lesson 10-4 (continued)

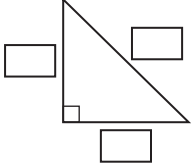
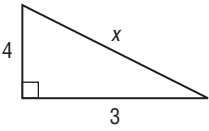
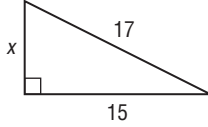
Main Idea

Details

Use the Pythagorean Theorem

pp. 558–559

Fill in the organizer about using the *Pythagorean Theorem*.

<p>Definition</p>	<p>Symbols</p> <p>_____</p> <p>Label a, b, c.</p> 
<p>Pythagorean Theorem</p>	
<p>Find the length of the hypotenuse.</p> 	<p>Find the missing length.</p> 

Use the Converse of the Pythagorean Theorem

p. 600

Fill in the blanks and determine whether each triangle is a right triangle.

1. 12 in., 35 in., 37 in.

$$a^2 + b^2 = c^2$$

$$\square + \square \stackrel{?}{=} \square$$

$$\square + \square \stackrel{?}{=} \square$$

$$\square = \square$$

Is it a right triangle?

2. 7 cm, 23 cm, 24 cm

$$a^2 + b^2 = c^2$$

$$\square + \square \stackrel{?}{=} \square$$

$$\square + \square \stackrel{?}{=} \square$$

$$\square \neq \square$$

Is it a right triangle?

10-5 The Distance Formula

What You'll Learn

Skim the lesson. Predict two things that you expect to learn based on the headings and the Key Concept boxes.

1. _____

2. _____

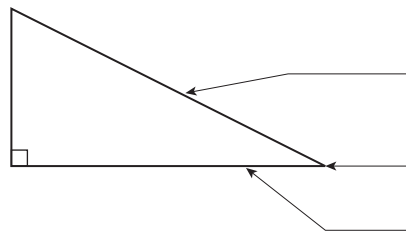
Active Vocabulary

Review Vocabulary Label the diagram with the correct term. (Lessons 10-3 and 10-4)

hypotenuse ▶

leg ▶

vertex ▶



New Vocabulary Fill in each blank with the correct term or phrase.

distance formula ▶

The distance d between _____ with coordinates _____ and _____ is given by the formula

$$d = \underline{\hspace{2cm}}$$

Lesson 10-5 (continued)

Main Idea

Details

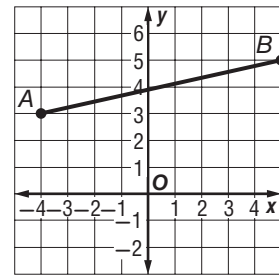
Find the Distance Between Points

pp. 565–566

Model the solution to find the distance between the points on the coordinate plane. Use the lines to show your calculations. Round to the nearest tenth if necessary.

$(x_1, y_1) = (-4, 3); (x_2, y_2) = (5, 5)$

AB



Apply the Distance Formula

p. 567

Fill in each blank to describe the steps to classify a triangle by its sides on a coordinate plane and then find its perimeter.

Step 1

Use the distance formula,
to find the _____
of each side.

Step 2

_____ the
triangle as scalene,
equilateral, or
isosceles using the
_____.

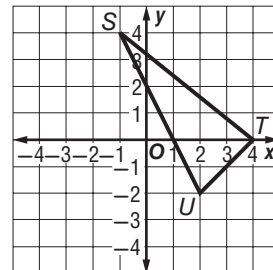
Step 3

Find the _____
of the triangle's
_____ to find the
_____.

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Describe how you would find the perimeter of $\triangle STU$. List any formulas that must be used.



10-6 Special Right Triangles

What You'll Learn

Scan Lesson 10-6. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to each definition. (Lessons 6-7, 10-1, 10-3, and 10-4)

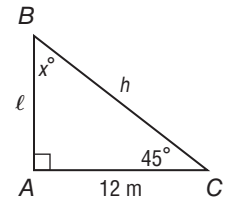
- _____ ► formed by three line segments that intersect only at their endpoints
- _____ ► the point where two line segments that form a side of a triangle meet
- _____ ► figures that have the same shape but not necessarily the same size

Main Idea

Find Measures in 45–45–90 Triangles
pp. 571–572

Details

Use $\triangle ABC$ to fill in each blank.



1. The measure of $\angle B$ is _____ because _____

2. The length of the hypotenuse, h , is _____ because

3. The length of side, l , is 12 meters because _____

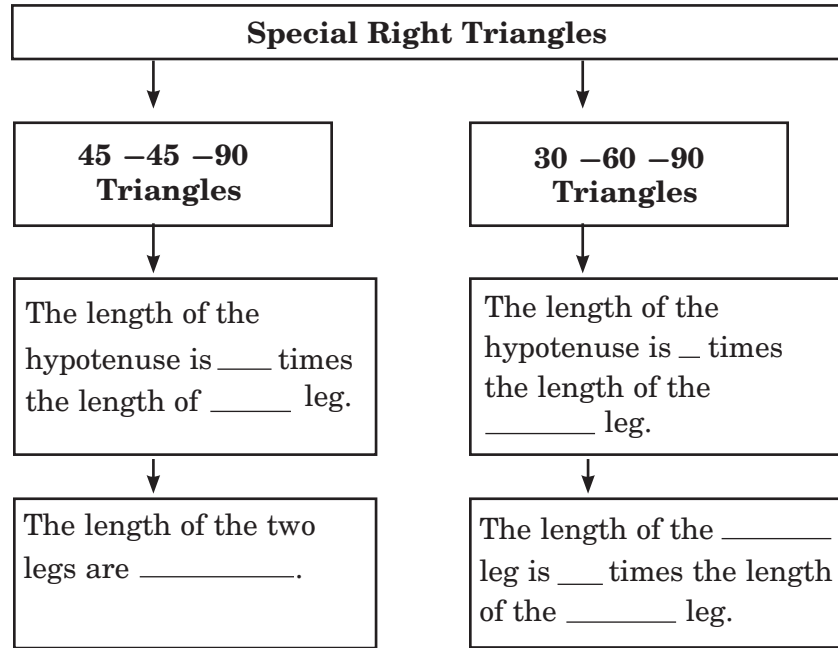
Lesson 10-6 (continued)

Main Idea

**Find Measures in
30 –60 –90 Triangles**
pp. 572–573

Details

Compare 45 –45 90 and 30 60 90 triangles by filling in each blank of the organizer.



Helping You Remember

Describe the properties of a 30° 60°–90° triangle. Include the ways that students sometimes mismeasure the side lengths or angles.

CHAPTER
10

Real Numbers and Right Triangles

Tie It Together

Sketch an example of each type of triangle if possible. If the sketch is not possible mark an X in the box.

Angle Measure/ Side Length	Acute	Obtuse	Right
Equilateral			
Isosceles			
Scalene			


**CHAPTER
10**

Real Numbers and Right Triangles

Before the Test

Review the ideas you listed in the table at the beginning of the chapter. Cross out any incorrect information in the first column. Then complete the table by filling in the third column.

K What I know...	W What I want to find out...	L What I learned...

Math Online Visit *glencoe.com* to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 10.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 10 Study Guide and Review in the textbook.
- I took the Chapter 10 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Use abbreviations while note-taking to use less time and room. Write neatly and place a question mark by any information that you do not understand.


 CHAPTER
11

Distance and Angle

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Distance and Angle
	<ul style="list-style-type: none"> • Parallel lines intersect to form right angles.
	<ul style="list-style-type: none"> • A figure that rotates about a fixed point does not change shape or size.
	<ul style="list-style-type: none"> • A quadrilateral is a polygon that has four sides.
	<ul style="list-style-type: none"> • An example of a polygon is a circle.
	<ul style="list-style-type: none"> • The formula to find the circumference of a circle is $C = 2\pi r$.


FOLDABLES Study Organizer

Construct the Foldable as directed at the beginning of this chapter.


Note Taking Tips

- **It is helpful to read through your notes before beginning your homework.**
Look over any page referenced material.
- **As soon as possible, go over your notes.**
Clarify any ideas that were not complete.


 CHAPTER
11

Distance and Angle

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on quadrilaterals, one fact might be that the sum of the measures of the angles of a quadrilateral is 360° . After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
11-1 Angle and Line Relationships	
11-2 Congruent Triangles	
11-3 Rotations	
11-4 Quadrilaterals	
11-5 Polygons	
11-6 Area of Parallelograms, Triangles, and Trapezoids	
11-7 Circles and Circumference	
11-8 Area of Circles	
11-9 Area of Composite Figures	

11-1 Angle and Line Relationships

What You'll Learn

Skim Lesson 11-1. Predict two things that you expect to learn based on the headings and the Key Concept boxes.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

vertical angles ▶

adjacent angles ▶

complementary angles ▶

supplementary angles ▶

perpendicular lines ▶

parallel lines ▶

transversal ▶

alternative interior angles ▶

alternative exterior angles ▶

corresponding angles ▶

Lesson 11-1 (continued)

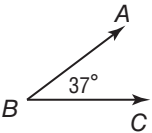
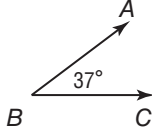
Main Idea

Details

Angle Relationships

pp. 589–590

Complete the model so that $\angle ABC$ is complementary to $\angle ABD$ and $\angle ABC$ is supplementary to $\angle ABD$. Label each angle measure.

Complementary Angles	Supplementary Angles
	

Parallel Lines

pp. 590–591

Draw a transversal t which intersects with two parallel lines a and b . Label all interior angles, exterior angles, alternative interior and exterior angles, and corresponding angles.

Helping You Remember

Look up the meaning of the prefix *trans-* in the dictionary. Write down four words that have *trans-* as a prefix. How can the meaning of the prefix help you remember the meaning of transversal?

11-2 Congruent Triangles

What You'll Learn

Scan Lesson 11-2. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the correct term next to each definition. (*Lesson 10-3*)

_____ ► formed by three line segments that intersect only at their endpoints

_____ ► the point where two line segments that form a side of a triangle meet

_____ ► the part of a line containing two endpoints and all of the points between them

New Vocabulary Fill in each blank with the correct term or phrase.

congruent ► _____ that have the same _____ and _____ are congruent.

corresponding parts ► The _____ of _____ triangles that _____ or correspond are called corresponding parts.

Lesson 11-2 (continued)

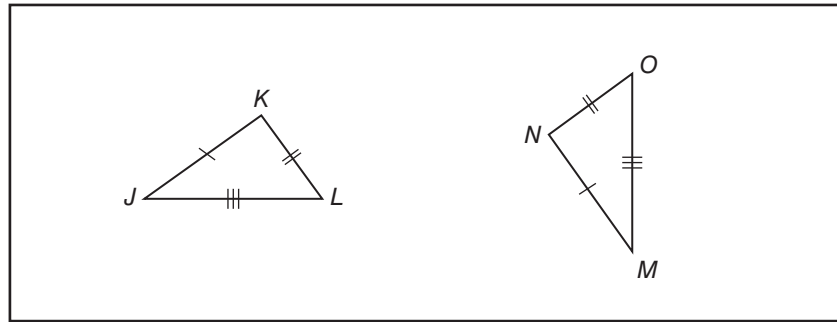
Main Idea

Details

Corresponding Parts

pp. 598–600

Fill in each blank to complete the congruence statements for the congruent triangles below.



1. $\triangle JKL \cong \triangle \square$
2. $\triangle \square \cong \triangle NOM$
3. $\triangle JLK \cong \triangle \square$
4. $\triangle KJL \cong \triangle \square$
5. $\triangle \square \cong \triangle OMN$
6. $\triangle LKJ \cong \triangle \square$

Identify Congruent Triangles

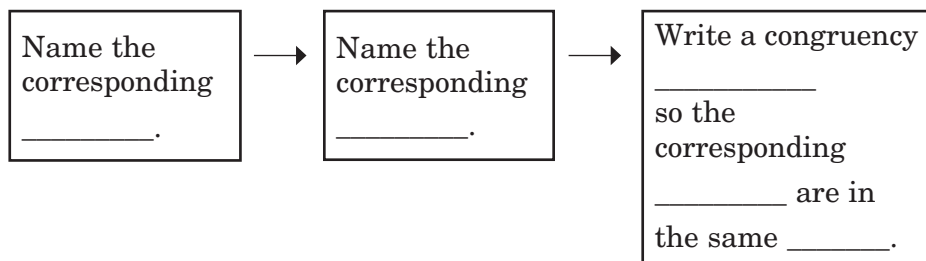
pp. 600–601

Fill in the diagram to complete the steps to determine congruent triangles. Use the terms *statement*, *order*, *angles*, *vertices*, and *sides*.

Step 1

Step 2

Step 3



Helping You Remember

Corresponding is a word used in everyday English as well as in mathematics. Write the definition of *corresponding*. Explain how the English definition can help you remember how *corresponding* is used in mathematics.

11-3 Rotations

What You'll Learn

Skim the Examples for Lesson 11-3. Predict two things that you will learn about rotations.

1. _____

2. _____

Active Vocabulary

New Vocabulary Match each definition with the correct term by drawing a line to connect the two.

rotation the fixed point that a figure is rotated about

center of rotation when a figure can be rotated less than 360° about its center so that its image matches the original figure

rotational symmetry a transformation where a figure is turned about a fixed point

Vocabulary Link *Rotational* and *symmetry* are two words used in everyday English. Find the definitions of *rotational* and *symmetry* using a dictionary. List three examples of something that has rotational symmetry.

Lesson 11-3 (continued)

Main Idea

Rotations
pp. 605–607

Details

Draw the letter after a 90° counterclockwise rotation around the point.



Rotational Symmetry
p. 607

Fill in the organizer about rotational symmetry.

<p>How do you decide if a figure has rotational symmetry?</p>	<p>How do you find the angle of rotation?</p>
<p>Rotational Symmetry</p>	
<p>Draw a figure with a 90° angle of rotation.</p>	<p>Draw a figure with no rotational symmetry.</p>

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

A classmate was absent the day that rotation and rotational symmetry were taught. Provide an explanation of the two concepts.

11-4 Quadrilaterals

What You'll Learn

Skim the lesson. Write two things you already know about quadrilaterals.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term.
 (*Lesson 10-3*)

vertex ►

segment ►

New Vocabulary Fill in each blank with the correct term or phrase.

quadrilateral ►

A quadrilateral is a _____ figure with _____ sides and _____ angles. The segments that form a quadrilateral _____ only at their _____.

Vocabulary Link *Quad-* is a prefix used in everyday English as well as in mathematics. Write the meaning of the prefix *quad-*. Write two examples of words used in everyday life that have *quad-* as a prefix and their meanings.

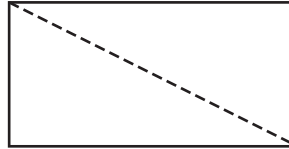
Lesson 11-4 (continued)

Main Idea

Find Angle Measures
pp. 612–613

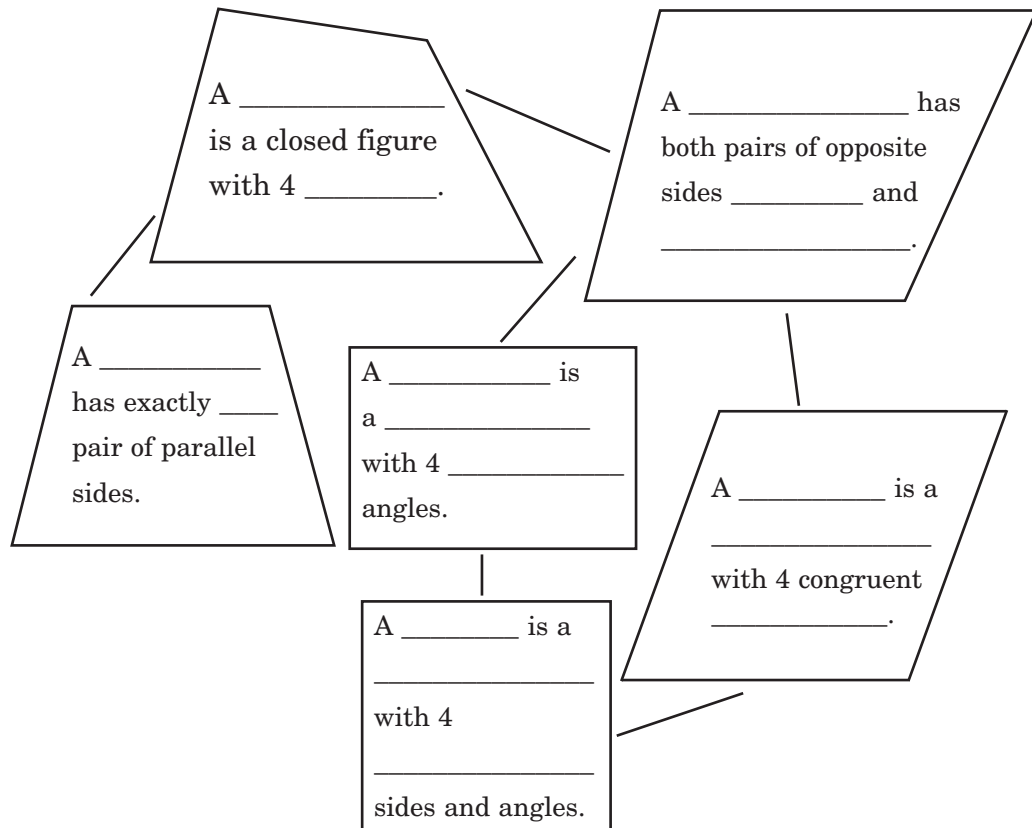
Details

Explain how the model proves that a quadrilateral has angles whose measures have a sum of 360° .



Classify Quadrilaterals
p. 613

Fill in the organizer to classify and describe each figure. Then draw lines to connect the figures and show their relationships.



11-5 Polygons

What You'll Learn

Scan the text in Lesson 11-5. Write two facts you learned about polygons.

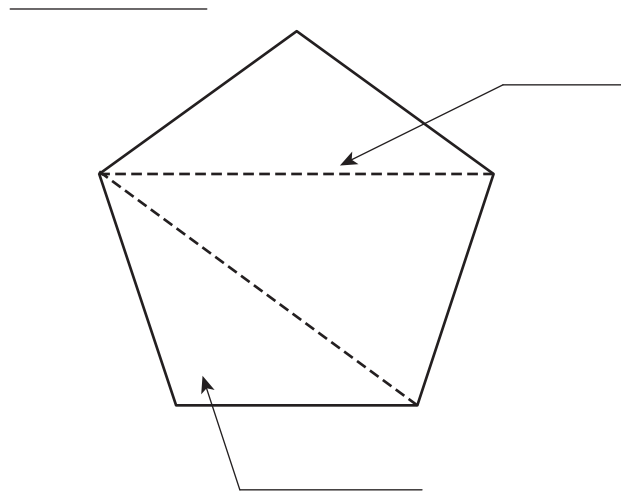
1. _____

2. _____

Active Vocabulary

New Vocabulary Label the diagram with the correct terms.

- diagonal* ▶
- interior angles* ▶
- regular polygon* ▶



Vocabulary Link *Tessellation* can be illustrated by real-world examples. Look around the room. Give two examples of real-world tessellations.

Lesson 11-5 (continued)

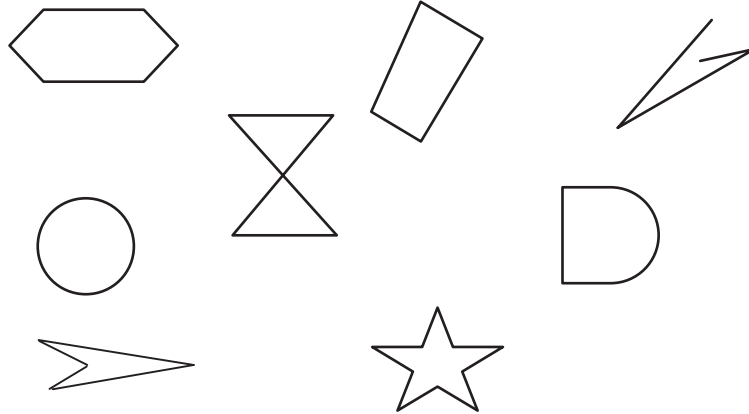
Main Idea

Details

Classify Polygons

p. 617

Circle the figures that are *not* polygons. If a figure is not a polygon, write the reason inside or beside the figure.



Find Angle Measures of a Polygon

pp. 618–619

Fill in each blank with the number of interior angles for each figure. Then write the sum of the measures of the interior angles.

1. heptagon

A heptagon is a -sided figure.
So, $(n - 2)180 = (\underline{\quad} - 2)180$
 $n = \underline{\quad}$. The sum is .

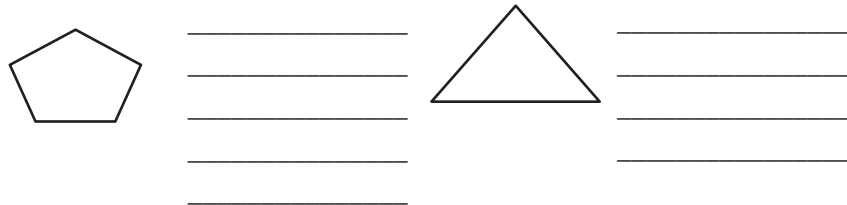
2. rhombus

A rhombus is a 4-sided figure.
So, $(n - 2)180 = (\underline{\quad} - 2)180$
 $n = \underline{\quad}$. The sum is .

Tessellations

p. 619

Cross out the figure that can not be used to make a tessellation. Explain.



11-6 Area: Parallelograms, Triangles, and Trapezoids

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

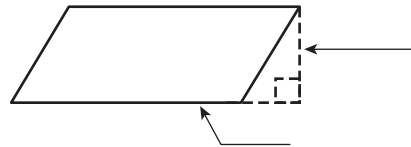
1. _____

2. _____

Active Vocabulary

New Vocabulary Label the diagram with the correct terms.

- base* ▶
- altitude* ▶



Vocabulary Link *Altitude* is a word that is used in everyday English. Find the definition of *altitude* using a dictionary. Explain how the English definition can help you remember how *altitude* is used in mathematics.

Lesson 11-6 (continued)

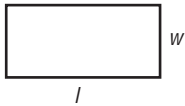
Main Idea

Details

Area of Parallelograms

p. 624

Compare the area of a rectangle and the area of a parallelogram.

Area		
	Rectangle	Parallelogram
Formula	$A = lw$	$A = \underline{\hspace{2cm}}$
Words	Area is length times width.	Area is $\underline{\hspace{2cm}}$ times $\underline{\hspace{2cm}}$.
Model		
Examples	A rectangle with length 6 cm and width 5 cm has an area of $\underline{\hspace{2cm}}$.	A parallelogram with base 10 mm and height 9 mm has an area of $\underline{\hspace{2cm}}$.

Area of Triangles and Trapezoids

pp. 625–626

Complete to summarize the area of a triangle and a trapezoid.

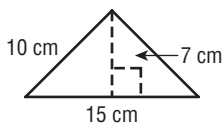
A parallelogram divided in half by a diagonal results in two congruent triangles. The area of a parallelogram is the sum of the area of the two $\underline{\hspace{2cm}}$. Because the area of a parallelogram is $\underline{\hspace{2cm}}$ times $\underline{\hspace{2cm}}$, the area of a triangle is half the $\underline{\hspace{2cm}}$ times $\underline{\hspace{2cm}}$ or $\underline{\hspace{2cm}}$.

A trapezoid with base a and base b can be divided in half by a $\underline{\hspace{2cm}}$ resulting in two noncongruent triangles. The sum of the area of those two triangles is $\frac{1}{2}ah + \frac{1}{2}bh$ which is equal to $\underline{\hspace{2cm}}(\underline{\hspace{1cm}} + \underline{\hspace{1cm}})$.

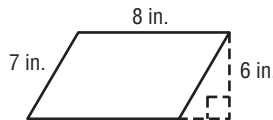
Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

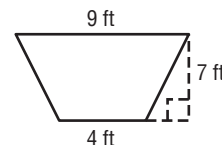
Match the formula with the correct figure by drawing a line to connect them. Then find its area.



$$A = \frac{1}{2}h(a + b)$$



$$A = \frac{1}{2}(bh)$$



$$A = bh$$

11-7 Circles and Circumference

What You'll Learn

Skim Lesson 11-7. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

New Vocabulary Fill in each blank with the correct term or phrase.

circle ▶ the set of all _____ in a plane that is the same _____ from a given _____ in the plane

center ▶ the given _____ in the middle of a _____

radius ▶ the _____ from the _____ to any point on the circle

diameter ▶ the _____ across the circle through the _____

chord ▶ the _____ between any two _____ on the circle

circumference ▶ the distance _____ the circle

π (*pi*) ▶ the _____ of the _____ to the _____ of a circle

Lesson 11-7 (continued)

Main Idea

Details

Circumference of Circles
pp. 631–632

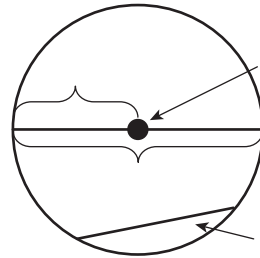
Label each part of the circle. Then find its circumference with the given diameter or radius. Round to the nearest tenth.

- $r = 15$ mm Use $C = 2\pi r$.

$C = 2\pi(\underline{\hspace{1cm}})$

$C = \underline{\hspace{1cm}}\pi$

$C \approx \underline{\hspace{1cm}}$ mm



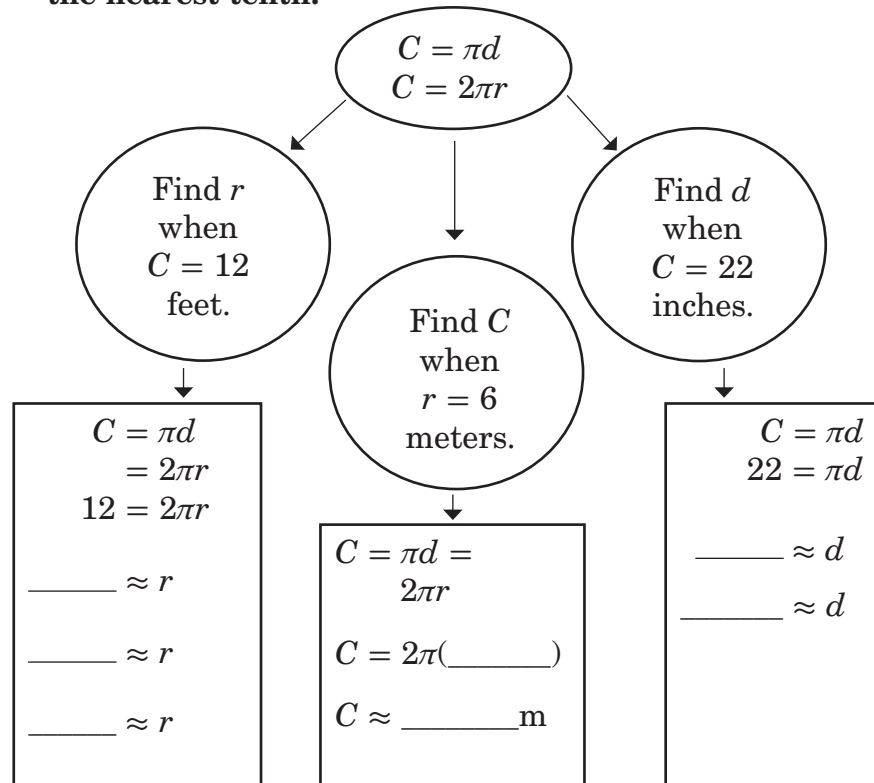
- $d = 8$ yd Use $C = \pi d$.

$C = \pi(\underline{\hspace{1cm}})$

$C \approx \underline{\hspace{1cm}}$ yd

Use Circumference to Solve Problems
p. 632

Fill in the blanks to complete the organizer. Round to the nearest tenth.



11-8 Area of Circles

What You'll Learn

Scan Lesson 11-8. List two headings you would use to make an outline of this lesson.

1. _____

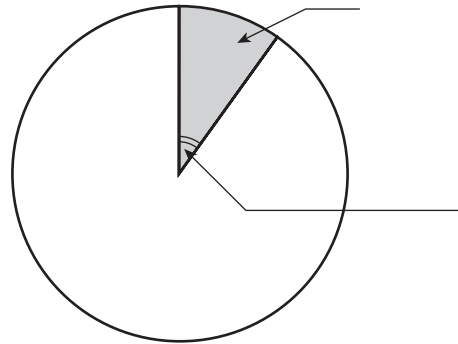
2. _____

Active Vocabulary

New Vocabulary Label the diagram with the correct term or phrase.

sector ▶

central angle ▶



Vocabulary Link *Sector* is a word that is used in everyday English. Find the definition of *sector* using a dictionary. Explain how the English definition can help you remember how *sector* is used in mathematics.

Lesson 11-8 (continued)

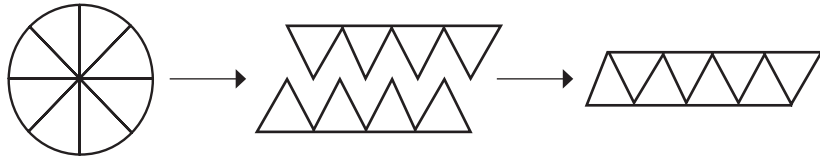
Main Idea

Details

Area of Circles

pp. 636–637

Fill in each blank to summarize the formula for the area of a circle.



Divide a circle into equal _____.

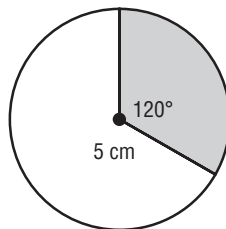
Fit the pieces together to make a _____.

1. The area of a parallelogram is _____.
2. The circumference of a circle is _____.
3. The base of the parallelogram is _____ the circumference of the circle.
So, $b = \frac{1}{2}C = \frac{1}{2}(\text{_____}) = \text{_____}$.
4. The height of the parallelogram is the _____ of the circle.
So, $h = \text{_____}$.
5. Substitute the values for b and h .
 $A = bh = \text{_____} = \text{_____}$

Area of Sectors

p. 638

Fill in each blank to find the area of a sector.



$$\begin{aligned}
 A &= \frac{N}{360}(\pi r^2) \\
 &= \frac{\boxed{}}{360}(\pi \boxed{}^2) \\
 &= \text{_____} \pi \\
 &= \text{_____} \pi \\
 &\approx \text{_____}
 \end{aligned}$$

Use the formula.

N is the number of degrees of the central angle.

Substitute for N and r .

Simplify.

11-9 Area of Composite Figures

What You'll Learn

Skim the Examples for Lesson 11-9. Predict two things that you will learn about the area of composite figures.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term.
(Lesson 11-7)

circle ▶

radius ▶

diameter ▶

chord ▶

circumference ▶

π (*pi*) ▶

New Vocabulary Fill in the blank with the correct term or phrase.

composite figure ▶ A composite figure is made up of _____.

Lesson 11-9 (continued)

Main Idea

Details

Area of Composite Figures

pp. 644–645

Fill in each blank to find the area of the composite figure.

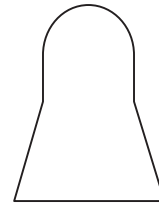
<p>Step 1: Divide the figure into _____ that help you find the area.</p>	<p>Step 2: Calculate the _____ of each _____.</p>	<p>Step 3: The _____ of the _____ of the _____ is the area of the _____ figure.</p>
---	--	--

Name the shapes that make up each composite figure. Then draw lines that show the shapes.

1.



2.



Helping You Remember

Find the area of each polygon and then the area of the composite figure.

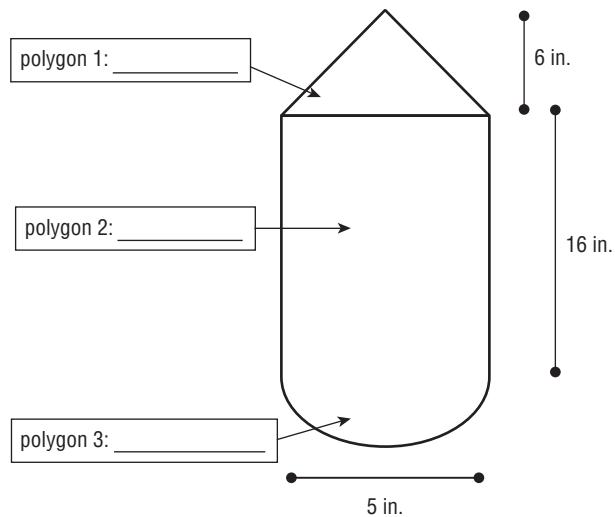
Polygon 1: _____

Polygon 2: _____

Polygon 3: _____

Composite Figure: _____

Find the area of each polygon and then the area of the composite figure.



CHAPTER
11

Distance and Angle

Tie It Together

Complete each graphic organizer with a term or formula from the chapter.

QUADRILATERALS

CIRCLES

Two-Dimensional Figures

AREA FORMULAS

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
11

Distance and Angle

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Distance and Angles	After You Read
<ul style="list-style-type: none"> • Parallel lines intersect to form right angles. 	
<ul style="list-style-type: none"> • A figure that rotates about a fixed point does not change shape or size. 	
<ul style="list-style-type: none"> • A quadrilateral is a polygon that has four sides. 	
<ul style="list-style-type: none"> • An example of a polygon is a circle. 	
<ul style="list-style-type: none"> • The formula to find the circumference of a circle is $C = 2\pi r$. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 11.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 11 Study Guide and Review in the textbook.
- I took the Chapter 11 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- Use the SQ3R method of reading: **S**urvey, **Q**uestion, **R**ead, **R**ecite, and **R**evise. Survey the text by previewing the headings, boldface words, and examples. Ask questions about what you survey, read with purpose, recite out loud the main points and concepts without looking at the text, and review your text notes or use the chapter review at the end of the chapter.


 CHAPTER
12

Surface Area and Volume

Before You Read

Before you read the chapter, think about what you know about surface area and volume. List three things you already know about them in the first column. Then list three things you would like to learn about them in the second column.

K What I know...	W What I want to find out...


FOLDABLES Study Organizer

Construct the Foldable as directed at the beginning of this chapter.



Note Taking Tips

- **Include pictures with your notes.**
Having diagrams that are labeled with specific parts of each figure will help you understand the formulas.
- **Remember to study your notes daily.**
Reviewing small amounts at a time will help you retain the information.

CHAPTER
12

Surface Area and Volume

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on three-dimensional figures, one fact might be that a face is a flat surface. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
12-1 Three-Dimensional Figures	
12-2 Volume of Prisms	
12-3 Volume of Cylinders	
12-4 Volume of Pyramids, Cones, and Spheres	
12-5 Surface Area of Prisms	
12-6 Surface Area of Cylinders	
12-7 Surface Area of Pyramids and Cones	
12-8 Similar Solids	

12-1 Three-Dimensional Figures

What You'll Learn

Skim Lesson 12-1. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____
2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

- plane* ▶ _____

- solid* ▶ _____
- polyhedron* ▶ _____
- edge* ▶ _____
- vertex* ▶ _____
- face* ▶ _____
- prism* ▶ _____
- base* ▶ _____
- pyramid* ▶ _____
- cylinder* ▶ _____

- cone* ▶ _____

- cross section* ▶ _____

Lesson 12-1

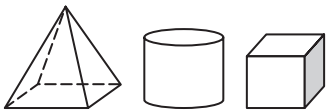
Lesson 12-1 (continued)

Main Idea

Identify Three-Dimensional Figures
pp. 664–665

Details

Complete the organizer about *three-dimensional* figures.

<p>What are they?</p>	<p>Draw a picture of a three-dimensional figure.</p>
<p>Three-Dimensional Figures</p>	
<p>Name some examples.</p>	<p>Identify these figures.</p> <div style="text-align: center;">  </div>

Cross Sections
p. 666

Fill in each blank to summarize cross sections.

1. If a cylinder is sliced vertically, the cross section that would result is a(n) _____.
2. When a triangular pyramid is sliced horizontally, the cross section that results is a(n) _____.
3. When a cone is sliced at an angle, the cross section that results is a(n) _____.
4. If a _____ is sliced vertically, the cross section that would result is a square.

Helping You Remember

The word *polyhedron* is composed of the prefix *poly-* and the root word *hedron*. Find the definitions of *poly-* and *hedron-* in a dictionary. Write their definitions.

12-2 Volume of Prisms

What You'll Learn

Scan Lesson 12-2. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match the term with its definition by drawing a line to connect the two. (*Lessons 4-1, 4-2, and 5-1*)

simplest form equation that shows a relationship between quantities

like terms terms that contain the same variable

simplifying the expressions an algebraic expression that has no like terms and no parentheses

formula combine like terms

New Vocabulary Fill in each blank with the correct word or phrase.

volume ► The measure of the _____ occupied by a three-dimensional _____.

Vocabulary Link *Volume* is a word that is used in everyday English. Find the definition of *volume* using a dictionary. Write two sentences of how the word *volume* is used in everyday life.

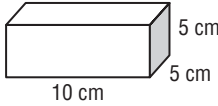
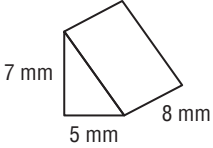
Lesson 12-2 (continued)

Main Idea

Details

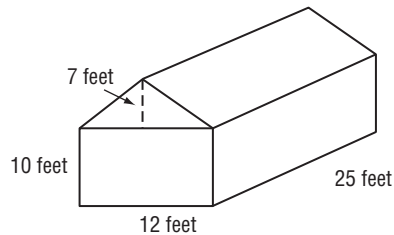
Volume of Prism
pp. 671–672

Compare finding the volume of a rectangular prism with a triangular prism.

	Rectangular Prism	Triangular Prism
Formula	$V =$	$V =$
Area of base	$B =$	$B =$
Sketch the prism and find its volume.		

Volume of Composite Figures
p. 673

Find the volume of the figure. Show your work.



Find the volume of the top. _____

Find the volume of the bottom. _____

Add the volumes. _____

12-3 Volume of Cylinders

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to each definition.
(Lessons 5-1 and 11-7)

- _____ ▶ the distance around a figure
- _____ ▶ an equation that shows a relationship between quantities
- _____ ▶ the surface enclosed by a figure
- _____ ▶ a set of all points in a plane that is the same distance from a given point called the center
- _____ ▶ the given point from which all points on the circle are the same distance
- _____ ▶ the distance from the center to any point on the circle
- _____ ▶ the distance across the circle through its center
- _____ ▶ the distance around a circle
- _____ ▶ the ratio of the circumference to the diameter of the circle

Lesson 12-3 (continued)

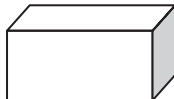
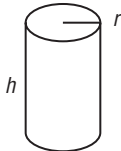
Main Idea

Details

Volume of Cylinders

pp. 677–678

Compare how to find the volume of the two figures by completing the chart.

Volume		
	Rectangular Prism	Cylinder
Formula	$V = Bh = lwh$	$V = Bh =$
Words	Volume is the area of the base times the height.	Volume is the _____ times the _____.
Model		sample model: 
Examples	A rectangular prism with length 5 in., a width 9 in., and a height of 10 in. has a volume of _____.	A cylinder with radius 7 mm and height 15 mm has a volume of _____.

Volumes of Composite Figures

p. 678

Fill in each blank to complete the steps to find the volume of a composite figure.

Step 1

_____ the figure into _____.

Step 2

Find the _____ of each _____ using the correct _____.

Step 3

Find the _____ of the _____ for the volume of the _____.

Helping You Remember

Describe how to find the height of a cylinder that has a volume of $2,211 \text{ mm}^3$ and a radius of 8 mm.

12-4 Volume of Pyramids, Cones, and Spheres

What You'll Learn

Skim Lesson 12-4. Predict two things you expect to learn based on the headings and the Key Concept boxes.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match each term with its definition by drawing a line to connect the two. (*Lesson 12-1*)

solid a three-dimensional figure with one circular base and a vertex connected by a curved side

polyhedron a three-dimensional figure

prism a solid with flat surfaces that are polygons

cone a polyhedron with one base that is a polygon

pyramid a polyhedron with two parallel congruent bases

New Vocabulary Fill in each blank with the correct term or phrase.

sphere ► A set of _____ in space that are a given _____ r from the _____.

Lesson 12-4 (continued)

Main Idea

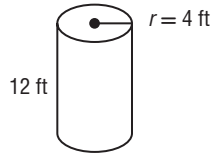
Details

Volume of a Cone

p. 684

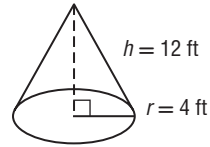
Compare the volume of a cylinder and a cone.

Step 1: Find the volume of the two figures.



$V =$

$V \approx$



$V =$

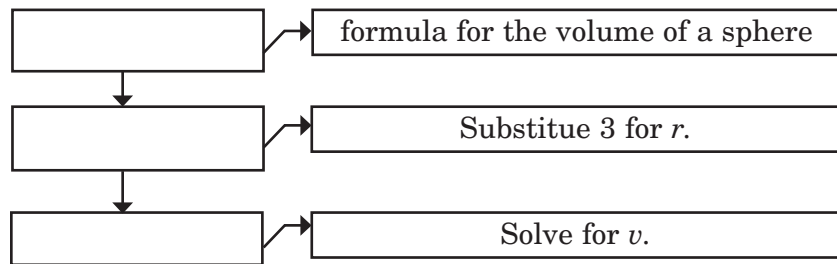
$V \approx$

Step 2: Make a conjecture about the relationship between the volume of a cylinder and the volume of a cone with the same height and radius.

Volume of a Sphere

pp. 684–685

Write out each step to find the volume of a sphere with $r = 3$ cm.



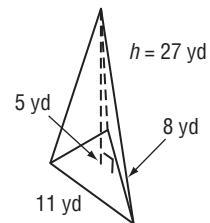
Helping You Remember

Describe each step in finding the volume of the pyramid at the right.

$V = \frac{1}{3}Bh$

$V = \frac{1}{3}(\frac{1}{2} \cdot 5 \cdot 8)27$

$V \approx 180$



12-5 Surface Area of Prisms

What You'll Learn

Scan the text in Lesson 12-5. Write two facts you learned about the surface area of prisms as you scanned the text.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to each definition. (*Lessons 5-1 and 12-1*)

- _____ ▶ the distance around a figure
- _____ ▶ a flat surface of a solid
- _____ ▶ one of two congruent faces of a prism

New Vocabulary Write the definition next to each term.

lateral face ▶ _____

lateral area ▶ _____

surface area ▶ _____

Vocabulary Link *Lateral* is a word that is used in everyday English. Find the definition of *lateral* using a dictionary. Explain how the English definition can help you remember how *lateral* is used in mathematics.

Lesson 12-5 (continued)

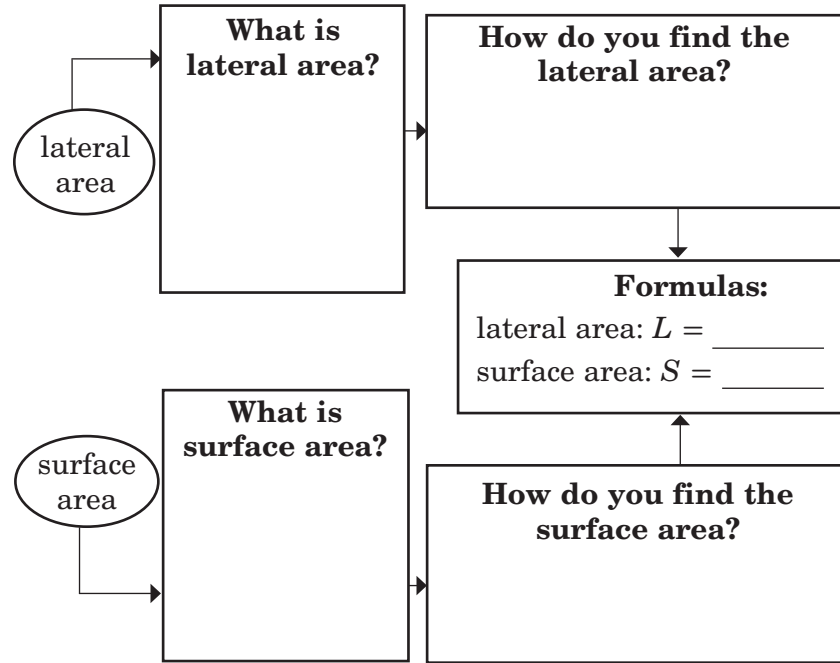
Main Idea

Details

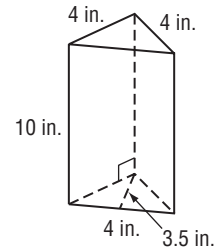
Prisms

pp. 691–692

Summarize information about *lateral* and *surface area* in the graphic organizer below.



Describe how to find the surface area of the figure below.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

How does drawing a net help you find the surface area of a prism? Draw a prism and its net to justify your answer.

12-6 Surface Area of Cylinders

What You'll Learn

Skim the lesson. Write two things you already know about the surface area of cylinders.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Fill in each blank with the correct term or phrase. (*Lesson 12-1*)

cylinder ▶ a three-dimensional figure with congruent, _____ bases that are circles connected by a _____ side

cone ▶ a three-dimensional figure with one _____ base and a _____ connected by a _____ side

vertex ▶ where _____ or more planes intersect at a _____

face ▶ a flat _____ of a _____

Vocabulary Link Cylinders are used in everyday life. List four examples of when the lateral area or surface area of a cylinder may be needed.

Lesson 12-6

Lesson 12-6 (continued)

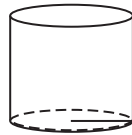
Main Idea

Surface Area of Cylinders

pp. 697–698

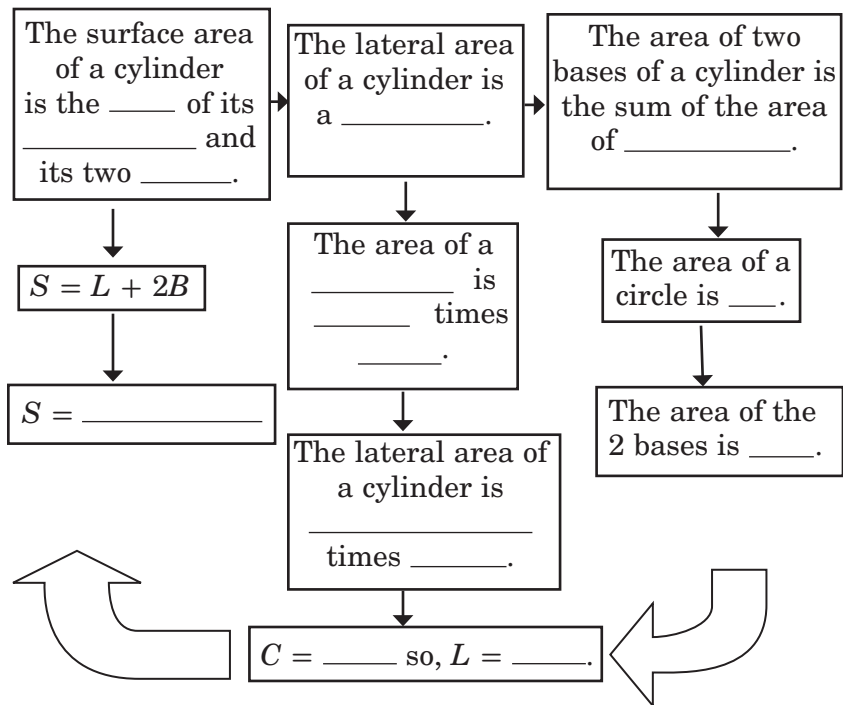
Details

Draw the net of the cylinder. Label the radius (r), height (h), and circumference (C) on the net.



Net

Fill in the blanks to complete the organizer about surface area of a cylinder.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

You want to decorate the side and bottom of a cylindrical flower pot with material. Do you need to calculate the surface area of the pot or the lateral area?

12-7 Surface Area of Pyramids and Cones

What You'll Learn

Skim the Examples for Lesson 12-7. Predict two things you think you will learn about the surface area of pyramids and cones.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term. (Lesson 12-5)

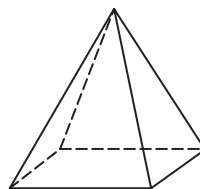
lateral face ▶ _____

lateral area ▶ _____

surface area ▶ _____

New Vocabulary Draw an arrow to the diagram that points the slant height of the pyramid. Then label it with the term *slant height*.

- slant height* ▶
- regular pyramid* ▶



This figure is a _____
_____ because it has
a base that is a regular
polygon.

Lesson 12-7

Lesson 12-7 (continued)

Main Idea

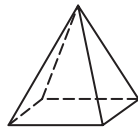
Details

Surface Area of Pyramids

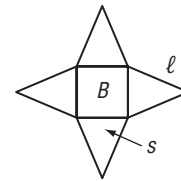
pp. 702–703

Draw the net of the pyramid. Label slant height (ℓ), base (B), and side length (s) of the base on the net.

Figure



Net



Surface Area of Cones

p. 704

Compare the volume of a cone and the surface area of a cone by filling out the chart. Sample answers are given.

Cone	Volume	Surface Area
Formula	$V = \frac{1}{3}\pi r^2 h$	$S = L + \pi r^2$
Words		
Example	Find the volume of a cone with a radius of 5 cm and a height of 7 cm. $V \approx$ _____	Find the surface area of a cone with a radius of 5 cm and a slant height of 7 cm. $S \approx$ _____

Helping You Remember

Prepare a script for a short presentation on how to find the surface areas of pyramids and cones. Be sure to include any necessary vocabulary terms in your explanation. You may wish to include diagrams with your presentation.

12-8 Similar Solids

What You'll Learn

Scan Lesson 12-8. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match the term with the definition by drawing a line to connect the two. (*Lessons 6-5 and 6-7*)

cross products an equation that states that two ratios or rates are equal

similar figures If $\frac{a}{b} = \frac{c}{d}$, then $ad = cb$.

proportion figures with congruent corresponding angles and proportional corresponding side lengths

New Vocabulary Fill in each blank with the correct term or phrase.

similar solid ▶ Two figures that have the same _____ and their _____ measures are _____.

Vocabulary Link Similar solids are seen in everyday life. Give an example of items that have the same shape but not necessarily the same size in real life.

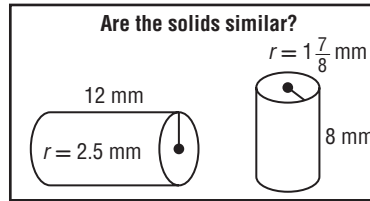
Lesson 12-8 (continued)

Main Idea

Identify Similar Solids
pp. 709–710

Details

Complete the organizer by filling in each blank to identify similar solids. Then complete the example.



Step 1:
Set up a _____.



Step 2:
Find the _____.



Step 3:
_____.
If the _____ are _____, the solids are _____.

Step 1:
 $\frac{\quad}{12} = \frac{1.875}{\quad}$



Step 2:
_____ = 12(1.875)



Step 3:
_____ ≠ 22.5
_____, the solids are _____.

Properties of Similar Solids
pp. 710–711

For each pair of solids listed in the table below, describe measurements you would need to determine if the pair is similar.

Pair of Solids	Measurements Needed
Rectangular Prisms	
Cylinders	
Square Pyramids	
Triangular Prisms	
Cones	

Helping You Remember

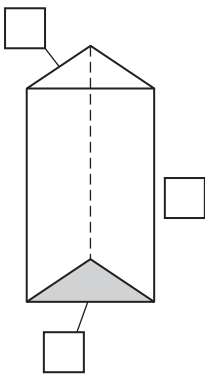
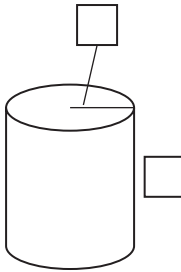
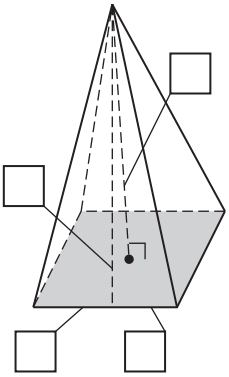
Describe the relationship between similar figures for surface area and volume.

CHAPTER
12

Surface Area and Volume

Tie It Together

Fill in the formulas for each solid. Label the appropriate variables on each figure.

	Prism	Cylinder	Pyramid
Volume			
Lateral Area			
Surface Area			
Diagram/Variables			

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.


 CHAPTER
12

Surface Area and Volume

Before the Test

Review the ideas you listed in the table at the beginning of the chapter. Cross out any incorrect information in the first column. Then complete the table by filling in the third column.

K What I know...	W What I want to find out...	L What I learned...

Math Online Visit *glencoe.com* to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 12.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 12 Study Guide and Review in the textbook.
- I took the Chapter 12 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- On handouts, homework, and workbooks that can be written in, underline and highlight significant information.


 CHAPTER
13

Statistics and Probability

Before You Read

Before you read the chapter, respond to these statements.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Before You Read	Statistics and Probability
	<ul style="list-style-type: none"> • The median of a set of data is the same thing as the average.
	<ul style="list-style-type: none"> • The range is the difference between the least and greatest numbers.
	<ul style="list-style-type: none"> • A histogram is a type of graph that uses bars.
	<ul style="list-style-type: none"> • Probability is expressed as a number between 1 and 100.
	<ul style="list-style-type: none"> • When something is likely to happen, it is certain.


FOLDABLES Study Organizer

Construct the Foldable as directed at the beginning of this chapter.


Note Taking Tips

- **When you take notes, it may be helpful to sit as close as possible to the front of the class.**
There are fewer distractions and it is easier to hear.
- **When taking notes on statistics, include your own statistical examples as you write down concepts and definitions.**
This will help you to better understand statistics.

CHAPTER
13

Statistics and Probability

Key Points

Scan the pages in the chapter and write at least one specific fact concerning each lesson. For example, in the lesson on measures of variation, one fact might be that the median of a set of data separates the set in half. After completing the chapter, you can use this table to review for your chapter test.

Lesson	Fact
13-1 Measures of Central Tendency	
13-2 Stem-and-Leaf Plots	
13-3 Measures of Variation	
13-4 Box-and-Whisker Plots	
13-5 Histograms	
13-6 Theoretical and Experimental Probability	
13-7 Using Sampling to Predict	
13-8 Counting Outcomes	
13-9 Permutations and Combinations	
13-10 Probability of Compound Events	

13-1 Measures of Central Tendency

What You'll Learn

Skim Lesson 13-1. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

New Vocabulary Fill in each blank with the missing term or phrase.

mode ▶ the _____ or _____ that occur _____

median ▶ the _____ when data is ordered from _____ to _____ or the _____ of the _____ two numbers

measures of central tendency ▶ describes the _____ of the data

mean ▶ the _____ of the data _____ by the _____ of items in the _____ set

Vocabulary Link *Median* is a word that is used in everyday English. Find the definition of *median* using a dictionary. Give two examples of how *median* might be used in everyday life.

Lesson 13-1 (continued)

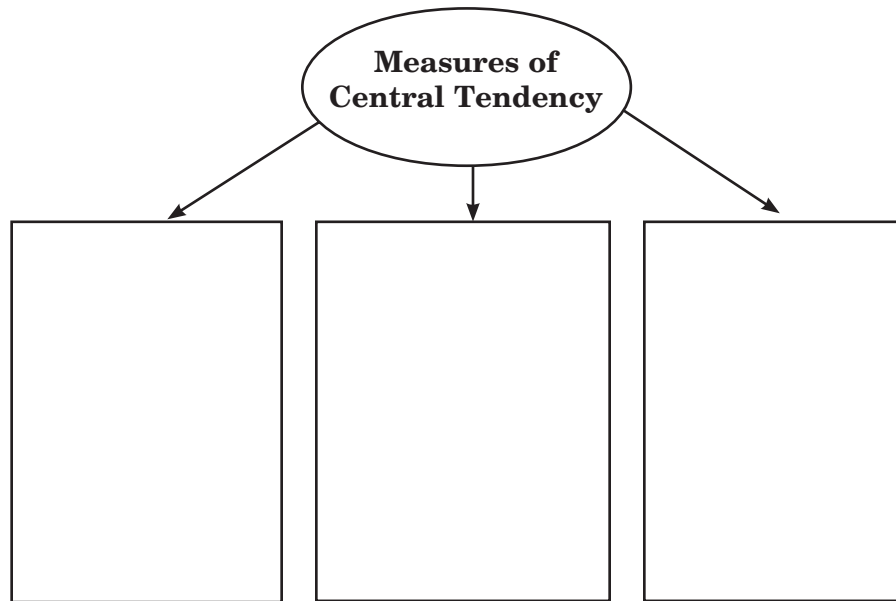
Main Idea

Details

Measures of Central Tendency

pp. 730–732

Complete the organizer. Write the three kinds of measures of central tendency with its definition. Then write a problem with the solution to show an example for each.



The heights of a group of friends are 54, 62, 48, 62, 58, and 58 inches. Fill in each blank to find the measures of central tendency.

1. Write the numbers in order from _____ to _____.
2. Find the _____ of the numbers and _____ by _____.
3. The mean is _____, the median is _____, and the mode is _____.

13-2 Stem-and-Leaf Plots

What You'll Learn

Scan Lesson 13-2. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Label the *stems* and *leaves* in both plots. Then name the two types of plots.

<i>stems</i> ▶	8 6 3	0	4 7 9	0	4 7 9
<i>leaves</i> ▶	0	1	3 7 7 9	1	3 7 7 9
	8 5 3 3	2	0 0 5 8	2	0 0 5 8
<i>stem-and-leaf plot</i> ▶	9 9 7 4	3	0 0 1 1 3	3	0 0 1 1 3 4 7
<i>back-to-back stem-and-plot</i> ▶	2 1	4	3 7	4	3 7
		5	1	5	1
			3 1 = 31		0 9 = 9

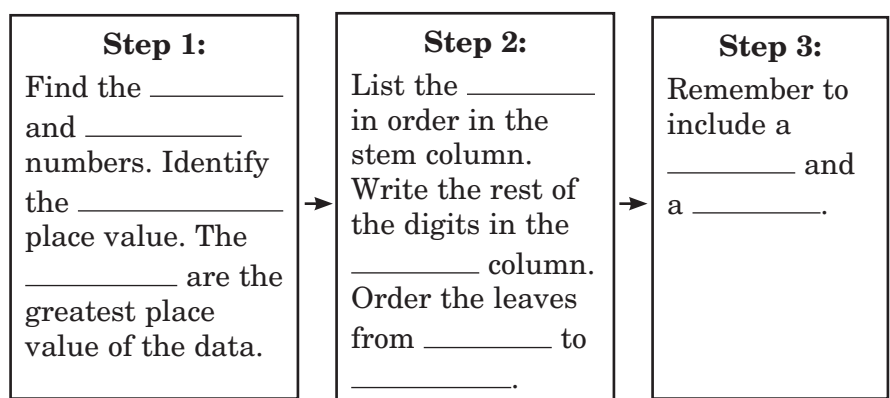
Lesson 13-2

Main Idea

Details

Display Data
p. 737

Explain the steps to construct a stem-and-leaf plot.



Lesson 13-2 *(continued)*

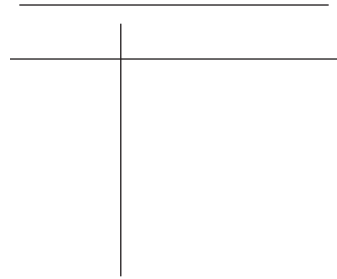
Main Idea

Details

Interpret Data
pp. 738–739

Complete the stem-and-leaf plot using the data in the table.

Books Checked Out Weekly					
115	113	125	145	119	117
101	156	154	118	154	132
100	122	106	111	126	130



What does the Stem '14' represent? _____

What is the greatest number of books checked out? _____

What is the mode of the data? _____

How many weeks does the data cover? _____

Helping You Remember

Measures of central tendency can be easily found using a stem-and-leaf plot. Explain how you could use the data in the stem-and-leaf plot below to find the mean, median, and mode. Then find the measures.

13-3 Measures of Variation

What You'll Learn

Skim the Examples for Lesson 13-3. Predict two things that you will learn about measures of variation.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to the definition. (Lesson 13-1)

_____ ▶

The middle number when data is ordered from least to greatest or the mean of the middle two numbers

New Vocabulary Fill in the diagram with correct terms.

range ▶

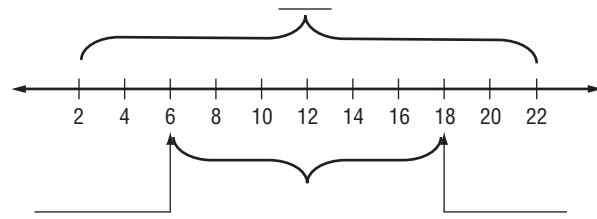
quartiles ▶

upper quartile ▶

lower quartile ▶

interquartile range ▶

outlier ▶



_____ are the values that divide the data into four equal parts.

An _____ is a value that is more than 1.5 times the value of the interquartile range beyond the quartiles.

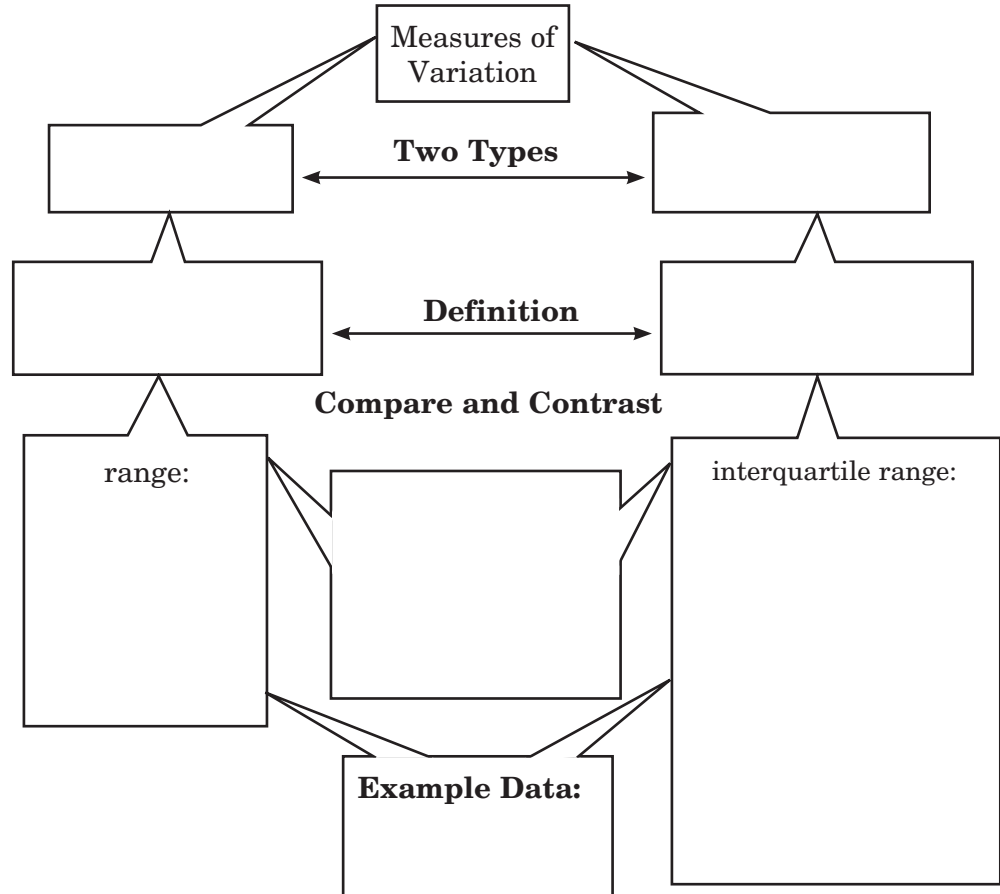
Lesson 13-3 (continued)

Main Idea

Details

Measures of Variation
pp. 743–745

Complete the diagram and the example.



Use Measures of Variation
pp. 745–746

Use the test scores from the table to answer the questions below.

Jackson	67	80	78	75	80	79	77	79	55
Terry	68	77	60	77	71	72	52	63	59

What is the range of Jackson’s and Terry’s scores? _____

What conclusions can be drawn from the ranges? _____

What are the interquartile ranges for each student?

What conclusions can be drawn from the interquartile ranges? _____

13-4 Box-and-Whisker Plots

What You'll Learn

Skim the lesson. Write two things you already know about box-and-whisker plots.

1. _____

2. _____

Active Vocabulary

New Vocabulary Fill in each blank with the correct term or phrase.

box-and-whisker plot ► uses a _____ to show the _____ of a set of _____; also known as a _____

Main Idea

Details

Display Data
p. 750

Complete the organizer to explain the steps to construct a box-and-whisker plot. Then complete the example.

<p>Step 1: Draw a _____ that includes the _____ and _____ values.</p>	<p>Data: 14, 33, 28, 8, 32, 36, 31</p>
↓	↓
<p>Step 2: Mark the _____ and _____ values, the _____, the _____ and _____. Check for _____.</p>	<div style="border: 1px solid black; height: 100px;"></div>
↓	↓
<p>Step 3: Draw the _____ and _____.</p>	<div style="border: 1px solid black; height: 100px;"></div>

Lesson 13-4 (continued)

Main Idea

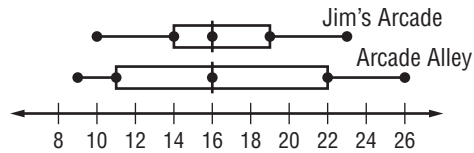
Interpret Box-and-Whisker Plots

p. 750

Details

Use the information from the box-and-whisker plot to answer each question.

Ages of Arcade Players



- Which arcade attracts a wider range of ages? _____
- What age is 25% of the age group at Jim's Arcade less than? _____
- Compare the median for both arcades. What can you conclude?

Helping You Remember

Describe in detail how to determine if an outlier exists in a data set.

13-5 Histograms

What You'll Learn

Scan the text in Lesson 13-5. Write two facts you learned about histograms.

1. _____

2. _____

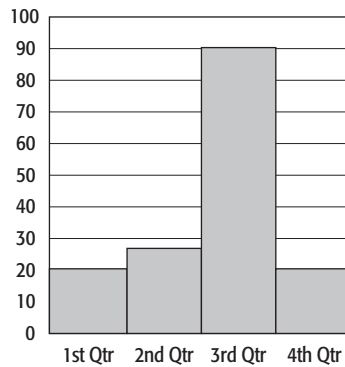
Active Vocabulary

Review Vocabulary Write the term under the correct display. (Lessons 13-2 and 13-4)

stem-and-leaf plot ▶

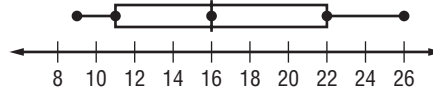
box-and-whisker plot ▶

histogram ▶



Stem	Leaf
0	4 7 9
1	3 7 7 9
2	0 0 5 8
3	0 3
4	3 7
5	1

3 | 3 = 33



New Vocabulary Write the term *histogram* under the correct display.

Vocabulary Link The data on a histogram is in equal intervals. Name three examples of data that could be displayed in a histogram.

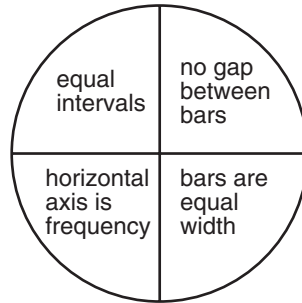
Lesson 13-5 (continued)

Main Idea

Details

Displayed Data
p. 757

Cross out the part of the concept circle that does not belong. Explain.

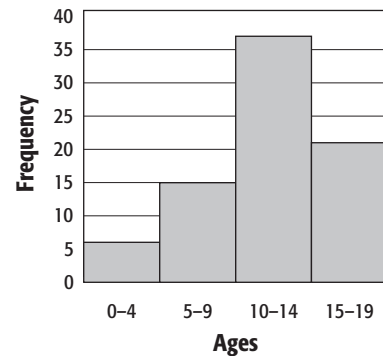


Interpret Data
p. 758

Use the information from the histogram to answer each question.

1. How many park visitors are under the age of 10? _____
2. How many more visitors are in the 10-14 age interval than in the 0-4 age interval? _____
3. About what percent of the visitors are between ages 15 and 19? _____

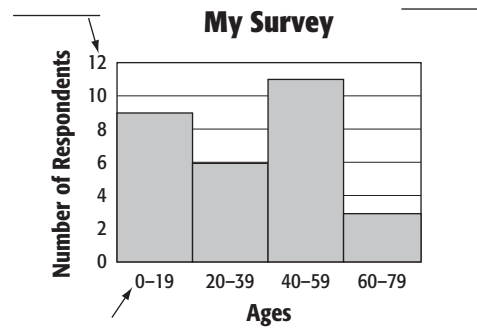
Ages of Park Visitors



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Label the histogram: frequency, bar, interval, and histogram. Make a frequency table showing the same information as the histogram.



13-6 Theoretical and Experimental Probability

What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. _____

2. _____

Active Vocabulary

New Vocabulary Fill in each blank with the correct term or phrase.

simple event ▶ one _____ or a collection of _____

outcomes ▶ the _____ of an event or experiment

sample space ▶ the set of all possible _____

random ▶ when each outcome is equally _____ to occur

probability ▶ a _____ that compares the number of _____ outcomes to the number of _____ outcomes

theoretical probability ▶ what _____ occur in an experiment

experimental probability ▶ what _____ occurs when repeating a probability experiment many times

odds in favor ▶ the _____ that compares the number of ways an event _____ occur to the number of ways that the event _____ occur

odds against ▶ the _____ that compares the number of ways an event _____ occur to the number of ways that the event _____ occur

Lesson 13-6 (continued)

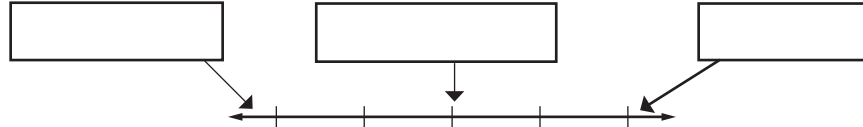
Main Idea

Details

Probability of Simple Events

pp. 765–767

Fill in each blank with the terms, *certain*, *impossible*, or *equally likely*. Then answer the questions below with *true* or *false*.



1. Probability is a ratio that compares the number of possible outcomes to the number of favorable incomes. _____
2. The closer a probability is to 1, the less likely it is to occur. _____
3. Experimental probability is what actually happens, while theoretical probability is what should happen. _____

Use a Sample to Make a Prediction

p. 767

The table shows the results from a survey that asked students about their favorite school subject. If 50 more students are picked at random, predict how many will *not* have a favorite subject of math?

Favorite Subject	
subject	frequency
science	22
social studies	22
language arts	26
math	30

Helping You Remember

Look up *theoretical* and *experimental* in the dictionary. How can the definitions help you to remember the difference between *theoretical* probability and *experimental* probability?

13-7 Using Sampling to Predict

What You'll Learn

Skim the lesson. Write two things you already know about using sampling to predict.

1. _____

2. _____

Active Vocabulary

New Vocabulary Write the definition next to each term.

sample ▶

population ▶

unbiased sample ▶

simple random sample ▶

stratified random sample ▶

systemic random sample ▶

biased sample ▶

convenience sample ▶

voluntary response sample ▶

Lesson 13-7

Lesson 13-7 (continued)

Main Idea

Details

Identify Sampling Techniques

pp. 771–772

Compare *biased* and *unbiased* sampling techniques by completing the chart below. Sample answers are given.

Technique	Biased Sampling	Unbiased Sampling
What is it?		
How are they the same?		
How are they different?		
What are some examples?		
Is it biased or unbiased?	on-line polls that request visitors to participate: _____ a surveyor who visits every 25 th house in neighborhood: _____	

Validating and Predicting Samples

pp. 772–773

A manufacturer makes 1500 phones and tests every 10th phone for defects. Of the phones, 24 were defective.

Is this sampling valid? _____

How many of the 1500 could you expect to be defective? _____

Helping You Remember

How can you remember the difference between *biased* and *unbiased* sampling?

13-8 Counting Outcomes

What You'll Learn

Skim Lesson 13-8. Predict two things that you expect to learn based on the headings and the Key Concept box.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Match each definition with the term by drawing a line to connect the two. (*Lesson 13-6*)

random the results of an event or experiment

sample space the set of all possible outcomes

probability when each outcome is likely to occur

outcomes a ratio that compares the number of favorable outcomes to the number of possible outcomes

New Vocabulary Fill in each blank with the missing term or phrase.

tree diagram ▶ a _____ that shows different _____ for an _____ or _____

Fundamental Counting Principle ▶ _____ the number of _____ to the _____ of _____

Lesson 13-8 *(continued)*

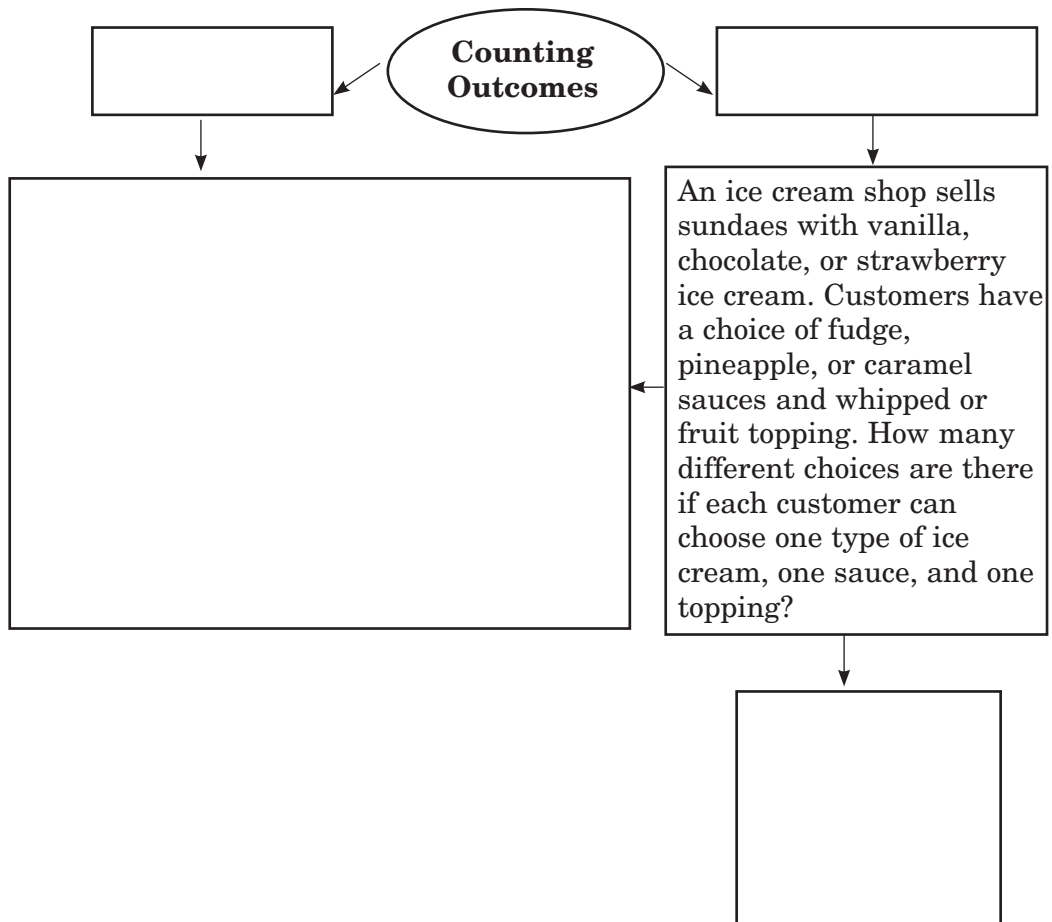
Main Idea

Details

Counting Outcomes

pp. 777–778

Write the two methods to find possible outcomes of an event. Then use each method to find the outcomes of the example.



Find the Probability of an Event

pp. 778–779

Find each probability using a number cube labeled 1 through 6.

1. What is the probability of tossing a 1 and then a 2?
2. What is the probability of tossing a number greater than 4 on two consecutive tosses?

Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

13-9 Permutations and Combinations

What You'll Learn

Scan Lesson 13-9. List two headings you would use to make an outline of this lesson.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the definition next to each term. (Lesson 13-6)

random ▶

probability ▶

theoretical probability ▶

experimental probability ▶

New Vocabulary Fill in each blank with the correct word or phrase.

permutations ▶ an _____ or listing in which order ____ important

combinations ▶ an _____ or listing in which order ____ important

Vocabulary Link The root of permutation is *permute*. Look up *permute* in the dictionary. How can the English definition help you remember the mathematic definition?

Lesson 13-9 (continued)

Main Idea

Details

Use Permutations

pp. 783–784

Fill in each blank to answer the question.

How many ways can a 4-digit PIN number be made using the numbers 0 through 9 if each number can only be used once?

$P(\underline{\quad} \underline{\quad}) =$

Write the notation for a permutation with 10 digits used 4 at a time.

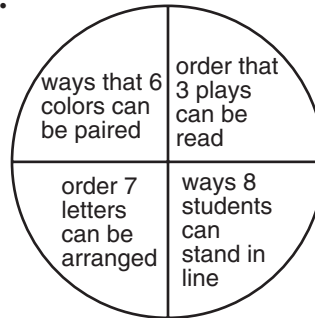
$P(\underline{\quad} \underline{\quad}) = \underline{\quad} \cdot \underline{\quad} \cdot \underline{\quad} \cdot \underline{\quad}$
 $= \underline{\quad}$

Use the Fundamental Counting Principle to find the number of possible permutations.

Use Combinations

pp. 784–785

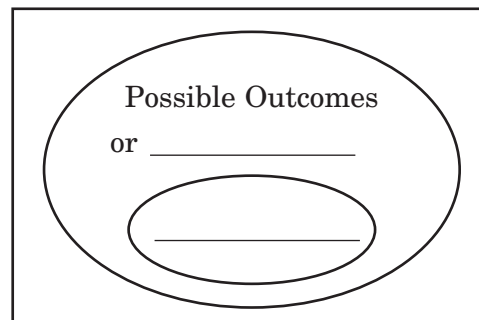
Cross out the part of the concept circle that does not belong. Then state the relationship between the remaining parts.



Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc.

Helping You Remember

Complete the diagram by writing the words *combinations* and *permutations* in the correct blanks. Then write a sentence based on the diagram stating the difference between permutations and combinations.



13-10 Probability of Compound Events

What You'll Learn

Skim the Examples for Lesson 13-10. Predict two things that you will learn about the probability of compound events.

1. _____

2. _____

Active Vocabulary

Review Vocabulary Write the term next to the definition. (*Lesson 13-6*)

- ▶ one outcome or a collection of outcomes

New Vocabulary Write the term next to each definition.

- ▶ The outcome of one event does not influence the outcomes of a second event.
- ▶ consists of two or more simple events
- ▶ two events that cannot happen at the same time
- ▶ The outcomes of one event affects the outcomes of a second event.

Vocabulary Link *Independent* and *dependent* are words that are used in everyday English. Describe an independent and dependent event that occurs in everyday life.

Lesson 13-10 (continued)

Main Idea

Probabilities of Independent and Dependent Events

pp. 790–791

Mutually Exclusive Events

p. 792

Details

Fill in each blank with *dependent* or *independent*.

1. A card is turned over and a number cube is tossed.

2. One marble is randomly picked from a bag. Then a second marble is chosen without replacing the first marble. _____
3. A scarf is randomly chosen from a bag. After putting the first scarf back into the bag, another scarf is chosen.

4. Two coins are tossed at the same time. _____
5. There are a dozen different flavored bagels in a bag. Jackson reaches in and grabs one. Then Iona grabs one.

Compare finding the probability of an independent or dependent event, and two mutually exclusive events. Sample answers are given.

	Independent Events	Dependent Events	Mutually Exclusive Events
What is it?			
How do you find the probability?			

**CHAPTER
13****Statistics and Probability****Tie It Together**

List concepts and vocabulary from the chapter that fit into each square.

Statistics	Data Displays
Sampling	Probability


**CHAPTER
13**

Statistics and Probability

Before the Test

Now that you have read and worked through the chapter, think about what you have learned and complete the table below. Compare your previous answers with these.

1. Write an **A** if you agree with the statement.
2. Write a **D** if you disagree with the statement.

Statistics and Probability	After You Read
<ul style="list-style-type: none"> • The median of a set of data is the same thing as the average. 	
<ul style="list-style-type: none"> • The range is the difference between the least and greatest numbers. 	
<ul style="list-style-type: none"> • A histogram is a type of graph that uses bars. 	
<ul style="list-style-type: none"> • Probability is expressed as a number between 1 and 100. 	
<ul style="list-style-type: none"> • When something is likely to happen, it is certain. 	

Math Online Visit glencoe.com to access your textbook, more examples, self-check quizzes, personal tutors, and practice tests to help you study for concepts in Chapter 13.

Are You Ready for the Chapter Test?

Use this checklist to help you study.

- I used my Foldable to complete the review of all or most lessons.
- I completed the Chapter 13 Study Guide and Review in the textbook.
- I took the Chapter 13 Practice Test in the textbook.
- I used the online resources for additional review options.
- I reviewed my homework assignments and made corrections to incorrect problems.
- I reviewed all vocabulary from the chapter and their definitions.



Study Tips

- If possible, rewrite your notes. Not only can you make them clearer and neater, rewriting them will help you remember the information.